



General Certificate of Education (A-level)
June 2012

Mathematics

MS03

(Specification 6360)

Statistics 3

Mark Scheme

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Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
✓or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
–x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MS03

Q	Solution	Marks	Total	Comments
1(a)	$r = 0.665$ to 0.666 $r = 0.6$ to 0.7	B2 (B1)	2	AWFW AWFW (0.66577)
	Alternative Use of a correct formula	(M1)		$\Sigma x = 20.40$ $\Sigma x^2 = 34.785$ $\Sigma xy = 49.1155$ $\Sigma y = 28.86$ $\Sigma y^2 = 69.4698$ $S_{xx} = 0.105$ $S_{yy} = 0.0615$ $S_{xy} = 0.0535$
	$r = 0.665$ to 0.666	(A1)		
	(b) $H_0: \rho = 0$ $H_1: \rho > 0$	B1		Both; do not accept in terms of r but accept in words
	SL $\alpha = 0.01$ (1%) CV $r = (+)0.658$	B1		AWRT (0.6581) $H_1: \rho \neq 0 \Rightarrow CV = (\pm)0.7079$
	Calculated $r = 0.666 >$ Tabulated r	M1		Comparison
	Evidence , at 1% level, of a positive correlation between the neck length and the tail length of mature male giraffes	A1F	4	F on r and CV At 1% level, reject hypothesis of no correlation
Total			6	
2(a)	$H_0: \mu_F = \mu_M$ $H_1: \mu_F \neq \mu_M$	B1		Both; allow suffices of 1 & 2 or X & Y
	SL $\alpha = 0.01$ (1%) CV $z = 2.57$ to 2.58	B1		AWFW (2.5758)
	$z = \frac{\bar{f} - \bar{m}}{\sqrt{\frac{s_F^2}{n_F} + \frac{s_M^2}{n_M}}} = \frac{22.0 - 21.6}{\sqrt{\frac{1.31^2}{50} + \frac{0.702^2}{75}}}$	M1		Numerator
		M1		Denominator; allow $\div 49$ and $\div 74$ but not pooling
	1.95 to 2(0)	A1		AWFW (1.98)
	No evidence , at 1% level, to suggest that there is a difference between mean lengths	A1F	6	F on CV and z -value allow following pooling
(b)	Diameter, thickness, girth, width, weight, shape, colour, texture	B1	1	Accept any sensible alternative but not 'quality'
Total			7	

MS03 (cont)

Q	Solution	Marks	Total	Comments
3(a)(i)	$P(S \cap U) = 0.15 \times 0.10 = \mathbf{0.015}$	B1	1	CAO
(ii)	$P(O \cap \geq 2) = (0.40 \times 0.50) + (0.45 \times 0.40) + (0.15 \times 0.70)$ $= 0.20 + 0.18 + 0.105 = \mathbf{0.485}$	M1 A1	2	≥ 1 term correct; may be implied CAO
(iii)	$P(U) = (0.40 \times 0.15) + (0.45 \times 0.05) + (0.15 \times 0.10) \text{ or (i)}$ $= 0.06 + 0.0225 + 0.015 = \mathbf{0.097 \text{ to } 0.098}$	M1 A1	2	≥ 2 terms correct; may be implied AWFW (0.0975)
(iv)	$P(D U) = \frac{P(D \cap U)}{P(U)} = \frac{0.40 \times 0.15}{\text{(iii)}}$ $= \frac{0.06}{0.0975} = \mathbf{0.612 \text{ to } 0.619}$	M1 A1	2	May be implied AWFW (0.61538)
(v)	$P(S O) = \frac{0.15 \times (1 - 0.10)}{1 - \text{(iii)}} = \frac{0.135}{0.9025}$ $= \mathbf{0.149 \text{ to } 0.15}$	M1 M1 A1	3	Numerator Denominator AWFW (0.14958)
(b)	$P(D \cap T \cap S O)$ $= \frac{0.40 \times 0.85}{1 - \text{(iii)}} \times \frac{0.45 \times 0.95}{1 - \text{(iii)}} \times \text{(v)} \times 3!$ $= \frac{0.34 \times 0.4275 \times 0.135 \times 6}{0.9025^3}$ <p>or</p> $= 0.3767 \times 0.4737 \times 0.1496 \times 6$ $= \mathbf{0.16}$	M1 M1 M1 A1	4	≥ 2 terms correct in numerator (1 – (iii)) in denominator 3! or 6 or 3 AWRT (0.16016)
Total			14	

MS03 (cont)

Q	Solution	Marks	Total	Comments
4	$H_0: \lambda = 2.6$ (650) $H_1: \lambda > 2.6$ (650) SL $\alpha = 0.05$ (5%) CV $z = 1.64$ to 1.65 $\hat{\lambda} = \frac{688}{250} = 2.75(2)$ $z = \frac{2.752 - 2.6}{\sqrt{\frac{2.6}{250}}} = \frac{688 - 650}{\sqrt{650}} = 1.47$ to 1.49 $p\text{-value} = 0.068$ to $0.071 > 0.05$ No evidence , at 5% level, to support manager's suspicion	B1 B1 B1 M1 A1 (M1) A1F	6	Both; accept μ instead of λ AWFW (1.6449) Allow 1.96 iff $H_1: \lambda \neq 2.6$ AWRT (2.752) Can be implied by use of 688 Allow use of 2.752 or 688 or 687.5 in denominator AWFW Use of $P(X \geq 688 \lambda = 650) = 0.072 \Rightarrow M0 A0 (M1) AF1$ F on CV and z -value
Total			6	
5(a)	$\hat{p} = \frac{68}{125} = 0.544$ 98% $\Rightarrow z = 2.32$ to 2.33 Approximate CI for p is $0.544 \pm 2.3263 \times \sqrt{\frac{0.544 \times 0.456}{125}}$ $0.544 \pm (0.103$ to $0.104)$ or $(0.44$ to $0.441, 0.647$ to $0.65)$ $(44\%, 65\%)$	B1 B1 M1 A1F A1 A1	6	CAO; or equivalent AWFW (2.3263) F on \hat{p} and z CAO/AWFW May be implied by correct answer AWFW AWRT
(b)	Require $2 \times 2.3263 \times \sqrt{\frac{p(1-p)}{n}} \leq 0.1$ (10%) Thus $\sqrt{n} = 22.1$ to 23.3 $n = 490, 495, \dots, 545$	M1 A1 M1 A1	4	Allow 'no 2' and FT on CI from (a) Allow $p = 0.44$ to 0.65 Attempted solution for \sqrt{n} or n Must be to 'nearest 5'
Total			10	

