



**General Certificate of Education**

**Mathematics 6360**

**MS03      Statistics 3**

**Mark Scheme**

*2007 examination - June series*

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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## Key to mark scheme and abbreviations used in marking

M	mark is for method		
m or dM	mark is dependent on one or more M marks and is for method		
A	mark is dependent on M or m marks and is for accuracy		
B	mark is independent of M or m marks and is for method and accuracy		
E	mark is for explanation		
✓ or ft or F	follow through from previous incorrect result	MC	mis-copy
CAO	correct answer only	MR	mis-read
CSO	correct solution only	RA	required accuracy
AWFW	anything which falls within	FW	further work
AWRT	anything which rounds to	ISW	ignore subsequent work
ACF	any correct form	FIW	from incorrect work
AG	answer given	BOD	given benefit of doubt
SC	special case	WR	work replaced by candidate
OE	or equivalent	FB	formulae book
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme
-x EE	deduct x marks for each error	G	graph
NMS	no method shown	c	candidate
PI	possibly implied	sf	significant figure(s)
SCA	substantially correct approach	dp	decimal place(s)

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

**Otherwise we require evidence of a correct method for any marks to be awarded.**

## MS03

Q	Solution	Marks	Total	Comments
<b>1(a)</b>	Samples are independent or random	B1		
	98% $\Rightarrow z = 2.3263$	B1		AWFW 2.32 to 2.33
	CI for $\mu_1 - \mu_2$ is:	M1		Form
	$(\bar{x}_S - \bar{x}_A) \pm z \times \sqrt{\frac{s_S^2}{n_S} + \frac{s_A^2}{n_A}}$	A1		Allow: sigmas, A&B or 1&2 and $n - 1$ Correct
	$(19268 - 17896) \pm 2.3263 \times \sqrt{\frac{7321^2}{175} + \frac{8205^2}{225}}$	A1✓		✓ on $z$ only $s_p = 7830$ to 7850
<b>(b)</b>	ie $1372 \pm (1805 \text{ to } 1820)$ or (-450 to -430, 3170 to 3200)	A1	6	$1372 \pm (1830 \text{ to } 1845)$ AWFW
	Confidence interval includes zero so (at 5% level)	B1✓ ↑dep↑		✓ on CI; OE
	Mean starting salaries may be equal	B1✓	2	✓ on CI; OE
<b>Total</b>			<b>8</b>	

**MS03 (cont)**

<b>Q</b>	<b>Solution</b>	<b>Marks</b>	<b>Total</b>	<b>Comments</b>
<b>2(a)</b>	$P(\geq 18 \mid \text{Road}) = 0.85$	B1	1	CAO; OE; <b>not</b> 85
<b>(b)</b>	$P(18 \text{ to } 64) =$ $P(\text{Route}) \times P(18 \text{ to } 64 \mid \text{Route}) =$ $(0.25 \times 0.80) + (0.60 \times 0.35) + (0.55 \times 0.40)$ $= 0.20 + 0.21 + 0.22 = 0.63$	M1  A1  A1	3	Use of 3 possibilities, each the product of 2 probabilities  At least 1 term correct  CAO; OE
<b>(c)</b>	$P(\text{FR} \cap >64) = P(\text{FR}) \times P(>64 \mid \text{FR})$ $= 0.35 \times 0.15$ $= 0.052 \text{ to } 0.053$	B1  B1	2	Correct expression  AWFW (0.0525)
<b>(d)</b>	$P(\text{FR} \mid >64) = \frac{(c)}{P(>64)} =$ $\frac{0.0525}{(0.25 \times 0.05) + (0.35 \times 0.15) + (0.40 \times 0.35)}$ $= \frac{0.0525}{0.0125 + 0.0525 + 0.1400} = \frac{0.0525}{0.205}$ $= 0.256 \text{ or } \frac{21}{82}$	M1 M1  A1  A1  A1	5	$\frac{\text{answer}(c)}{\sum(3 \times 2) \text{ probabilities}}$  At least 2 terms correct  CAO  AWRT/CAO; OE
<b>Total</b>			<b>11</b>	

**MS03 (cont)**

<b>Q</b>	<b>Solution</b>	<b>Marks</b>	<b>Total</b>	<b>Comments</b>
<b>3(a)</b>	$H_0: p_K = p_S$ $H_1: p_K \neq p_S$	B1		Both; OE; allow A&B or 1&2
	SL $\alpha = 0.05$ CV $ z  = 1.96$	B1		CAO
	$\hat{p} = \frac{(150 \times 0.28) + (250 \times 0.34)}{400}$	M1		Used
	$= \frac{127}{400}$ or 0.317 to 0.318	A1		CAO/AFWW (0.3175)
	$z = \frac{(\hat{p}_K - \hat{p}_S) - 0}{\sqrt{\hat{p}(1-\hat{p})\left(\frac{1}{n_K} + \frac{1}{n_S}\right)}}$	M1		Used; accept unpooled denominator
	$ z  = \frac{ 0.28 - 0.34 }{\sqrt{0.3175 \times 0.6825 \left(\frac{1}{150} + \frac{1}{250}\right)}}$	A1✓		✓ on $\hat{p}$ ; accept no pooling
	$=  1.24 $ to $ 1.25 $	A1		AWFW; $ 1.26 $ to $ 1.27 $
	Thus accept $H_0$ as $ z  < 1.96$	A1✓		✓ on $z$ and CV with same sign
	Thus no evidence, at 5% level, of a difference between two proportions of male customers in two salons	E1✓	9	✓ on $z$ and CV with same sign In context and qualified
<b>(b)</b>	Zero	B1		CAO
	since Cannot make a Type I error when $H_0$ is false	B1	2	OE
	<b>Total</b>		<b>11</b>	

