

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										



General Certificate of Education
Advanced Subsidiary Examination
June 2010

Mathematics

MFP1

Unit Further Pure 1

Thursday 27 May 2010 9.00 am to 10.30 am

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
TOTAL	



J U N 1 0 M F P 1 0 1

Answer **all** questions in the spaces provided.

1 A curve passes through the point $(1, 3)$ and satisfies the differential equation

$$\frac{dy}{dx} = 1 + x^3$$

Starting at the point $(1, 3)$, use a step-by-step method with a step length of 0.1 to estimate the y -coordinate of the point on the curve for which $x = 1.3$. Give your answer to three decimal places.

(No credit will be given for methods involving integration.) (6 marks)

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[illegible]

QUESTION
PART
REFERENCE

Turn over ►



0 3

(a) Find, in terms of x and y , the real and imaginary parts of

$$(1 - 2i)z - z^* \quad (4 \text{ marks})$$

$$(1 - 2i)z - z^* = 10(2 + i) \quad (2 \text{ marks})$$
[illegible]

QUESTION
PART
REFERENCE

Turn over ►



3

Find the general solution, in degrees, of the equation

$$\cos(5x - 20^\circ) = \cos 40^\circ$$

*(5 marks)*QUESTION
PART
REFERENCE

QUESTION
PART
REFERENCE

Turn over ►



- 4** The variables x and y are related by an equation of the form

$$y = ax^2 + b$$

where a and b are constants.

The following approximate values of x and y have been found.

x	2	4	6	8
y	6.0	10.5	18.0	28.2

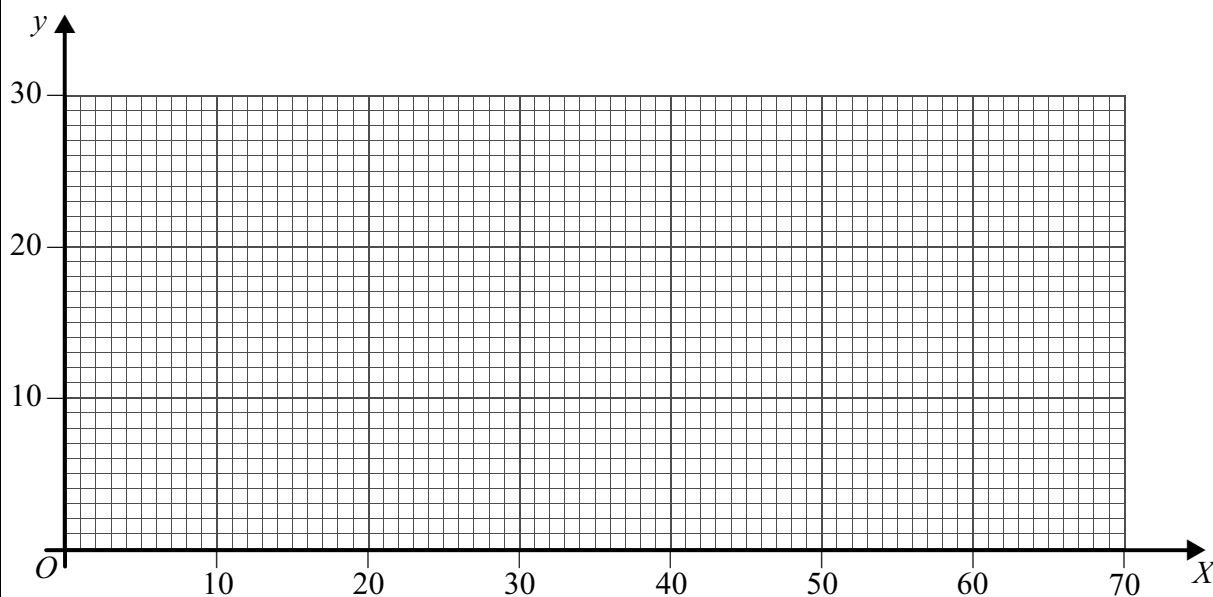
- (a) Complete the table below, showing values of X , where $X = x^2$. (1 mark)
- (b) On the diagram below, draw a linear graph relating X and y . (2 marks)
- (c) Use your graph to find estimates, to two significant figures, for:
- (i) the value of x when $y = 15$; (2 marks)
- (ii) the values of a and b . (3 marks)

QUESTION
PART
REFERENCE

(a)

x	2	4	6	8
X				
y	6.0	10.5	18.0	28.2

(b)



[illegible]

(b) Explain how the result of part **(a)** can be used to show that A is a stationary point on the curve. (2 marks)

QUESTION	PART	REFERENCE
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[illegible]

$$\mathbf{A} = \begin{bmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{bmatrix}, \quad \mathbf{B} = \begin{bmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{bmatrix}$$

(a) \mathbf{A} ; (2 marks)

(b) \mathbf{B} ; (2 marks)

(c) \mathbf{A}^2 ; (2 marks)

(d) \mathbf{B}^2 ; (2 marks)

(e) \mathbf{AB} . (3 marks)

QUESTION	PART	REFERENCE
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[illegible]

7 (a) (i) Write down the equations of the two asymptotes of the curve $y = \frac{1}{x-3}$. (2 marks)

(ii) Sketch the curve $y = \frac{1}{x-3}$, showing the coordinates of any points of intersection with the coordinate axes. (2 marks)

(iii) On the same axes, again showing the coordinates of any points of intersection with the coordinate axes, sketch the line $y = 2x - 5$. (1 mark)

(b) (i) Solve the equation

$$\frac{1}{x-3} = 2x - 5 \quad (3 \text{ marks})$$

(ii) Find the solution of the inequality

$$\frac{1}{x-3} < 2x - 5 \quad (2 \text{ marks})$$

QUESTION
PART
REFERENCE



[illegible]

8 The quadratic equation

$$x^2 - 4x + 10 = 0$$

has roots α and β .

(a) Write down the values of $\alpha + \beta$ and $\alpha\beta$. (2 marks)

(b) Show that $\frac{1}{\alpha} + \frac{1}{\beta} = \frac{2}{5}$. (2 marks)

(c) Find a quadratic equation, with integer coefficients, which has roots $\alpha + \frac{2}{\beta}$ and $\beta + \frac{2}{\alpha}$. (6 marks)

QUESTION
PART
REFERENCE



[illegible]

9 A parabola P has equation $y^2 = x - 2$.

(a) (i) Sketch the parabola P . (2 marks)

(ii) On your sketch, draw the two tangents to P which pass through the point $(-2, 0)$. (2 marks)

(b) (i) Show that, if the line $y = m(x + 2)$ intersects P , then the x -coordinates of the points of intersection must satisfy the equation

$$m^2x^2 + (4m^2 - 1)x + (4m^2 + 2) = 0 \quad (3 \text{ marks})$$

(ii) Show that, if this equation has equal roots, then

$$16m^2 = 1 \quad (3 \text{ marks})$$

(iii) Hence find the coordinates of the points at which the tangents to P from the point $(-2, 0)$ touch the parabola P . (3 marks)

QUESTION
PART
REFERENCE



[illegible]

QUESTION
PART
REFERENCE**END OF QUESTIONS**

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