



**General Certificate of Education**

**Mathematics 6360**

**MPC4      Pure Core 4**

**Mark Scheme**

*2007 examination - January series*

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## Key to mark scheme and abbreviations used in marking

|              |                                                                    |     |                            |
|--------------|--------------------------------------------------------------------|-----|----------------------------|
| M            | mark is for method                                                 |     |                            |
| m or dM      | mark is dependent on one or more M marks and is for method         |     |                            |
| A            | mark is dependent on M or m marks and is for accuracy              |     |                            |
| B            | mark is independent of M or m marks and is for method and accuracy |     |                            |
| E            | mark is for explanation                                            |     |                            |
| ✓ or ft or F | follow through from previous incorrect result                      | MC  | mis-copy                   |
| CAO          | correct answer only                                                | MR  | mis-read                   |
| CSO          | correct solution only                                              | RA  | required accuracy          |
| AWFW         | anything which falls within                                        | FW  | further work               |
| AWRT         | anything which rounds to                                           | ISW | ignore subsequent work     |
| ACF          | any correct form                                                   | FIW | from incorrect work        |
| AG           | answer given                                                       | BOD | given benefit of doubt     |
| SC           | special case                                                       | WR  | work replaced by candidate |
| OE           | or equivalent                                                      | FB  | formulae book              |
| A2,1         | 2 or 1 (or 0) accuracy marks                                       | NOS | not on scheme              |
| -x EE        | deduct x marks for each error                                      | G   | graph                      |
| NMS          | no method shown                                                    | c   | candidate                  |
| PI           | possibly implied                                                   | sf  | significant figure(s)      |
| SCA          | substantially correct approach                                     | dp  | decimal place(s)           |

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

**Otherwise we require evidence of a correct method for any marks to be awarded.**

**MPC4**

| <b>Q</b>       | <b>Solution</b>                                                                                                                                   | <b>Marks</b>                | <b>Total</b> | <b>Comments</b>                                                                                                                                                                             |
|----------------|---------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------|--------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>1(a)(i)</b> | $\frac{dx}{dt} = 2, \quad \frac{dy}{dt} = -8t$                                                                                                    | B1, B1                      | 2            | CAO                                                                                                                                                                                         |
| <b>(ii)</b>    | $\frac{dy}{dx} = \frac{dy}{dt} \frac{dt}{dx} = \frac{-8t}{2} = -4t$                                                                               | M1<br>A1F                   | 2            | Chain rule in correct form<br>ft on sign coefficient errors ( <b>not</b> power of $t$ )                                                                                                     |
| <b>(b)</b>     | $m_T = -4, \quad m_N = \frac{1}{4}$<br>$x = 3 \quad y = -3$<br>$\frac{y - -3}{x - 3} = \frac{1}{4} \Rightarrow \frac{y + 3}{x - 3} = \frac{1}{4}$ | B1F,<br>B1F<br><br>M1<br>A1 | 4            | ft on $\frac{dy}{dx}$ if $f(t)$<br><br>Use candidate's $(x, y)$ and $m_N$<br>Any correct form; ISW; CAO                                                                                     |
| <b>(c)</b>     | $t = \frac{x-1}{2}$<br>$y = 1 - 4\left(\frac{x-1}{2}\right)^2$                                                                                    | M1<br><br>M1A1              | 3            | Substitute for $t$<br>Simplification not required but CAO<br>Or equivalent methods / forms:<br>$y = 2x - x^2, \quad t^2 = \frac{1-y}{4},$<br>$\left(\frac{x-1}{2}\right)^2 = \frac{1-y}{4}$ |
| <b>Total</b>   |                                                                                                                                                   |                             | <b>11</b>    |                                                                                                                                                                                             |
| <b>2(a)</b>    | $f\left(\frac{3}{2}\right) = 2\left(\frac{3}{2}\right)^3 - 7\left(\frac{3}{2}\right)^2 + 13$<br>$= 4$                                             | M1<br>A1                    | 2            | Substitute $\pm \frac{3}{2}$ in $f(x)$                                                                                                                                                      |
| <b>(b)</b>     | $g\left(\frac{3}{2}\right) = 0 \Rightarrow d + 4 = 0 \Rightarrow d = -4$                                                                          | M1A1                        | 2            | AG (convincingly obtained)<br>SC Written explanation with $g\left(\frac{3}{2}\right) = 0$<br>not seen/clear E2,1,0                                                                          |
| <b>(c)</b>     | $a = -2, \quad b = -3$                                                                                                                            | B1, B1                      | 2            | Inspection expected<br>By division: M1 – complete method<br>A1 CAO<br>Multiply out and compare coefficients:<br>M1 – evidence of use<br>A1 – both $a$ and $b$ correct                       |
| <b>Total</b>   |                                                                                                                                                   |                             | <b>6</b>     |                                                                                                                                                                                             |