MS03 (cont)

Q	Solution	Marks	Total	Comments
6(a)(i)	$M = U + V$ $E(M) = 13 + 15 = \mathbf{28}$ $V(M) = 3^2 + 6^2$ $+ 2 \times 3 \times 6 \times (-0.6)$ $= 9 + 36 - 21.6 = \mathbf{23.4}$	B1 M1 M1 A1	4	CAO Allow 'no 2' CAO
(ii)	$D = W - 2U$ $E(D) = 24 - 2 \times 13 = \mathbf{-2}$ $V(D) = 4^2 + (2^2 \times 3^2)$ $= 16 + 36 = \mathbf{52}$	B1 M1 A1	3	CAO CAO
(iii)	$T = M + W + X$ $E(T) = 28 + 24 + 9 = \mathbf{61}$ $V(T) = 23.4 + 4^2 + 2^2 = \mathbf{43.4}$	B1F B1F	2	F on $E(M)$ from (a)(i) F on $V(M)$ from (a)(i)
(b)(i)	$P(M = 30) = \mathbf{0}$	B1	1	CAO
(ii)	$P(W > 2U) = P(D > 0) = P\left(Z > \frac{0 - (-2)}{\sqrt{52}}\right)$ $= P(Z > 0.28) = 1 - 0.61026$ $= \mathbf{0.389 \text{ to } 0.394}$	M1 m1 A1	3	Standardising 0 using c's $E(D)$ & c's $V(D)$ from (a)(ii) Area change AFWW (0.39076)
(iii)	$P(50 < T < 70) =$ $P\left(Z < \frac{70 - 61}{\sqrt{43.4}}\right) - P\left(Z < \frac{50 - 61}{\sqrt{43.4}}\right)$ $= P(Z < \mathbf{1.37}) - P(Z < \mathbf{-1.67})$ $= 0.91466 - (1 - 0.95254)$ $= \mathbf{0.865 \text{ to } 0.87}$	M1 A1 m1 A1	4	Standardising 70 & 50 using c's $E(T)$ & c's $V(T)$ from (a)(iii) AWRT either Area change AFWW (0.86657)
	Total		17	

MS03 (cont)

Q	Solution	Marks	Total	Comments
7(a)(i)	$X \sim B(n, p)$			
	$E(X) = \sum_{x=0}^n x \times \binom{n}{x} p^x (1-p)^{n-x}$	M1		Used; ignore limits until A1
	$= np \times \sum_{x=1}^{n-1} \frac{(n-1)!}{(x-1)!(n-x)!} p^{x-1} (1-p)^{n-x}$	M1		Factor of np plus p^x to p^{x-1} , $n!$ to $(n-1)!$ and $x!$ to $(x-1)!$ Ignore limits until A1
	$= np \times \sum_{x=1}^{n-1} B(n-1, p) = np$	A1	3	Fully correct and complete derivation AG
(ii)	$\text{Var}(X) = E(X^2) - [E(X)]^2$			
	$= E[X(X-1)] + E(X) - [E(X)]^2$	M1		Used
	$= n(n-1)p^2 + np - n^2p^2 = np(1-p)$	A1	2	(Other derivations are possible) Fully correct and complete derivation
(b)(i)	$\binom{n}{m} p^m (1-p)^{n-m} \geq \binom{n}{m-1} p^{m-1} (1-p)^{n-m+1}$	M1		Stated or used
	$\frac{n!}{m!(n-m)!} p^{n-m} \geq \frac{n!}{(m-1)!(n-m+1)!} (1-p)^{n-m+1}$	m1		Expanding $\binom{n}{m}$ and $\binom{n}{m-1}$
	$(n-m+1)p \geq m(1-p)$	A1		Simplification
	$np - mp + p \geq m - mp$			
	$m \leq (n+1)p$	A1	4	Fully correct and complete derivation AG
(ii)	$B(10, 0.65)$			
	$(n+1)p = 7.15$ and $(n+1)p - 1 = 6.15$	M1		Can be implied by '7'
	$m = 7$	A1		CAO
	$B(35, 0.5)$			
	$(n+1)p = 18$ and $(n+1)p - 1 = 17$	(M1)		Can be implied by '17 or 18'
	$m = 17$ and 18	A1	3	CAO; accept 'or'
(c)	$Y \sim B(4000, 0.00095) \approx \text{Po}(3.8)$	B1		May be implied
	$k = 3$	B1		CAO; may be implied
	$P(Y \leq 3) = 0.473$ to 0.474	B1	3	AWFW (0.4735)
	SC: $k = 4 \Rightarrow P(Y \leq 4) = 0.667$ to 0.668 Award B1 B0 B1			AWFW (0.6678)
	Total		15	
	TOTAL		75	