

General Certificate of Education (A-level) January 2011

## Statistics

SS04

## (Specification 6380)

Statistics 4

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## Key to mark scheme abbreviations

| M | mark is for method |
| :---: | :---: |
| m or dM | mark is dependent on one or more M marks and is for method |
| A | mark is dependent on M or m marks and is for accuracy |
| B | mark is independent of M or m marks and is for method and accuracy |
| E | mark is for explanation |
| Vor ft or F | follow through from previous incorrect result |
| CAO | correct answer only |
| CSO | correct solution only |
| AWFW | anything which falls within |
| AWRT | anything which rounds to |
| ACF | any correct form |
| AG | answer given |
| SC | special case |
| OE | or equivalent |
| A2,1 | 2 or 1 (or 0 ) accuracy marks |
| -x EE | deduct $x$ marks for each error |
| NMS | no method shown |
| PI | possibly implied |
| SCA | substantially correct approach |
| c | candidate |
| sf | significant figure(s) |
| dp | decimal place(s) |

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

\begin{tabular}{|c|c|c|c|c|}
\hline Q \& Solution \& Marks \& Total \& Comments \\
\hline 1(a) \& \begin{tabular}{l}
\[
p=114 / 250=0.456
\] \\
\(90 \%\) confidence interval for \(p\)
\[
\begin{aligned}
\& 0.456 \pm 1.6449 \sqrt{ } 0.456 \times 0.544 / 250 \\
\& 0.456 \pm 0.0518 \\
\& 0.404 \sim 0.508
\end{aligned}
\] \\
Values > 0.5 lie in the interval, as do values less than 0.5 . Claim may or may not be true.
\end{tabular} \& B1
M1B1
m1
A1

E1 $\checkmark$
E1 \& 5

2 \& | B1 114/250 acf |
| :--- |
| M1 method for s.d. |
| B1 1.6449 (1.64 ~ 1.65) |
| m1 method - allow incorrect |
| $z$-value |
| A1 0.404 ( $0.4035 \sim 0.4045$ ) and |
| 0.508 ( $0.507 \sim 0.508$ ) |
| allow in $\pm$ form |
| E1 $\sqrt{ } 0.5(><)$ lies in interval |
| E1 claim unproven | <br>

\hline \& Total \& \& 7 \& <br>

\hline 2(a) \& | $\bar{x}=22.45 \quad \mathrm{~s}=2.034$ |
| :--- |
| 95\% confidence interval for mean $\begin{aligned} & 22.45 \pm 2.262 \times 2.034 / \sqrt{ } 10 \\ & 22.45 \pm 1.455 \quad(1.45 \text { to } 1.46) \\ & \quad 21.0 \sim 23.9 \end{aligned}$ | \& \[

$$
\begin{gathered}
\text { B1 } \\
\text { B1B1 } \\
\text { M1m1 } \\
\text { A1 }
\end{gathered}
$$
\] \& 6 \& ```