**MPC4 (cont)**

| <b>Q</b>       | <b>Solution</b>                                                                                                                                                                                                                                                   | <b>Marks</b>                                         | <b>Total</b> | <b>Comments</b>                                                                                                                                                                                                                                                     |
|----------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------|--------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>3(a)</b>    | $\cos 2x = 1 - 2\sin^2 x$                                                                                                                                                                                                                                         | B1                                                   | 1            |                                                                                                                                                                                                                                                                     |
| <b>(b)(i)</b>  | $3\sin x - \cos 2x = 3\sin x - (1 - 2\sin^2 x)$<br>$= 3\sin x - 1 + 2\sin^2 x$                                                                                                                                                                                    | M1<br>A1                                             | 2            | Candidate's $\cos 2x$ or $\sin^2 x$<br>AG                                                                                                                                                                                                                           |
| <b>(ii)</b>    | $2\sin^2 x + 3\sin x - 2 = 0$<br>$(2\sin x - 1)(\sin x + 2) = 0$<br><br>$\sin x = \frac{1}{2} \quad x = 30 \quad x = 150$<br><br>Allow misread for<br>$2\sin^2 x + 3\sin x - 1 = 0$<br>$\sin x = \frac{-3 \pm \sqrt{17}}{4}$<br><br>$x = 16.3^\circ, 163.7^\circ$ | M1<br>M1<br><br>M1<br>A1<br><br>(M1)<br>(M1)<br>(A1) | 4            | Soluble quadratic form<br>Attempt to solve (allow one error in formula, allow sign errors)<br><br>$\sin^{-1}$ and two solutions ( $0^\circ < x < 360^\circ$ )<br>A0 if radians<br><br>Soluble quadratic form<br><br>Use of formula (allow one error)<br><br>Max 3/4 |
| <b>(c)</b>     | $\int \frac{1}{2}(1 - \cos 2x) = \frac{x}{2} - \frac{\sin 2x}{4} (+c)$                                                                                                                                                                                            | M1A1                                                 | 2            | M1 – solve integral, must have 2 terms for $\sin^2 x$ from (a)                                                                                                                                                                                                      |
|                |                                                                                                                                                                                                                                                                   |                                                      | <b>9</b>     |                                                                                                                                                                                                                                                                     |
| <b>4(a)(i)</b> | $\frac{3x-5}{x-3} = 3 + \frac{4}{x-3}$                                                                                                                                                                                                                            | B1, B1                                               | 2            | By division:<br><br>B1 for 3, B1 for $\frac{4}{x-3}$ or $B = 4$<br><br>By partial fractions: M1 multiply by $x - 3$ and using 2 values of $x$ , A1 both correct                                                                                                     |
| <b>(ii)</b>    | $\int 3 + \frac{4}{x-3} dx = 3x + 4\ln(x-3) (+c)$<br><br><b>Alternative:</b> By substitution $u = x - 3$<br>$\int \frac{3x-5}{x-3} dx = \int \frac{3u+4}{u} du$<br>$= 3(x-3) + 4\ln(x-3)$                                                                         | M1A1F<br><br>(M1)<br>(A1)                            | 2            | M1 $\int 3 + \frac{4}{x-3} dx$ and attempt at integrals<br>fit on A and B; condone omission of brackets around $x - 3$<br><br>Integral in terms of $u$<br><br>Correct, in $x$                                                                                       |
| <b>(b)(i)</b>  | $6x - 5 = P(2x - 5) + Q(2x + 5)$<br>$x = \frac{5}{2} \quad x = -\frac{5}{2}$<br>$10 = 10Q \quad -20 = -10P$<br>$Q = 1 \quad P = 2$                                                                                                                                | M1<br>m1<br><br>A1                                   | 3            | Clear evidence of use of cover-up rule M2                                                                                                                                                                                                                           |
| <b>(ii)</b>    | $\int \frac{2}{2x+5} + \frac{1}{2x-5} dx$<br><br>$\ln(2x+5) + \frac{1}{2}\ln(2x-5) (+c)$                                                                                                                                                                          | M1<br><br>M1<br>A1F                                  | 3            | Attempt at $\ln$ integral<br>$(a \ln(2x+5) + b \ln(2x-5))$<br><br>fit on P and Q; must have brackets                                                                                                                                                                |
|                | <b>Total</b>                                                                                                                                                                                                                                                      |                                                      | <b>10</b>    |                                                                                                                                                                                                                                                                     |

