



General Certificate of Education (A-level)
June 2011

Mathematics

MD02

(Specification 6360)

Decision 2

Final

Mark Scheme

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all examiners participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for standardisation each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, examiners encounter unusual answers which have not been raised they are required to refer these to the Principal Examiner.

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Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
✓or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
–x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MD02

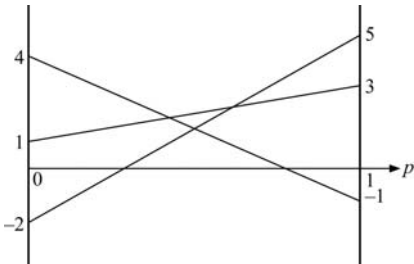
Q	Solution	Marks	Total	Comments
1(a)	<p>Earliest start times</p> <p>Latest finish times</p> <p>(b) Critical paths <i>A D H K L</i> <i>C F I K L</i> Minimum time = 19</p> <p>(c) Greatest float time at G $(13 - 8 - 2) = 3$ (days)</p> <p>(d) <i>A, D, H, K, L</i> and <i>C, F, I</i> <i>B, E, G, J</i> <i>B(1-2); E(3-6); G(11-13); J(13-18)</i></p>	<p>M1 A1</p> <p>M1 A1</p> <p>B1 B1 B1</p> <p>M1 A1 cso</p> <p>M1 A1</p> <p>M1 A1 cso</p>	<p>4</p> <p>3</p> <p>2</p> <p>4</p>	<p>condone one slip + ft all correct</p> <p>condone one slip + ft all correct</p> <p>one path correct second path correct and no others 19 days</p> <p>ft their activity with greatest float for M1 values at G must be correct</p> <p>one of 'their' critical paths "correct" all 8 of these activities correct</p> <p>3 of these with correct duration and latest start time (may omit slack) all 4 correct with correct slack shown</p>
	Total		13	

MD02 (cont)

Q	Solution	Marks	Total	Comments
2(a)	$ \begin{array}{ccccc} 3 & 1 & 0 & 4 & 1 \\ 1 & 4 & 1 & 2 & 4 \\ 1 & 0 & 3 & 1 & 2 \\ 2 & 3 & 2 & 0 & 0 \\ 0 & 5 & 1 & 2 & 1 \end{array} $ <hr/> $ \begin{array}{ccccc} 3 & 1 & 0 & 4 & 1 \\ 0 & k & 0 & 1 & 3 \\ 1 & 0 & 3 & 1 & 2 \\ 2 & 3 & 2 & 0 & 0 \\ 0 & 5 & 1 & 2 & 1 \end{array} $	M1		reducing columns first
		A1cso	2	then rows $k = 3$ stated or value 3 in table AG
(b)(i)	Lines through columns 1, 2, 3 and row 4	B1	1	
(ii)	$ \begin{array}{ccccc} 3 & 1 & 0 & 3 & 0 \\ 0 & 3 & 0 & 0 & 2 \\ 1 & 0 & 3 & 0 & 1 \\ 3 & 4 & 3 & 0 & 0 \\ 0 & 5 & 1 & 1 & 0 \end{array} $	M1		subtract 1 from all uncovered and add 1 to all double covered (condone one slip)
		A1	2	all correct ISW
	This now requires 5 lines to cover zeros			
(c)	$A2 \quad B3 \quad C1 \quad D4 \quad E5$	B1		one of these correct
	$A5 \quad B3 \quad C1 \quad D2 \quad E4$	B1		second way correct
	$A5 \quad B3 \quad C2 \quad D4 \quad E1$	B1	3	third way correct and no others
(d)	Minimum total = 68 (mins)	B1	1	
(e)	Replace each element x by $N - x$	E1	1	any value of N
	Total		10	

Q	Solution	Marks	Total	Comments
3(a)	Row minima are $-4, -3, -7$	M1		both row minima and column maxima attempted (condone 2 errors)
	Column maxima are $-3, 6, 8$	A1		all values correct
	$\max(\text{row min}) = \min(\text{col max}) = -3$	E1		condone arrows pointing to this element but must state $\max(\text{row min})$ and $\min(\text{col max})$ or equivalent
	Play-safe Tom II and Jerry A	B1	4	