## MS03 (cont)

Q	Solution	Marks	Total	Comments
4	98% $\Rightarrow z = 2.5758$	B1		AWFW 2.57 to 2.58
	CI width is $2 \times \frac{z\sigma}{\sqrt{n}}$	M1		Used; allow $\frac{z\sigma}{\sqrt{n}}$
	Thus $2 \times \frac{2.5758 \times 0.08}{\sqrt{n}} = 0.05$	A1✓		OE; ✓ on $z$ ; allow no '2 ×'
	Thus $\sqrt{n} = 8.24256$	m1		Solving for $\sqrt{n}$ or $n$
	Thus $n = 67.9 \Rightarrow 68$	A1✓		AWRT; ✓ on $z$
	Thus, to nearest 5, $n = 70$	A1	6	CAO
	<b>Total</b>		<b>6</b>	
5	$D = \sum^3 X_i - \sum^2 Y_i$ or $D' = \sum^2 Y_i - \sum^3 X_i$	M1		Used or implied
	have means $\mu = 162 - 166 = -4$ $\mu = 166 - 162 = +4$	B1		CAO either
	and variance $\sigma^2 = (3 \times 2^2) + (2 \times 3^2) = 12 + 18$ $= 30$	M1 A1		Use of $[a \times \text{Var}(Z)]$ ; implied CAO
	$P\left(\sum^3 X_i < \sum^2 Y_i\right) =$ $P(D < 0)$ or $P(D' > 0) =$	M1		Used or implied
	$P\left(Z > \frac{0 - (-4)}{\sqrt{30}}\right)$ or $P\left(Z > \frac{0 - (+4)}{\sqrt{30}}\right) =$	m1		Standardising 0 using $\mu$ and $\sqrt{\sigma^2}$
	$P(Z < +0.73)$ or $P(Z > -0.73) =$  0.767 to 0.768	A1	7	AWFW
	<b>Total</b>		<b>7</b>	

**MS03 (cont)**

Q	Solution	Marks	Total	Comments
<b>6(a)(i)</b>	$E(X) = \sum_{x=0}^n x \times \binom{n}{x} p^x (1-p)^{n-x}$	M1		Use of $\sum x \times P(X=x)$
	$= \sum_{x=1}^n \frac{n!}{(x-1)!(n-x)!} p^x (1-p)^{n-x}$	M1		Expansion of ${}^nC_x$ ; cancelling of $x$ (Ignore limits)
	$= np \times \sum_{x=1}^n \frac{(n-1)!}{(x-1)!(n-x)!} p^{x-1} (1-p)^{n-x}$	M1		Factors of $n$ and $p$ (Ignore limits)
	$= np \times \sum P(X=x)   B(n-1, p) = np$	M1	4	AG; must be convincing
<b>(ii)</b>	$\text{Var}(X) = E(X^2) - (E(X))^2$	M1		Used
	$= [E(X^2) - E(X)] + E(X) - (E(X))^2$			
	$= n(n-1)p^2 + np - n^2p^2$	m1		Attempted
	$= np(1-p)$	A1	3	AG; must be convincing
<b>(iii)</b>	Thus $np(1-p) = 3(1-p) = 2.97$	M1		Substituting $\mu$ in $\sigma^2$
	Thus $1-p = \frac{2.97}{3} = 0.99$			
	Thus $p = 0.01$ and $n = 300$	A1 A1	3	CAO CAO
<b>(iv)</b>	$B(300, 0.01) \sim \text{Po}(3)$	B1		CAO; PI
	$P(X > 2) = 1 - P(X \leq 2)$	M1		Must be applied to Poisson
	$= 1 - 0.4232 = 0.577$	A1	3	AWRT



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**MS03 (cont)**

<b>Q</b>	<b>Solution</b>	<b>Marks</b>	<b>Total</b>	<b>Comments</b>
<b>7(a)</b>	$H_0: \lambda = 13$	B1		CAO; OE
	$H_1: \lambda < 13$	B1		CAO; OE
	$P(R \leq 10 \mid \text{Po}(13))$	M1		Used or implied
	$= 0.2517$	A1		AWFW 0.251 to 0.252
	Prob of $0.2517 > 0.10$ (10%)	M1		Comparison of prob with 0.10
	$z = -0.83$ to $-0.70 > -1.28$			Comparison of $z$ with $-1.28$
	Thus no evidence, at 10% level, of a reduction in the mean value of $R$	A1✓	6	✓ on probability or $z$ In 'context' and qualified
	<b>(b)</b> Require $P(R \leq r \mid \text{Po}(13)) \approx 0.10$	M1		Stated or implied
	Critical Region is $R \leq 8$ or $R < 9$	A1	2	Accept $R = 8$ May be scored in (a)
	<b>(c)</b> Require $P(\text{accept } H_0 \mid H_0 \text{ false})$	B1		OE; PI
	$= P(R > 8 \mid \text{Po}(6.5))$	M1		Use of $\text{Po}(6.5)$
	$= 1 - P(R \leq 8 \mid \text{Po}(6.5))$	m1		
	$= 1 - 0.7916$			
	$= 0.208$ to $0.209$	A1	4	AWFW (0.2084)
	<b>Total</b>		<b>12</b>	
	<b>TOTAL</b>		<b>75</b>	