B1 22.45 (22.4 ~ 22.5) and
2.034 ( 2.03 ~ 2.04)
B1 9df
B1 2.262
M1 method for c.i - their s.d. and
$t$-value
m 1 correct method for c.i. their
$t$-value
A1 21.0 ( 20.95 ~ 21.05) and
23.9 (23.85~23.95)
allow in $\pm$ form

``` \\
\hline (b) & 95\% confidence interval for mean
\[
\begin{aligned}
18.27 & \pm 1.96 \times 1.638 / \sqrt{ } 55 \\
18.27 & \pm 0.433 \\
17.9 & \sim 18.7
\end{aligned}
\] & \[
\begin{aligned}
& \text { B1 } \\
& \text { M1 } \\
& \text { A1 }
\end{aligned}
\] & 3 & \begin{tabular}{l}
B1 1.96 or 2.004 ~ 2.009 \\
M1 method for c.i \\
A1 17.9 ( \(17.8 \sim 17.9\) ) and 18.7 ( 18.65 ~ 18.75) allow in \(\pm\) form
\end{tabular} \\
\hline (c) & \begin{tabular}{l}
Evidence to support Olivia's claim for this rodent as lower limit of confidence interval for rodents on island is above upper limit of confidence interval on mainland. \\
Only one island examined and no evidence for other species
\end{tabular} & \begin{tabular}{l}
E1 \\
E1 \\
E1
\end{tabular} & 3 & \begin{tabular}{l}
E1 statement supported for this rodent \\
E1 relevant comparison of confidence intervals \\
E1 note of caution
\end{tabular} \\
\hline & Total & & 12 & \\
\hline 3(a) & \begin{tabular}{l}
\(\mathrm{H}_{0}: p=0.3 \mathrm{H}_{1}: p<0.3\) \\
\(\mathrm{B}(20,0.3)\)
\[
\mathrm{P}(\leq 4)=0.2375
\] \\
Accept \(\mathrm{H}_{0}\), since \(0.2375>0.1\) \\
No significant evidence to support newspapers articles claim. \\
\(p\) may not be constant - may depend on cyclist/speed/weather. Events may not be independent - 2 cyclists may arrive together
\end{tabular} & \[
\begin{gathered}
\hline \text { B1 } \\
\text { B1 } \\
\text { M1m1 } \\
\text { A1 } \checkmark \\
\text { A1 } \checkmark \\
\\
\\
\text { E1 }
\end{gathered}
\] & 6 & \begin{tabular}{l}
B1 hypotheses \\
B1 attempted use of \(\mathrm{B}(20,0.3)\) \\
M1 attempt to find \(\mathrm{P}(\leq 4)\) m1 0.2375 ( \(0.237 \sim 0.238\) ) \\
A1 \(\checkmark\) Conclusion - their figures A1 \(\sqrt{ }\) Conclusion in context \\
E1 relevant suggestion
\end{tabular} \\
\hline & Total & & 7 & \\
\hline
\end{tabular}

\section*{SS04(cont)}


SS04(cont)
\begin{tabular}{|c|c|c|c|c|}
\hline Q & Solution & Marks & Total & Comments \\
\hline \multirow[t]{4}{*}{\[
\begin{array}{r}
5(\mathbf{a}) \\
\text { (i) } \\
\text { (ii) }
\end{array}
\]} & B(85,0.62) & B1 & \multirow[t]{3}{*}{1} & \multirow[t]{3}{*}{```
B1 \(n=85 p=0.62\) - may be implied
    later
B1 52.7 cao
M1 method for s.d. or variance
```} \\
\hline & \(\mathrm{B}(85,0.62) \rightarrow\) Normal mean 52.7 & B1 & & \\
\hline & \[
\begin{aligned}
& \text { s.d. }=\sqrt{ } 85 \times 0.62 \times 0.28=4.475 \\
&(\text { variance }=20.026)
\end{aligned}
\] & M1 & & \\
\hline & \[
\begin{aligned}
& z=(50.5-52.7) / 4.475=-0.492 \\
& \mathrm{P}(>50)=0.689
\end{aligned}
\] & \[
\underset{\text { A1 }}{\text { m1 }}
\] & 5 & \begin{tabular}{l}
m1 method for \(z\) - ignore cc \\
m 1 attempt at cc \\
A1 0.689 ( 0.687 ~ 0.69)
\end{tabular} \\
\hline \multirow[t]{4}{*}{(b)(i)} & \(\mathrm{H}_{0}: \lambda=7 \mathrm{H}_{1}: \lambda<7\) & B1 & & B1 hypotheses \\
\hline & \(\mathrm{P}(X \leq 3)=0.0818\) & M1 & & M1 attempt to calculate \(\mathrm{P}(X \leq 3)\) using Poisson \\
\hline & \begin{tabular}{l}
\[
0.0818<0.1
\] \\
reject \(\mathrm{H}_{0}\) :
\end{tabular} & & & \begin{tabular}{l}
A1 0.0818 \\
A1 \(\sqrt{ }\) conclusion
\end{tabular} \\
\hline & significant evidence to support Mervin's belief that there has been a decrease in the number of volunteers. & A1 \(\checkmark\) & 4 & A1 \(\sqrt{ }\) conclusion \\