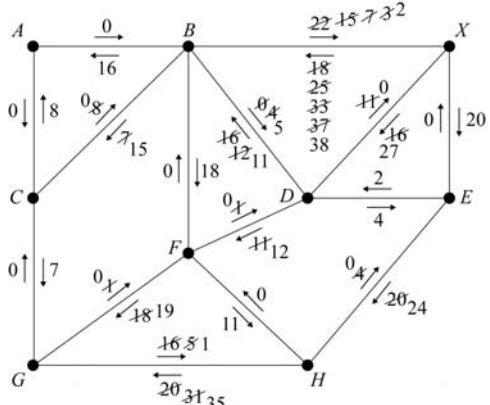
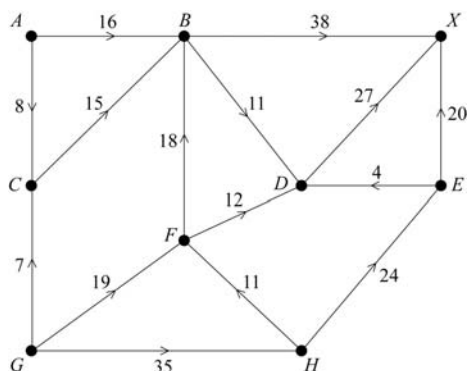
MD02 (cont)

Q	Solution	Marks	Total	Comments
3(b)(i)	<p>Let Rohan play R_1 with prob p \Rightarrow plays R_2 with prob $1 - p$</p> <p>When Carla plays C_1, Rohan's expected gain $= 3p + (1 - p)$ $= 1 + 2p$</p> <p>$C_2 : 5p + (-2)(1 - p) = 7p - 2$</p> <p>$C_3 : -p + 4(1 - p) = 4 - 5p$</p>  <p>$7p - 2 = 4 - 5p$ $12p = 6$ $\Rightarrow p = \frac{1}{2} \Rightarrow$ Rohan plays R_1 50% of the time and R_2 50% of the time</p> <p>Value of game $= 7 \times \frac{1}{2} - 2 = \frac{3}{2}$ AG</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1cso</p> <p>B1</p>	<p>7</p> <p>4</p>	<p>at least 2 expected gains correct unsimplified</p> <p>all 3 correct unsimplified</p> <p>at least 2 lines correct</p> <p>all lines correct for $0 \leq p \leq 1$ and values at 0 and 1 clear</p> <p>choosing highest point or using correct equation</p> <p>or $4 - \frac{5}{2} = \frac{3}{2}$ must see working</p> <p>either expression correct unsimplified</p> <p>correct simultaneous equations unsimplified</p> <p>condone 0.42 or better</p> <p>Must have all 3 correct probabilities</p>
(b)(ii)	<p>When Rohan plays R_1, expected loss for Carla is $3p + 5q + (-1)(1 - p - q)$</p> <p>and when Rohan plays R_2, expected loss for Carla is $p + (-2)q + 4(1 - p - q)$</p> <p>$4p + 6q = \frac{3}{2} + 1$</p> <p>$3p + 6q = 4 - \frac{3}{2}$</p> <p>$\Rightarrow p = 0, q = \frac{5}{12}$</p> <p>$\Rightarrow$ Carla never plays C_1, plays C_2 with prob $\frac{5}{12}$ and plays C_3 with prob $\frac{7}{12}$</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>E1cso</p>	<p>4</p>	
Total			15	

MD02 (cont)

Q	Solution	Marks	Total	Comments
4(a)	$5x + 3y + 10z \leq 15$ $7x + 6y + 4z \leq 28$ $4x + 3y + 6z \leq 12$	M1 A1	2	2 inequalities correct or all 3 LHS & RHS correct but using < all correct
(b)(i)	Choosing 3 from bottom row as pivot $\begin{array}{cccccccc} 1 & 6 & 0 & 12-k & 0 & 0 & 2 & 24 \\ 0 & 1 & 0 & 4 & 1 & 0 & -1 & 3 \\ 0 & -1 & 0 & -8 & 0 & 1 & -2 & 4 \\ 0 & \frac{4}{3} & 1 & 2 & 0 & 0 & \frac{1}{3} & 4 \end{array}$	B1 M1 A1 A1	4	identified or used row operations (even with wrong pivot) one of rows 1, 2, 3 correct all correct (condone multiples of rows)
(ii)	$12 - k < 0$ $\Rightarrow k > 12$	M1 A1	2	their '12 - k' < 0 SC B1 for $k \geq 13$
(c)(i)	$\begin{array}{cccccccc} 1 & 6 & 0 & -8 & 0 & 0 & 2 & 24 \\ 0 & 1 & 0 & 4^* & 1 & 0 & -1 & 3 \\ 0 & -1 & 0 & -8 & 0 & 1 & -2 & 4 \\ 0 & \frac{4}{3} & 1 & 2 & 0 & 0 & \frac{1}{3} & 4 \end{array}$ <hr/> $\begin{array}{cccccccc} 1 & 8 & 0 & 0 & 2 & 0 & 0 & 30 \\ 0 & \frac{1}{4} & 0 & 1 & \frac{1}{4} & 0 & -\frac{1}{4} & \frac{3}{4} \\ 0 & 1 & 0 & 0 & 2 & 1 & -4 & 10 \\ 0 & \frac{5}{6} & 1 & 0 & -\frac{1}{2} & 0 & \frac{5}{6} & \frac{5}{2} \end{array}$	M1 A1 A1 A1	4	correct pivot from z column 4* (identified or used) one of rows 1, 3 or 4 correct another of rows 1, 3 or 4 correct all correct (condone multiples of rows)
(ii)	Maximum value of P now reached $P = 30, x = 0, y = \frac{5}{2}, z = \frac{3}{4}$ $s = 0, t = 10, u = 0$	E1 B1✓ B1cao	3	their tableau must have no negatives in top row fit their values from their tableau provided at least 2 marks earned in (c)(i) condone up to 2 slips in their final tableau
	Total		15	