**MPC4 (cont)**

| Q             | Solution                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | Marks          | Total    | Comments                                                                                                                                               |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------|----------|--------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>5(a)</b>   | $(1+x)^{\frac{1}{3}} = 1 + \frac{1}{3}x + \frac{1}{3}\left(-\frac{2}{3}\right)\frac{1}{2}x^2$                                                                                                                                                                                                                                                                                                                                                                                                                           | M1<br>A1       | 2        | $1 + \frac{1}{3}x + kx^2$                                                                                                                              |
| <b>(b)(i)</b> | $\sqrt[3]{8}\left(1 + \frac{3}{8}x\right)^{\frac{1}{3}}$<br>$= 2\left(1 + \frac{1}{3}\left(\frac{3}{8}x\right) - \frac{1}{9}\left(\frac{3}{8}x\right)^2\right)$<br>$= 2 + \frac{1}{4}x - \frac{1}{32}x^2$<br><br><b>Alternative:</b><br>B1 – all powers of 8 correct: $8^{\frac{1}{3}} 8^{-\frac{2}{3}} 8^{-\frac{5}{3}}$<br>M1 – powers of 3x (condone $3x^2$ )<br>$2 + \frac{1}{8^{\frac{2}{3}}}x - \frac{1}{9} \frac{1}{8^{\frac{5}{3}}}9x^2$<br><br>A1 – see some arithmetic processing<br>must see 9s in last term | B1<br>M1<br>A1 | 3        | $8^{\frac{1}{3}}(1+kx)^{\frac{1}{3}}$<br><br>Replacing x with kx in answer to (a)<br><br>For numerical expression which would evaluate to answer given |
| <b>(ii)</b>   | $x = \frac{1}{3}: \sqrt[3]{8+1} = 2 + \frac{1}{4} \times \frac{1}{3} - \frac{1}{32} \times \left(\frac{1}{3}\right)^2$<br>$\sqrt[3]{9} = \frac{576+24-1}{288} = \frac{599}{288}$                                                                                                                                                                                                                                                                                                                                        | M1<br>A1       | 2        | Using $x = \frac{1}{3}$ in given answer<br><br>Any correct numerical expression = $\frac{599}{288}$                                                    |
| <b>Total</b>  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                | <b>7</b> |                                                                                                                                                        |

