

### **General Certificate of Education**

## Statistics 6380

SS04 Statistics 4

# **Mark Scheme**

2009 examination – June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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#### Key to mark scheme and abbreviations used in marking

M	mark is for method				
m or dM	mark is dependent on one or more M marks and is for method				
A	mark is dependent on M or m marks and is for accuracy				
В	mark is independent of M or m marks and is for method and accuracy				
E	mark is for explanation				
√or ft or F	follow through from previous incorrect result	MC	mis-copy		
CAO	correct answer only	MR	mis-read		
CSO	correct solution only	RA	required accuracy		
AWFW	anything which falls within	FW	further work		
AWRT	anything which rounds to	ISW	ignore subsequent work		
ACF	any correct form	FIW	from incorrect work		
AG	answer given	BOD	given benefit of doubt		
SC	special case	WR	work replaced by candidate		
OE	or equivalent	FB	formulae book		
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme		
–x EE	deduct x marks for each error	G	graph		
NMS	no method shown	c	candidate		
PI	possibly implied	sf	significant figure(s)		
SCA	substantially correct approach	dp	decimal place(s)		

#### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

### **SS04**

Q	Solution	Marks	Total	Comments
1	X = number of days out of 200 when			
	delay occurs.			
(a)	$X \sim B(200, 0.005)$	B1	1	
(b)	, , ,	B1		
(~)	$P(X \ge 3) = 1 - P(X \le 2)$	M1		$P(X \ge 3) = 1 - P(X \le 2)$ using
		1V11		Poisson or binominal
	= 1 - 0.9197 = 0.0803	A1	3	AWRT
(c)	Poisson approximation to binomial with			
	large n	E1		
	and very small $p$ .	E1	2	
	Total		6	
2(a)	$\overline{x} = 32.75$ $s = 3.059$	B1		Allow 3.06 for sd
	$H_0: \mu = 30$			
	$H_1: \mu > 30$	B1		Both
	1 ,			
	Test statistic = $\frac{32.75 - 30}{3.059}$	N/1		( 20) /4
	3.059	M1		(x-30) / their sd Correct sd.
	$\sqrt{8}$	m1		
	= 2.543	A1		2.54 to 2.55 (B3 by calculator)
	v = 8 - 1 = 7	B1		Allow B1 total for $t = 2.896$
	t = 2.998	B1		Using $v = 8$
	2.543 < 2.998 so cannot reject H <sub>0</sub> .			
	There is not enough evidence at the 1%			
	significance level to say that the level of			
	nitrate pollution is a cause for	A1√	8	ft on ts and critical value
	environmental concern.			Must be 1-tailed test
(b)(i)	$H_0: p = 0.6$			
	$H_1: p < 0.6$	B1		Both
	Under $H_0$ , $X \sim B(42, 0.6)$			
	$\approx N(25.2, 10.08)$	В2		B1 mean; B1 variance
	- (			M1 if correct method with wrong <i>n</i>
	16.5-25.2			With the correct method with wrong n
	Test statistic = $\frac{10.3 - 23.2}{\sqrt{10.08}} = -2.74$	M1		
		A1		-2.75 to -2.73
	or $\frac{16-25.2}{\sqrt{10.08}} = -2.90$			-2.91 to -2.89
	$\sqrt{10.08}$			2.91 to 2.09
	Or using proportions,			
	$Y \sim N(0.6, 0.005714)$	(B2)		B1 if $\hat{p}$ used instead of $p$
	Test statistic = $\frac{\frac{16}{42} - 0.6}{\sqrt{0.005714}} = -2.90$			
	Test statistic = $\frac{42}{42}$ = -2.90	(M1)		
	$\sqrt{0.005714}$	(A1√)		ft on use of $\hat{p}$
	z = -2.3263	B1		Accept 2.33; ignore sign
				Allow $t = 2.423$
	ts < critical value so $H_0$ can be rejected.			
	There is evidence at the 1% level that			
	nitrate pollution is a cause for concern in	A1√	7	ft on ts and z
	less than 60% of the length of rivers in the			Exact binomial:
	region			$P(X \le 16) = 0.00338 < 0.01$ full marks
(ii)	Assume that the sections tested are chosen			, ,
(11)	at random or independent of each other	B1	1	
	Total	D1	16	
<u> </u>	1 Utai		10	

SS04 (cont)

