

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										



General Certificate of Education  
Advanced Subsidiary Examination  
June 2011

# Mathematics

**MFP1**

**Unit Further Pure 1**

**Friday 20 May 2011 1.30 pm to 3.00 pm**

**For this paper you must have:**

- the blue AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

**Time allowed**

- 1 hour 30 minutes

**Instructions**

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

**Information**

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

**Advice**

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
<b>TOTAL</b>	



J U N 1 1 M F P 1 O 1

Answer **all** questions in the spaces provided.

- 1** A curve passes through the point (2, 3) and satisfies the differential equation

$$\frac{dy}{dx} = \frac{1}{\sqrt{2+x}}$$

Starting at the point (2, 3), use a step-by-step method with a step length of 0.5 to estimate the value of  $y$  at  $x = 3$ . Give your answer to four decimal places.

(5 marks)

QUESTION  
PART  
REFERENCE



QUESTION  
PART  
REFERENCE

Turn over ►



**2** The equation

$$4x^2 + 6x + 3 = 0$$

has roots  $\alpha$  and  $\beta$ .

**(a)** Write down the values of  $\alpha + \beta$  and  $\alpha\beta$ . (2 marks)

**(b)** Show that  $\alpha^2 + \beta^2 = \frac{3}{4}$ . (2 marks)

**(c)** Find an equation, with integer coefficients, which has roots  
 $3\alpha - \beta$  and  $3\beta - \alpha$  (5 marks)

QUESTION  
PART  
REFERENCE



QUESTION  
PART  
REFERENCE

Turn over ►



0 5

**3** It is given that  $z = x + iy$ , where  $x$  and  $y$  are real.

**(a)** Find, in terms of  $x$  and  $y$ , the real and imaginary parts of

$$(z - i)(z^* - i) \quad (3 \text{ marks})$$

**(b)** Given that

$$(z - i)(z^* - i) = 24 - 8i$$

find the two possible values of  $z$ . (4 marks)

QUESTION  
PART  
REFERENCE



QUESTION  
PART  
REFERENCE

Turn over ►



- 4** The variables  $x$  and  $Y$ , where  $Y = \log_{10} y$ , are related by the equation

$$Y = mx + c$$

where  $m$  and  $c$  are constants.

- (a)** Given that  $y = ab^x$ , express  $a$  in terms of  $c$ , and  $b$  in terms of  $m$ . (3 marks)

- (b)** It is given that  $y = 12$  when  $x = 1$  and that  $y = 27$  when  $x = 5$ .

On the diagram opposite, draw a linear graph relating  $x$  and  $Y$ . (3 marks)

- (c)** Use your graph to estimate, to two significant figures:

- (i)** the value of  $y$  when  $x = 3$ ; (2 marks)

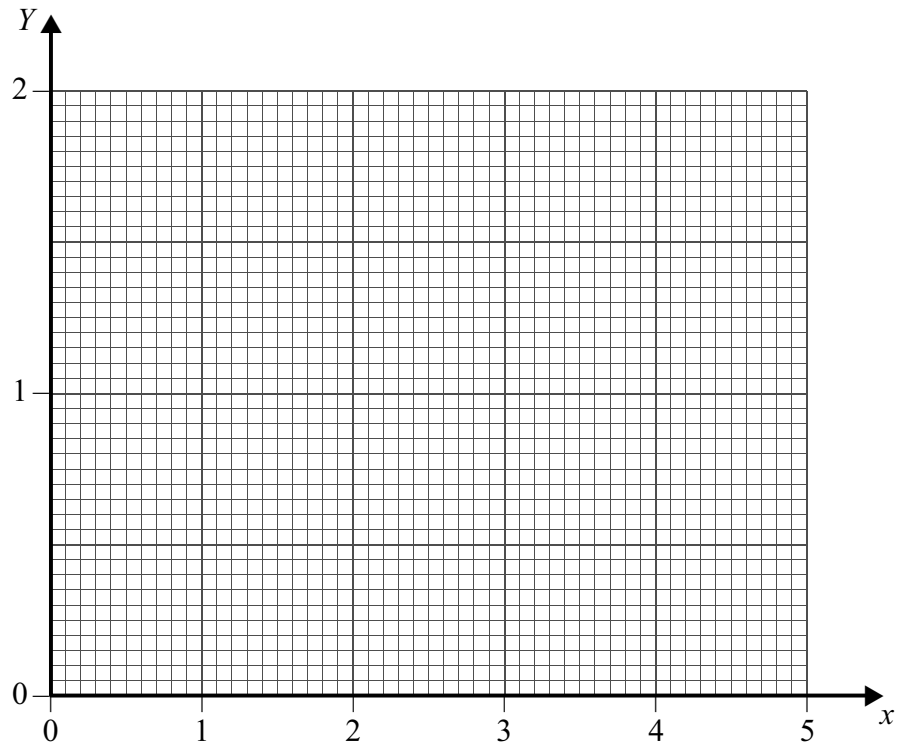
- (ii)** the value of  $a$ . (2 marks)

QUESTION  
PART  
REFERENCE



QUESTION  
PART  
REFERENCE

(b)



Turn over ►



- 5 (a)** Find the general solution of the equation

$$\cos\left(3x - \frac{\pi}{6}\right) = \frac{\sqrt{3}}{2}$$

giving your answer in terms of  $\pi$ .

