

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
TOTAL	



General Certificate of Education
Advanced Level Examination
June 2011

Mathematics

MM05

Unit Mechanics 5

Friday 24 June 2011 1.30 pm to 3.00 pm

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The **final** answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.
- Take $g = 9.8 \text{ m s}^{-2}$, unless stated otherwise.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.



J U N 1 1 M M 0 5 0 1

Answer **all** questions in the spaces provided.

1 A simple pendulum of length L metres is set in motion. The period of the motion is 3 seconds.

(a) Find the frequency of the motion. *(1 mark)*

(b) Find the value of L . *(2 marks)*

QUESTION
PART
REFERENCE

Area with horizontal dotted lines for writing answers.



2 A particle moves along a straight line AB with simple harmonic motion. The point O is the mid-point of AB . When the displacement of the particle relative to O is x metres, its speed is $v \text{ m s}^{-1}$.

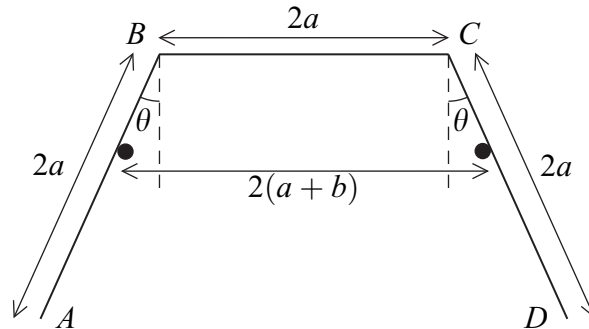
When $x = 3$, $v = 5$ and when $x = 6$, $v = 2.5$.

- (a) Show that the amplitude of the motion is $3\sqrt{5}$ metres. (4 marks)
- (b) Find the maximum speed of the particle during the motion. (4 marks)

QUESTION
PART
REFERENCE



- 4 Three uniform rods, AB , BC and CD , are each of length $2a$ and mass m . The rods are smoothly jointed at B and C and rest in equilibrium in a vertical plane. The rod BC is horizontal and the rods AB and CD rest on two small smooth fixed pegs. The pegs are at the same horizontal level and are a distance $2(a + b)$ apart. The rods AB and CD are inclined at an angle of θ to the vertical, as shown in the diagram below, where $0 < \theta < \pi$.



- (a) The gravitational potential energy is taken to be zero at the level of the pegs. Show that V , the total potential energy of the system, is given by

$$V = mg(3b \cot \theta - 2a \cos \theta) \quad (6 \text{ marks})$$

- (b) Hence show that any equilibrium positions of the system occur when

$$\sin^3 \theta = \frac{3b}{2a} \quad (5 \text{ marks})$$

- (c) It is given that $b = \frac{a}{3}$.

- (i) Find the two values of θ for which the system is in equilibrium. (3 marks)

- (ii) Show that, when the system is in equilibrium,

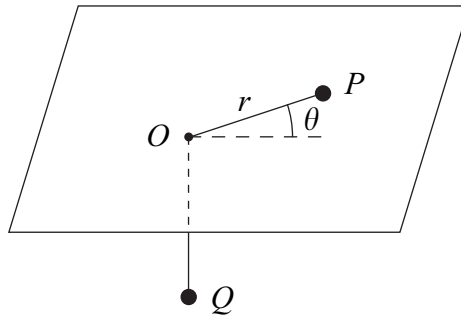
$$\frac{d^2V}{d\theta^2} = 6mga \cos \theta \quad (3 \text{ marks})$$

- (iii) Hence determine, for each of the values found in part (c)(i), whether the system is in stable or unstable equilibrium. (2 marks)

QUESTION
PART
REFERENCE



- 6** Two particles, P and Q , both of mass m , are attached to the ends of a light inextensible string. The string passes through a small hole, O , in a smooth horizontal table. The particle P is held in contact with the table at a distance a from O and the particle Q hangs at rest below the table. The particle P is projected horizontally with velocity $2\sqrt{ag}$ at right angles to the portion of string resting on the table. The polar coordinates of P during its subsequent motion are (r, θ) relative to O , as shown in the diagram below.



- (a)** Draw a diagram to show the forces acting on:
- (i)** the particle P ; (1 mark)
- (ii)** the particle Q . (1 mark)
- (b)** By considering the forces acting on Q , explain why
- $$T - mg = m\ddot{r}$$
- where T is the tension in the string. (2 marks)
- (c)** Hence show that $2\ddot{r} = r\dot{\theta}^2 - g$. (4 marks)
- (d)** Hence show that $2\ddot{r} = \frac{4a^3g}{r^3} - g$. (5 marks)
- (e)** Deduce that P will begin to move further away from O after it is set in motion. (2 marks)

QUESTION
PART
REFERENCE



QUESTION
PART
REFERENCE

A large rectangular area with horizontal dotted lines for writing, intended for student answers.

END OF QUESTIONS

Copyright © 2011 AQA and its licensors. All rights reserved.