**MPC4 (cont)**

| Q              | Solution                                                                                                                                                       | Marks | Total | Comments                                                                                                                                                                                                         |
|----------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|-------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>6(a)(i)</b> | $\overrightarrow{BA} = \begin{bmatrix} 3 \\ -2 \\ 4 \end{bmatrix} - \begin{bmatrix} 5 \\ 4 \\ 0 \end{bmatrix} = \begin{bmatrix} -2 \\ -6 \\ 4 \end{bmatrix}$   | M1A1  | 2     | Attempt $\pm \overrightarrow{BA}$ ( $OA - OB$ or $OB - OA$ )                                                                                                                                                     |
| <b>(ii)</b>    | $\overrightarrow{BC} = \begin{bmatrix} 6 \\ 2 \\ -4 \end{bmatrix}$                                                                                             | B1    |       | Allow $\overrightarrow{CB}$ ; or $\begin{bmatrix} -6 \\ -2 \\ 4 \end{bmatrix} = \overrightarrow{BC}$ or $\overrightarrow{CB} = \begin{bmatrix} 6 \\ 2 \\ -4 \end{bmatrix}$<br>May not see explicitly             |
|                | $ \overrightarrow{BA}  = \sqrt{(-2)^2 + (-6)^2 + (4)^2} = \sqrt{56}$                                                                                           | B1F   |       | Calculate modulus of $\overrightarrow{BA}$ or $\overrightarrow{BC}$ ; for finding modulus of one of vectors they have used                                                                                       |
|                | $\overrightarrow{BA} \cdot \overrightarrow{BC} = \begin{bmatrix} -2 \\ -6 \\ 4 \end{bmatrix} \cdot \begin{bmatrix} 6 \\ 2 \\ -4 \end{bmatrix} = -12 - 12 - 16$ | M1    |       | Attempt at $\overrightarrow{BA} \cdot \overrightarrow{BC}$ with numerical answer; or $\overrightarrow{AB} \cdot \overrightarrow{CB}$                                                                             |
|                |                                                                                                                                                                | A1    |       | for $-40$ , or correct if done with multiples of vectors                                                                                                                                                         |
|                | $\cos ABC = \frac{-40}{\sqrt{56}\sqrt{56}} = -\frac{5}{7}$                                                                                                     | A1    | 5     | AG (convincingly obtained)<br><br>Cosine rule: M1 attempt to find 3 sides<br>A1 lengths of sides<br>M1 cosine rule<br>A1F correct<br>A1 rearrange to get<br>$\cos ABC = \frac{-5}{7}$<br>(ft on length of sides) |

