Version 1.0: 0106

General Certificate of Education

Mathematics 6360

MFP1 Further Pure 1

Mark Scheme

2006 examination - January series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Key To Mark Scheme And Abbreviations Used In Marking

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation

√or ft or F	follow through from previous incorrect result	MC	mis-copy
CAO	correct answer only	MR	mis-read
CSO	correct solution only	RA	required accuracy
AWFW	anything which falls within	FW	further work
AWRT	anything which rounds to	ISW	ignore subsequent work
ACF	any correct form	FIW	from incorrect work
AG	answer given	BOD	given benefit of doubt
SC	special case	WR	work replaced by candidate
OE	or equivalent	FB	formulae book
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme
$-x$ EE	deduct x marks for each error	G	graph
NMS	no method shown	c	candidate
PI	possibly implied	sf	significant figure(s)
SCA	substantially correct approach	dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MFP1

Q	Solution	Marks	Totals	Comments
1(a)	f(0.5) = −0.875, f(1) = 1	B1		
	Change of sign, so root between	E1	2	
(b)	Complete line interpolation method	M2,1		M1 for partially correct method
	Estimated root = $\frac{11}{15} \approx 0.73$	A1	3	Allow $\frac{11}{15}$ as answer
	Total		**5**	
2(a)(i)	$\int x^{-\frac{1}{2}}\,dx = 2x^{\frac{1}{2}}\ (+c)$	M1A1		M1 for $kx^{\frac{1}{2}}$
	$\int_0^9 \frac{1}{\sqrt{x}}\,dx = 6$	A1√	3	ft wrong coeff of $x^{\frac{1}{2}}$
(ii)	$\int x^{-\frac{1}{2}}\,dx = -2x^{-\frac{1}{2}}\ (+c)$	M1A1		M1 for $kx^{-\frac{1}{2}}$
	$x^{-\frac{1}{2}} \to \infty$ as $x \to 0$, so no value	E1	3	'Tending to infinity' clearly implied
(b)	Denominator $\to 0$ as $x \to 0$	E1	1	
	Total		**7**	
3	One solution is $x = 10°$	B1		PI by general formula
	Use of sin 130º = sin 50º	M1		OE
	Second solution is $x = 30°$	A1		OE
	Introduction of 90*n*º, or 360*n*º or 180*n*º	M1		Or $\pi n/2$ or $2\pi n$ or πn
	GS $(10+90n)°, (30+90n)°$	A1√	5	OE; ft one numerical error or omission of 2nd soln
	Total		**5**	
4(a)	Asymptotes $x = 1$, $y = 6$	B1B1	2	
(b)	Curve (correct general shape)	M1		SC Only one branch:
	Curve passing through origin	A1		B1 for origin
	Both branches approaching $x = 1$	A1		B1 for approaching both asymptotes
	Both branches approaching $y = 6$	A1	4	(Max 2/4)
(c)	Correct method	M1		
	Critical values ±1	B1B1		From graph or calculation
	Solution set $-1 < x < 1$	A1√	4	ft one error in CVs; NMS 4/4 after a good graph
	Total		**10**	
5(a)(i)	Full expansion of product	M1		
	Use of $i^2 = -1$	m1		
	$(2+\sqrt{5}i)(\sqrt{5}-i) = 3\sqrt{5}+3i$	A1	3	$\sqrt{5}\sqrt{5} = 5$ must be used − Accept not fully simplified
(ii)	$z^* = x - iy\ (= \sqrt{5} + i)$	M1		
	Hence result	A1	2	Convincingly shown (AG)
(b)(i)	Other root is $\sqrt{5} + i$	B1	1	
(ii)	Sum of roots is $2\sqrt{5}$	B1		
	Product is 6	M1A1	3	
(iii)	$p = -2\sqrt{5}$, $q = 6$	B1 B1√	2	ft wrong answers in (ii)
	Total		**11**	

MFP1

Q	Solution	Marks	Totals	Comments
6(a)	X values 1.23, 2.18			
	Y values 0.70, 1.48	B3,2,1	3	−1 for each error
(b)	$\lg y = \lg k + \lg x^n$	M1		
	$\lg x^n = n \lg x$	M1		
	So $Y = nX + \lg k$	A1	3	
(c)	Four points plotted	B2,1√		B1 if one error here; ft wrong values in (a)
	Good straight line drawn	B1√	3	ft incorrect points (approx collinear)
(d)	Method for gradient	M1		
	Estimate for n	A1√	2	Allow AWRT 0.75 - 0.78; ft grad of candidate's graph
	Total		**11**	
7(a)(i)	Reflection ...	M1		
	... in $y = -x$	A1	2	OE
(ii)	$\mathbf{A}^2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$	M1A1	2	M1A0 for three correct entries
(iii)	$\mathbf{A}^2 = \mathbf{I}$ or geometrical reasoning	E1	1	
(b)(i)	$\mathbf{B}^2 = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$	M1A1		M1A0 for three correct entries
	$\mathbf{B}^2 - \mathbf{A}^2 = \begin{bmatrix} 0 & 2 \\ 0 & 0 \end{bmatrix}$	A1√	3	ft errors, dependent on both M marks
(ii)	$(\mathbf{B} + \mathbf{A})(\mathbf{B} - \mathbf{A}) = \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix}\begin{bmatrix} 1 & 2 \\ 1 & 1 \end{bmatrix}$	B1		
	$... = \begin{bmatrix} 1 & 2 \\ 0 & -1 \end{bmatrix}$	M1 A1√	3	ft one error; M1A0 for three correct (ft) entries
	Total		**11**	
8(a)	Good attempt at sketch	M1		
	Correct at origin	A1	2	
(b)(i)	y replaced by $y - 2$	B1		
	Equation is $(y-2)^2 = 12x$	B1√	2	ft $y + 2$ for $y - 2$
(ii)	Equation is $x^2 = 12y$	B1	1	
(c)(i)	$(x+c)^2 = x^2 + 2cx + c^2$	B1		
	$... = 12x$	M1		
	Hence result	A1	3	convincingly shown (AG)
(ii)	Tangent if $(2c-12)^2 - 4c^2 = 0$	M1		
	ie if $-48c + 144 = 0$ so $c = 3$	A1	2	
(iii)	$x^2 - 6x + 9 = 0$	M1		
	$x = 3, y = 6$	A1	2	
(iv)	$c = 4 \Rightarrow$ discriminant $= -48 < 0$	M1A1		OE
	So line does not intersect curve	A1	3	
	Total		**15**	
	TOTAL		**75**	