(5 marks)

- (b)** Use your general solution to find the smallest solution of this equation which is greater than  $5\pi$ .

(2 marks)

QUESTION  
PART  
REFERENCE





(ii) Show how the answer to part (b)(i) can be used to find the gradient of the curve at the point  $(5, 100)$ . State the value of this gradient. (2 marks)

QUESTION	PART	REFERENCE
----------	------	-----------

[illegible]

[illegible]

P39432/Jun11/MFP1



7 The matrix  $\mathbf{A}$  is defined by

$$\mathbf{A} = \begin{bmatrix} -1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{bmatrix}$$

(a) (i) Calculate the matrix  $\mathbf{A}^2$ . (2 marks)

(ii) Show that  $\mathbf{A}^3 = k\mathbf{I}$ , where  $k$  is an integer and  $\mathbf{I}$  is the  $2 \times 2$  identity matrix. (2 marks)

(b) Describe the single geometrical transformation, or combination of two geometrical transformations, corresponding to each of the matrices:

(i)  $\mathbf{A}^3$ ; (2 marks)

(ii)  $\mathbf{A}$ . (3 marks)

QUESTION  
PART  
REFERENCE



[illegible]

P39432/Jun11/MFP1



**8** A curve has equation  $y = \frac{1}{x^2 - 4}$ .

**(a) (i)** Write down the equations of the three asymptotes of the curve. (3 marks)

**(ii)** Sketch the curve, showing the coordinates of any points of intersection with the coordinate axes. (4 marks)

**(b)** Hence, or otherwise, solve the inequality

$$\frac{1}{x^2 - 4} < -2 \quad \text{ (3 marks)}$$

QUESTION  
PART  
REFERENCE



[illegible]

P39432/Jun11/MFP1

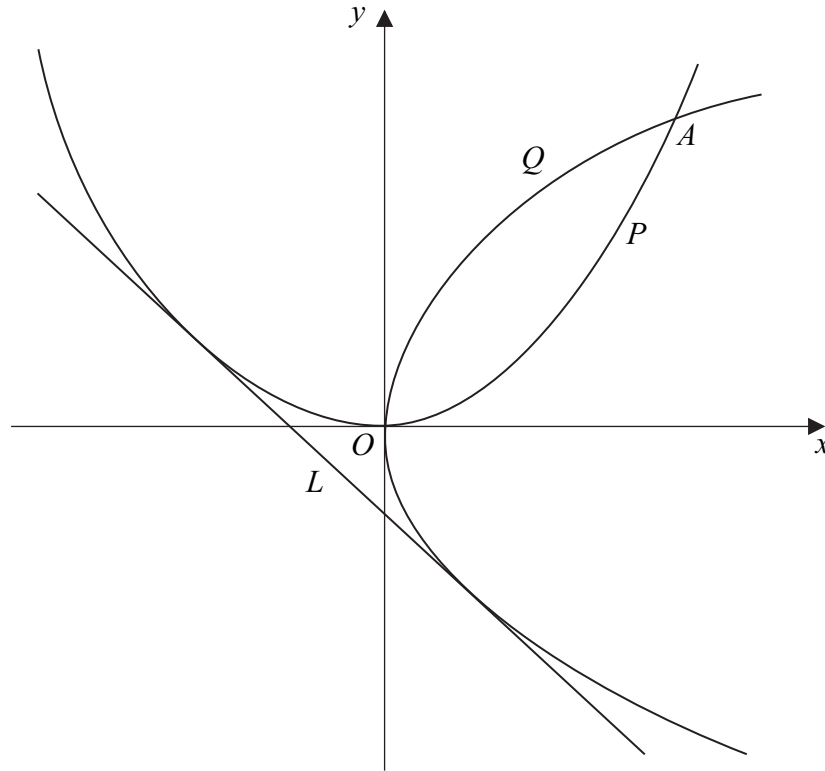


9

The diagram shows a parabola  $P$  which has equation  $y = \frac{1}{8}x^2$ , and another parabola  $Q$  which is the image of  $P$  under a reflection in the line  $y = x$ .

The parabolas  $P$  and  $Q$  intersect at the origin and again at a point  $A$ .

The line  $L$  is a tangent to both  $P$  and  $Q$ .



- (a) (i) Find the coordinates of the point  $A$ . (2 marks)
- (ii) Write down an equation for  $Q$ . (1 mark)
- (iii) Give a reason why the gradient of  $L$  must be  $-1$ . (1 mark)
- (b) (i) Given that the line  $y = -x + c$  intersects the parabola  $P$  at two distinct points, show that
- $$c > -2 \quad (3 \text{ marks})$$
- (ii) Find the coordinates of the points at which the line  $L$  touches the parabolas  $P$  and  $Q$ . (4 marks)
- (No credit will be given for solutions based on differentiation.)



[illegible]

P39432/Jun11/MFP1



This image shows a blank sheet of white paper designed for handwriting practice. It features a solid black vertical line on the left side, creating a narrow margin. The rest of the page is filled with horizontal dashed lines, providing guides for letter height and placement. There are no other markings or text on the page.

Copyright © 2011 AQA and its licensors. All rights reserved.

