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| Centre Number       |  |  |  |  |  | Candidate Number |  |  |  |  |
| Surname             |  |  |  |  |  |                  |  |  |  |  |
| Other Names         |  |  |  |  |  |                  |  |  |  |  |
| Candidate Signature |  |  |  |  |  |                  |  |  |  |  |



General Certificate of Education  
Advanced Subsidiary Examination  
January 2011

# Mathematics

**MPC1**

**Unit Pure Core 1**

**Monday 10 January 2011 9.00 am to 10.30 am**

**For this paper you must have:**

- the blue AQA booklet of formulae and statistical tables.
- You must **not** use a calculator.



**Time allowed**

- 1 hour 30 minutes

## Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The use of calculators is **not** permitted.

## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

## Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.

| For Examiner's Use  |      |
|---------------------|------|
| Examiner's Initials |      |
| Question            | Mark |
| 1                   |      |
| 2                   |      |
| 3                   |      |
| 4                   |      |
| 5                   |      |
| 6                   |      |
| 7                   |      |
| TOTAL               |      |



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Answer **all** questions in the spaces provided.

- 1** The curve with equation  $y = 13 + 18x + 3x^2 - 4x^3$  passes through the point  $P$  where  $x = -1$ .
- (a) Find  $\frac{dy}{dx}$ . (3 marks)
- (b) Show that the point  $P$  is a stationary point of the curve and find the other value of  $x$  where the curve has a stationary point. (3 marks)
- (c) (i) Find the value of  $\frac{d^2y}{dx^2}$  at the point  $P$ . (3 marks)
- (ii) Hence, or otherwise, determine whether  $P$  is a maximum point or a minimum point. (1 mark)

QUESTION  
PART  
REFERENCE



QUESTION  
PART  
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Turn over ►



0 3

(1 mark)

**(b)** Express  $\frac{4\sqrt{3} + 3\sqrt{7}}{3\sqrt{3} + \sqrt{7}}$  in the form  $\frac{m + \sqrt{21}}{n}$ , where  $m$  and  $n$  are integers. (4 marks)

[illegible]

QUESTION  
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0 5

- 3** The line  $AB$  has equation  $3x + 2y = 7$ . The point  $C$  has coordinates  $(2, -7)$ .
- (a) (i)** Find the gradient of  $AB$ . (2 marks)
- (ii)** The line which passes through  $C$  and which is parallel to  $AB$  crosses the  $y$ -axis at the point  $D$ . Find the  $y$ -coordinate of  $D$ . (3 marks)
- (b)** The line with equation  $y = 1 - 4x$  intersects the line  $AB$  at the point  $A$ . Find the coordinates of  $A$ . (3 marks)
- (c)** The point  $E$  has coordinates  $(5, k)$ . Given that  $CE$  has length 5, find the two possible values of the constant  $k$ . (3 marks)

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A Cartesian coordinate system with x and y axes. The origin is labeled O. A parabola opens downwards, with its vertex in the second quadrant. A line segment connects point A on the x-axis at x = -2 to point P(1, 12) on the parabola. The region bounded by the parabola, the line segment AP, and the x-axis is shaded gray. The x-axis is labeled with -2 and 1.

(ii) Hence find the area of the shaded region bounded by the curve  $y = 14 - x - x^4$  and the line  $AP$ . (2 marks)

| QUESTION | PART | REFERENCE |
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[illegible]

[illegible]

[illegible]

**5 (a) (i)** Sketch the curve with equation  $y = x(x - 2)^2$ . (3 marks)

**(ii)** Show that the equation  $x(x - 2)^2 = 3$  can be expressed as

$$x^3 - 4x^2 + 4x - 3 = 0 \quad (1 \text{ mark})$$

**(b)** The polynomial  $p(x)$  is given by  $p(x) = x^3 - 4x^2 + 4x - 3$ .

**(i)** Find the remainder when  $p(x)$  is divided by  $x + 1$ . (2 marks)

**(ii)** Use the Factor Theorem to show that  $x - 3$  is a factor of  $p(x)$ . (2 marks)

**(iii)** Express  $p(x)$  in the form  $(x - 3)(x^2 + bx + c)$ , where  $b$  and  $c$  are integers. (2 marks)

**(c)** Hence show that the equation  $x(x - 2)^2 = 3$  has only one real root and state the value of this root. (3 marks)

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[illegible]

(iii) Hence find an equation of the tangent to the circle at the point  $D$ . (2 marks)

[illegible]

[illegible]

[illegible]

[illegible]

**7 (a) (i)** Express  $4 - 10x - x^2$  in the form  $p - (x + q)^2$ . (2 marks)

**(ii)** Hence write down the equation of the line of symmetry of the curve with equation  $y = 4 - 10x - x^2$ . (1 mark)

**(b)** The curve  $C$  has equation  $y = 4 - 10x - x^2$  and the line  $L$  has equation  $y = k(4x - 13)$ , where  $k$  is a constant.

**(i)** Show that the  $x$ -coordinates of any points of intersection of the curve  $C$  with the line  $L$  satisfy the equation

$$x^2 + 2(2k + 5)x - (13k + 4) = 0 \quad (1 \text{ mark})$$

**(ii)** Given that the curve  $C$  and the line  $L$  intersect in two distinct points, show that

$$4k^2 + 33k + 29 > 0 \quad (3 \text{ marks})$$

**(iii)** Solve the inequality  $4k^2 + 33k + 29 > 0$ . (4 marks)

QUESTION  
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[illegible]

[illegible]

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