**MPC4 (cont)**

| <b>Q</b>                         | <b>Solution</b>                                                                                                                                                                                                                           | <b>Marks</b>   | <b>Total</b> | <b>Comments</b>                                                                                                                                                                                                                                                                                                                                                                                                                    |
|----------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------|--------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>6 (cont)</b><br><b>(b)(i)</b> | $\begin{bmatrix} 8 \\ -3 \\ 2 \end{bmatrix} + \lambda \begin{bmatrix} 1 \\ 3 \\ -2 \end{bmatrix} = \begin{bmatrix} 11 \\ 6 \\ -4 \end{bmatrix} \quad (\lambda = 3)$                                                                       | M1A1           | 2            | $\lambda = 3$ verified in three equations<br>M1 for $\begin{cases} 11 = 8 + \lambda \\ 6 = -3 + 3\lambda \\ -4 = 2 - 2\lambda \end{cases}$<br>A1 for $\lambda = 3$ shown for all three equations<br>$\lambda \begin{bmatrix} 1 \\ 3 \\ -2 \end{bmatrix} = \begin{bmatrix} 11 \\ 6 \\ -4 \end{bmatrix} - \begin{bmatrix} 8 \\ -3 \\ 2 \end{bmatrix} \therefore \lambda = 3$ M1A1<br>SC: $\lambda = 3$ written and nothing else: SC1 |
| <b>(ii)</b>                      | $\begin{bmatrix} 2 \\ 6 \\ -4 \end{bmatrix} = 2 \begin{bmatrix} 1 \\ 3 \\ -2 \end{bmatrix}$ <p><math>\therefore</math> same direction or same gradient or parallel</p>                                                                    | E1             | 1            |                                                                                                                                                                                                                                                                                                                                                                                                                                    |
| <b>(c)</b>                       | $\overrightarrow{OD} = \overrightarrow{OC} + \overrightarrow{BA}$ $= \begin{bmatrix} 11 \\ 6 \\ -4 \end{bmatrix} + \begin{bmatrix} -2 \\ -6 \\ 4 \end{bmatrix} = \begin{bmatrix} 9 \\ 0 \\ 0 \end{bmatrix} \quad D \text{ is } (9, 0, 0)$ | B1<br><br>M1A1 | <br>3        | PI; $\overrightarrow{OD}$ = correct vector expression which may involve $\overrightarrow{AD}$<br><br>M1 for substituting into vector expression for $\overrightarrow{OD}$<br>NMS 3/3                                                                                                                                                                                                                                               |
|                                  | <b>Total</b>                                                                                                                                                                                                                              |                | <b>13</b>    |                                                                                                                                                                                                                                                                                                                                                                                                                                    |
| <b>7(a)</b>                      | $\tan(x+x) = \frac{\tan x + \tan x}{1 - \tan x \tan x} \left( = \frac{2 \tan x}{1 - \tan^2 x} \right)$                                                                                                                                    | M1<br>A1       | 2            | $A = B = x$ used                                                                                                                                                                                                                                                                                                                                                                                                                   |
| <b>(b)</b>                       | $2 - 2 \tan x - \frac{2 \tan x(1 - \tan^2 x)}{2 \tan x}$                                                                                                                                                                                  | M1             |              | Substitute from (a)                                                                                                                                                                                                                                                                                                                                                                                                                |
|                                  | $2 - 2 \tan x - (1 - \tan x)(1 + \tan x)$                                                                                                                                                                                                 | M1             |              | Simplification $2 - 2 \tan x - (1 - \tan^2 x)$                                                                                                                                                                                                                                                                                                                                                                                     |
|                                  | $(1 - \tan x)(2 - (1 + \tan x))$                                                                                                                                                                                                          | M1             |              | $2 - 2 \tan x - 1 + \tan^2 x$                                                                                                                                                                                                                                                                                                                                                                                                      |
|                                  | $(1 - \tan x)^2$                                                                                                                                                                                                                          | A1             | 4            | AG (convincingly obtained)<br>$= (\tan x - 1)^2 = (1 - \tan x)^2$<br>Any equivalent method                                                                                                                                                                                                                                                                                                                                         |
|                                  | <b>Total</b>                                                                                                                                                                                                                              |                | <b>6</b>     |                                                                                                                                                                                                                                                                                                                                                                                                                                    |



