

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
TOTAL	



General Certificate of Education
Advanced Level Examination
January 2013

Mathematics

MPC3

Unit Pure Core 3

Wednesday 23 January 2013 9.00 am to 10.30 am

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



J A N 1 3 M P C 3 0 1

QUESTION
PART
REFERENCE

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Turn over ►



QUESTION
PART
REFERENCE

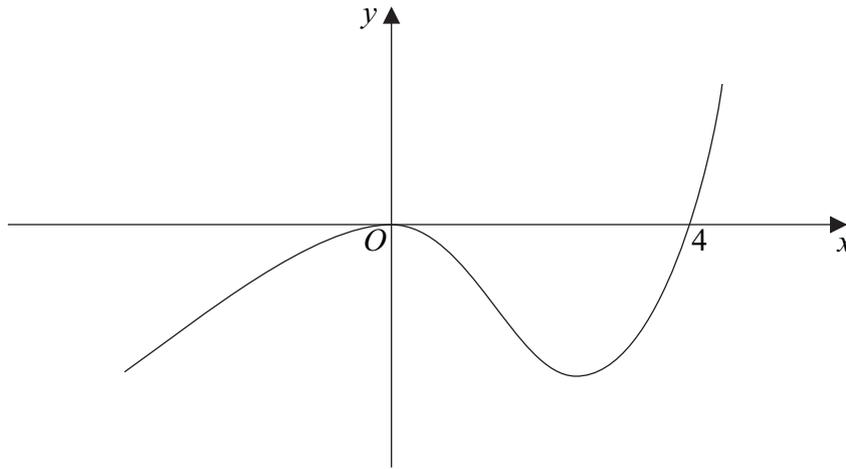
Answer space for question 3

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4 The diagram shows a sketch of the curve with equation $y = f(x)$.

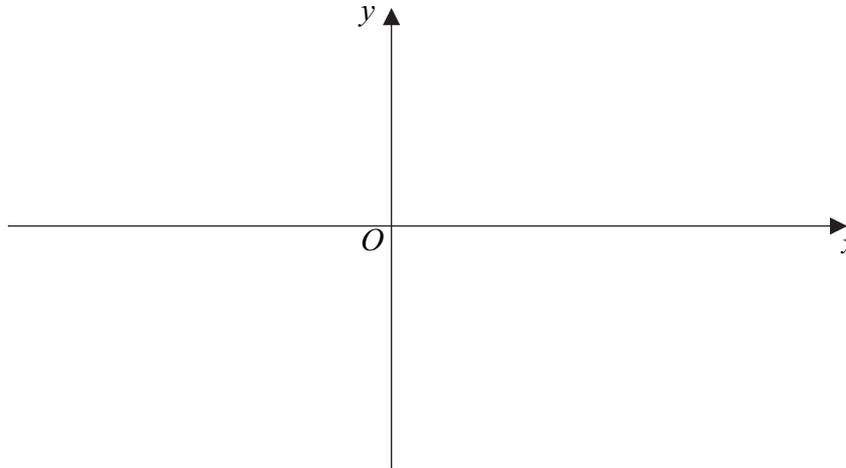


- (a) On the axes below, sketch the curve with equation $y = |f(x)|$. (2 marks)
- (b) Describe a sequence of two geometrical transformations that maps the graph of $y = f(x)$ onto the graph of $y = f(2x - 1)$. (4 marks)

QUESTION
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REFERENCE

Answer space for question 4

(a)



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5 The function f is defined by

$$f(x) = \frac{x^2 - 4}{3}, \text{ for real values of } x, \text{ where } x \leq 0$$

(a) State the range of f . (2 marks)

(b) The inverse of f is f^{-1} .

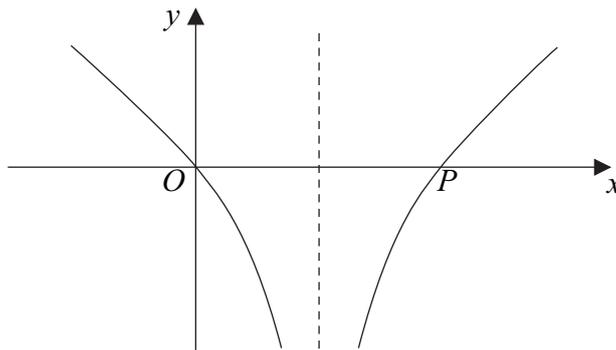
(i) Write down the domain of f^{-1} . (1 mark)

(ii) Find an expression for $f^{-1}(x)$. (3 marks)

(c) The function g is defined by

$$g(x) = \ln|3x - 1|, \text{ for real values of } x, \text{ where } x \neq \frac{1}{3}$$

The curve with equation $y = g(x)$ is sketched below.



(i) The curve $y = g(x)$ intersects the x -axis at the origin and at the point P .

Find the x -coordinate of P . (2 marks)

(ii) State whether the function g has an inverse. Give a reason for your answer. (1 mark)

(iii) Show that $gf(x) = \ln|x^2 - k|$, stating the value of the constant k . (2 marks)

(iv) Solve the equation $gf(x) = 0$. (4 marks)



QUESTION
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QUESTION
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QUESTION
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Answer space for question 6

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QUESTION
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Answer space for question 6

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QUESTION
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Answer space for question 6

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QUESTION
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Answer space for question 7

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QUESTION
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REFERENCE

Answer space for question 7

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8 (a) Show that

$$\int_0^{\ln 2} e^{1-2x} dx = \frac{3}{8}e \quad (4 \text{ marks})$$

(b) Use the substitution $u = \tan x$ to find the exact value of

$$\int_0^{\frac{\pi}{4}} \sec^4 x \sqrt{\tan x} dx \quad (8 \text{ marks})$$

QUESTION
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Answer space for question 8



QUESTION
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Answer space for question 8

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