MD02 (cont)

Q	Solution	Marks	Total	Comments																		
5(a)	Cut value = $40 + 27 + 0 + 24$ = 91	B1	1																			
(b)	$ABDX$ 16 $GFBX$ 18 $GHEX$ 20	B1 B1 B1	3																			
(c)(i)	One correct route with additional flow	M1		any feasible route and flow																		
	Another 2 routes and flows correct	A1		total flow at least 80																		
	All routes correct with total flow = 85	A1cso																				
	Forward and backward flows on diagram (directions must be clear)	M1		at least 8 edges with pairs of values 'correct'																		
	Augmenting flows	A1cso	5	correct																		
	<i>Consider other possible correct flows</i>																					
	<i>Condone diagram as shown but really should have initial flows in DE, etc</i>																					
				 <table data-bbox="1283 860 1506 1173"><thead><tr><th>Route</th><th>Flow</th></tr></thead><tbody><tr><td>$ABDX$</td><td>16</td></tr><tr><td>$GFBX$</td><td>18</td></tr><tr><td>$GHEX$</td><td>20</td></tr><tr><td>$GCBX$</td><td>7</td></tr><tr><td>$ACBX$</td><td>8</td></tr><tr><td>$GHFDX$</td><td>11</td></tr><tr><td>$GHEDBX$</td><td>4</td></tr><tr><td>$GFDBX$</td><td>1</td></tr></tbody></table>	Route	Flow	$ABDX$	16	$GFBX$	18	$GHEX$	20	$GCBX$	7	$ACBX$	8	$GHFDX$	11	$GHEDBX$	4	$GFDBX$	1
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$GHEDBX$	4																					
$GFDBX$	1																					
(ii)	Max flow = 85	B1																				
	Correct max flow	B1	2																			
	<i>Consider other possible correct flows</i>																					
																						
(d)	Considering 'their' $AB + CB + FB - 45$ = 4 fewer \Rightarrow max number = 81	M1 A1cao	2																			
	Total		13																			

MD02 (cont)

Q	Solution	Marks	Total	Comments																																																																																																																																																																															
6	<p>Wednesday profits</p> <p>Tuesday: use of maxima from Wednesday</p> <p>Monday values correct</p> <p>(Monday builds shed) <i>D</i></p> <p>\Rightarrow order <i>D B A C</i></p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1✓</p> <p>A1✓</p> <p>M1</p> <p>A1cso</p>	9	<p>4 more calculations/ profits correct</p> <p>6 more profits correct</p> <p>all profits correct</p> <p>6 more calculations/profits correct</p> <p>8 profits correct</p> <p>all profits correct</p> <p>ft one slip from Wednesday figures</p> <p>all profits correct</p> <p>ft one slip from Tuesday figures</p> <p>Choosing largest Monday profit from their table</p> <p>SC B1 only for order <i>D B A C</i></p> <p>NMS or without “correct” table</p>																																																																																																																																																																															
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Monday	-	<i>A</i>	50 + 247	297																																																																																																																																																																															
		<i>B</i>	65 + 239	304																																																																																																																																																																															
		<i>C</i>	70 + 228	298																																																																																																																																																																															
		<i>D</i>	80 + 226	306 →																																																																																																																																																																															
	Monday	Tuesday	Wednesday	Thursday																																																																																																																																																																															
Shed to build	<i>D</i>	<i>B</i>	<i>A</i>	<i>C</i>																																																																																																																																																																															
	Total		9																																																																																																																																																																																
	TOTAL		75																																																																																																																																																																																