**MPC4 (cont)**

| Q              | Solution                                                                                                                                | Marks    | Total | Comments                                                                                                                  |
|----------------|-----------------------------------------------------------------------------------------------------------------------------------------|----------|-------|---------------------------------------------------------------------------------------------------------------------------|
| <b>8(a)(i)</b> | $\int \frac{dy}{y} = \int \sin t \, dt$                                                                                                 | M1       | 4     | Attempt to separate and integrate                                                                                         |
|                | $\ln y = -\cos t + C$                                                                                                                   | A1,A1    |       | A1 for $\ln y$ ; A1 for $-\cos t$ ; condone missing $C$                                                                   |
|                | $y = Ae^{-\cos t}$                                                                                                                      | A1       |       | A present; or $y = e^{-\cos t + C}$                                                                                       |
| <b>(ii)</b>    | $y = 50, t = \pi: 50 = Ae^{-\cos \pi} = Ae$                                                                                             | M1<br>A1 | 3     | Substitute $y = 50, t = \pi$ to find constant<br>Can have $50 = e^{1+C}$ if substituted in above<br>$e^C = \frac{50}{e}$  |
|                | $y = 50e^{-1}e^{-\cos t}$                                                                                                               | A1       |       | AG (convincingly obtained)                                                                                                |
|                | <b>Alternative:</b><br>Must have a constant in answer to (a)(i)<br>$y = Ae^{-\cos t}$ or $y = e^{-\cos t + C}$ or $\ln y = -\cos t + c$ |          |       | <b>Alternative:</b><br>Substitute $y = 50, t = \pi$ into<br>$\ln y = -\cos t + c$ M1<br>$\ln y = -\cos t + \ln 50 - 1$ A1 |
|                | $50 = Ae^{-\cos \pi} \quad 50 = e^{-\cos \pi + c} \quad \ln 50 = -\cos \pi + c$                                                         | (M1)     |       | $\ln \frac{y}{50} = -1 - \cos t$ (AG)                                                                                     |
|                | $50 = Ae \quad 50 = e^{1+c} \quad \ln y = -\cos t + \ln 50 - 1$                                                                         | (A1)     |       |                                                                                                                           |
|                | $y = 50e^{-1-\cos t} \quad y = e^{-\cos t} \frac{50}{e} \quad \ln \left( \frac{y}{50} \right) = -1 - \cos t$                            | (A1)     |       |                                                                                                                           |
| <b>(b)(i)</b>  | $t = 6: y = 50e^{-1}e^{-\cos 6} = 7.0417... \approx 7\text{cm}$                                                                         | M1A1     | 2     | Degrees 6.8 SC1<br>7 or 7.0 for A1                                                                                        |
| <b>(ii)</b>    | $t = \pi \Rightarrow (\sin t = 0 \Rightarrow) \frac{dy}{dt} = 0$                                                                        | B1       |       | Condone $x$ for $t$                                                                                                       |
|                | $\frac{d^2y}{dt^2} = y \cos t + \frac{dy}{dt} \sin t$                                                                                   | M1       |       | For attempt at product rule including $\frac{dy}{dt}$ term; must have $\frac{d^2y}{dt^2} =$                               |
|                | $t = \pi$                                                                                                                               | A1       |       |                                                                                                                           |
|                | $\frac{d^2y}{dt^2} = y \cos \pi + \frac{dy}{dt} \sin \pi$                                                                               | A1       | 4     | Accept $= -y$ , with explanation that $y$ is never negative                                                               |
|                | $= -50 \Rightarrow \max$                                                                                                                |          |       |                                                                                                                           |

**MPC4 (cont)**

| <b>Q</b>                   | <b>Solution</b>                                                                                                                                                                                                                                                                                                                     | <b>Marks</b>                             | <b>Total</b> | <b>Comments</b>                                |
|----------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------|--------------|------------------------------------------------|
| <b>8(b)(ii)<br/>(cont)</b> | <b>Alternative:</b><br>$y = 50e^{-(1+\cos t)} = \frac{50}{e}e^{-\cos t}$<br>$\frac{dy}{dt} = \frac{50}{e}e^{-\cos t} \times \sin t = 0 \text{ at } t = \pi$<br>$\frac{d^2y}{dt^2} = \frac{50}{e}e^{-\cos t} \times \cos t + \frac{50}{e}e^{-\cos t} \times \sin^2 t$<br>Substitute $t = \pi \rightarrow -50 \Rightarrow \text{max}$ | <br><br><br>(B1)<br>(M1)<br>(A1)<br>(A1) |              | <br><br><br>Attempt at product rule<br>Correct |
|                            | <b>Total</b>                                                                                                                                                                                                                                                                                                                        |                                          | <b>13</b>    |                                                |
|                            | <b>TOTAL</b>                                                                                                                                                                                                                                                                                                                        |                                          | <b>75</b>    |                                                |