Comments
eept 1.645, 1.64
*
for sample value $+ z \times sd$
for correct sd
ow M1 if 11.75 used
7 to 35.8, 58.2 to 58.3)
mparison of CI with previous mean.
two valid points. Clear explanation
ed on CI gets 2
ow B1 if CI based on 54 (or 13.5) and
or 11.75) compared with it
ow 0.587, 0.588
•
e or in (ii)
m of CI Here or in (ii)
ndard error
33 to 0.534, 0.64 to 0.642)
,
00 1 0 20 0 21 1 0 211
89 to 0.39, 0.51 to 0.511)
allowed for correct conclusion with
ne comparison of CIs

SS04 (cont)

Q	Solution	Marks	Total	Comments
( )	Two candidates so Yvonne needs > 50%	E1		May be implied
	of votes. Lower bound for $q > 0.5$ so it is likely that	E1		Indication that more than half of females
	a majority of females voted for her, but	Lı		vote for Yvonne
	the proportion of males could be well	E1		Doubtful whether more than half of males
	under a half.	Г1	4	will vote for Yvonne
	Can't be sure that Yvonne will win. (Result may depend on numbers of males	E1	4	Conclusion based on evidence of CIs
	and females who vote)			
	Total		13	
5	$X \sim N(110, 5^2)$			
	$Y \sim N(370, 12^2)$			
(a)	$X+Y \sim N(110+370, 5^2+12^2)$	M1		Means and variances added.
	=N(480, 169)	A1		B1 if mean wrong but variance correct
	$P(X+Y<500) = \Phi\left(\frac{500-480}{13}\right)$	M1		
	$=\Phi(1.538)$			1.538 to 1.54
	= 0.938	A1	4	AWRT 0.937 to 0.938
(b)	$3X \sim N(3 \times 110, 9 \times 5^2)$			
	$Y-3X \sim N(370-330, 12^2+225)$	B1		B1 for mean
		M2		M1 for $3^2 \times Var(X)$
				M1 for adding variances
	= N(40, 369)	A1		CAO
	P(Y > 3X) = P(Y - 3X > 0)	M1		
	$=1-\Phi\bigg(\frac{0-40}{\sqrt{369}}\bigg)$	m1		or equivalent
	$= \Phi(2.082) \\ = 0.981$	A1	7	AWRT
	- 0.981 <b>Total</b>	AI	7 11	AWKI

SS04 (cont)

SS04 (cont) O	Solution	Marks	Total	Comments
6(a)	$H_0: p = 0.5$	11202125	10001	
( )	$H_1: p > 0.5$	B1		Both
	Under $H_0$ , $X \sim B(14, 0.5)$	B1		Dotti
	$P(X \ge 11) = 1 - P(X \le 10)$	M1		
		1,11		
	= 1 - 0.9713			
	= 0.0287	A1		Accept 0.029
	0.0287 < 5% so result is significant at the 5% level.	E1		Can be gained without previous M mark
	Evidence suggests that more than half of			
	car park users think it will be too small.	A1√	6	ft on probability
	car park asers timik it will be too small.	711	O	it on productinty
(b)(i)	v = 15;  t = 2.131	D1		
` ` ` `	95% confidence limits for $\mu$ are:	B1		
	•			
	$59.9 \pm 2.131 \times \frac{7.83}{4}$	M1		
	·	m1	4	sd divided by 4
	giving (55.7, 64.1)	A1	4	(AWRT, 64 to 64.1)
(ii)	65 is above upper confidence limit.	E1		
(11)	Seems likely that the claim is true.	B1	2	
	3			
(c)(i)	Parent population is (discrete) Poisson but			
	with large mean so closely approximated			
	by normal distribution.	E1		
	Reasonable to accept that CI is valid.	B1	2	
(ii)	$Y \sim Po(65) \approx N(65, 65)$	B1		
(11)	(70.5.65)	Di		
	$P(Y > 78) = 1 - \Phi\left(\frac{78.5 - 65}{\sqrt{65}}\right)$	M1		B1 for 0.0534 using calculator (no cc)
	( √65 )	m1		Continuity correction attempted.
	$=1-\Phi(1.674)$			
	= 1 - 0.9529 = 0.0471	A1	4	0.047 to 0.0475; CAO
				B1 for exact Poisson (0.0504)
(d)	P(Y > 78) = probability that smaller car			
	park is full.	E1		
	As $\mu$ was taken at the highest reasonable	E1		Significance of $\mu$ used
	value, this is a small probability.	E1	1	Assessment of probability  Regard on argument from $P(X > 78)$
	It seems likely that the car park will not be too small.	B1	4	Based on argument from $P(X > 78)$ , not CI for mean
	oc too sinan.			P(X>78) small so car park will not be
				too small gets E1 B1
	Total		22	2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2
	TOTAL		75	