\hline \multirow[t]{6}{*}{(b)(ii)} & \(\mathrm{H}_{0}: \lambda=42 \mathrm{H}_{1}: \lambda<42\) & B1 & & B1 hypotheses - allow \(\lambda=7\) etc; do not penalise same mistake twice \\
\hline & \[
\begin{aligned}
& \mathrm{Po}(42) \rightarrow \text { Normal mean } 42 \\
& \text { s.d. }=\sqrt{42}=6.481 \text { (variance }=42) \\
& z=(33.5-42) / 6.481=-1.31
\end{aligned}
\] & \[
\begin{aligned}
& \mathrm{M} 1 \\
& \mathrm{~m} 1 \\
& \mathrm{~m} 1
\end{aligned}
\] & & M1 attempt at normal approximation to Poisson \\
\hline & \[
\begin{aligned}
& {[(33-42) / 6.481=-1.39]} \\
& \text { c.v. } z=-2.3263
\end{aligned}
\] & A1 & & m 1 method for \(z\) - ignore incorrect sign/cc \\
\hline & Accept \(\mathrm{H}_{0}\) : No significant evidence to & A1 \(\checkmark\) & \multirow[b]{2}{*}{8} & A1-1.31 ( \(-1.3 \sim-1.4)\) \\
\hline & show mean less than 7 per week. & A1 \(\checkmark\) & & B1 use of sig level \(\leq 5 \%\) \\
\hline & \begin{tabular}{l}
Carmen should not authorise advert. \\
Exact Poisson P( \(\leq 33)=0.0912\) \\
allow B1 M0 m0 m0 A0 B1A1 \(\checkmark\) A1 \(\checkmark\)
\end{tabular} & & & \begin{tabular}{l}
A1 \(\checkmark\) conclusion, their sig level must be compared with lower tail of \(z\) \\
A1 \(\sqrt{ }\) in context
\end{tabular} \\
\hline \multirow[t]{2}{*}{(iii)} & Concluding there has been a decrease & B1 & \multirow[b]{2}{*}{2} & \multirow[t]{2}{*}{B1 idea of Type I error B1 in context} \\
\hline & in the number of applications when there has not & B1 & & \\
\hline \multirow[t]{2}{*}{(iv)} & Carmen wants very convincing & E1 & \multirow[b]{2}{*}{2} & \multirow[t]{2}{*}{\(\mathrm{E} 1 \leq 1 \%\) used E1 justification} \\
\hline & evidence, so low risk of Type I error required. & E1 & & \\
\hline & Total & & 22 & \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|}
\hline Q & Solution & Marks & Total & Comments \\
\hline \begin{tabular}{l}
\[
6(\mathrm{a})
\] \\
(i) \\
(ii)
\end{tabular} & \begin{tabular}{l}
\(T_{2}\) : \\
mean \(=0.25+0.25=0.5\) \\
variance \(=0.02^{2}+0.02^{2}=0.0008\)
\end{tabular} & \[
\begin{aligned}
& \text { B1 } \\
& \text { B1 }
\end{aligned}
\] & \[
\begin{aligned}
& 1 \\
& 1
\end{aligned}
\] & \begin{tabular}{l}
B1 0.5 cao \\
B1 method ag
\end{tabular} \\
\hline (iii) & \[
\begin{aligned}
& T_{5}: \text { normal } \\
& \quad \text { mean }=5 \times 0.25=1.25 \\
& \text { variance }=5 \times 0.02^{2}=0.002 \\
& \text { s.d. }=0.04472
\end{aligned}
\] & M1A1 & 2 & M1 method for variance or s.d. A1 1.25 and 0.002 cao (or 0.0447 (0.0447~0.045) \\
\hline (b)(i) & \[
z=(1.2-1.25) / 0.04472=-1.118
\] probability less than coffee used less than 1.2 litres \(1-0.868=0.132\) & \begin{tabular}{l}
M1 \\
A1
\end{tabular} & 2 & M1 method - allow wrong tail A1 0.132 ( \(0.131 \sim 0.134)\) \\
\hline \multirow[t]{3}{*}{(ii)} & \[
\] & \[
\begin{gathered}
\mathrm{B} 1 \\
\mathrm{M} 1 \mathrm{~m} 1 \\
\mathrm{~m} 1
\end{gathered}
\]
\[
\mathrm{m} 1
\] & & \begin{tabular}{l}
B1 0.05 cao \\
M1 use of \(0.5^{2} \times 0.15^{2}\) \\
m 1 method for variance or s.d. - \\
their (a)(iii)
\end{tabular} \\
\hline & \begin{tabular}{l}
\[
z=(0-0.05) / \sqrt{ } 0.007625=-0.573
\] \\
probability Manesh uses less than half the coffee \(=1-0.717\)
\end{tabular} & \[
\begin{aligned}
& \text { M1 } \\
& \text { m1 }
\end{aligned}
\] & & \begin{tabular}{l}
m 1 completely correct method for variance or s.d. \\
M1 attempting \(T_{5}-0.5 Y<0\), their
\end{tabular} \\
\hline & \(=0.283\) & A1 & 7 & m1 completely correct method disallow wrong tail A1 \(0.283(0.28 \sim 0.285)\) \\
\hline \multicolumn{2}{|r|}{Total} & & 13 & \\
\hline & TOTAL & & 75 & \\
\hline
\end{tabular}```

