

General Certificate of Secondary Education November 2012

Mathematics
Unit 1 Higher tier

FINAL

Mark Scheme

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all examiners participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for standardisation each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, examiners encounter unusual answers which have not been raised they are required to refer these to the Principal Examiner.
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## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A

B Marks awarded independent of method.

Q
ft

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.

M dep A method mark dependent on a previous method mark being awarded.

B dep A mark that can only be awarded if a previous independent mark has been awarded.
oe Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$
$[a, b] \quad$ Accept values between $a$ and $b$ inclusive.
3.14... Allow answers which begin $3.14 \mathrm{eg} 3.14,3.142,3.149$.

Use of brackets It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

## Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

## Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

## Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

## Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

## Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

## Work not replaced

Erased or crossed out work that is still legible should be marked.

## Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

## Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

## Unit 1 Higher Tier

| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 1a | Lists at least 4 correct combinations <br> from <br> (SC), SB, SP <br> CJ, CF, BJ, BF, PJ, PF | M 1 | $1 \times 3+3 \times 2$ or $3+6$ oe |
| :---: | :--- | :---: | :--- |
|  | 9 or 8 (more) | A1 |  |
| 1b | $\frac{3}{9}$ | B1 ft | oe <br> ft their 3 and their 9 if probability $>0$ <br> and $<1$ |
| 1c | $270 \times$ their $\frac{3}{9}$ | A1 ft | oe <br> ft their part (b) but must be $>0$ and $<1$ <br> Must give integer answer |
|  | 90 |  |  |


| 2 | $\frac{1}{4} \times 100(=25$ (green)) | M1 | oe |
| :---: | :---: | :---: | :---: |
|  | their $25 \times 2$ (= 50 (blue)) | M1 | oe |
|  | their $50 \div 5$ (= 10 (red) ) | M1 | oe |
|  | 15 | A1 |  |
|  | Alternative method |  |  |
|  | blue $=\frac{1}{2}$ | M1 | oe |
|  | $\operatorname{red}=\frac{1}{10}$ | M1 | oe |
|  | $1-\left(\frac{1}{4}+\frac{1}{2}+\frac{1}{10}\right)\left(=\frac{3}{20}\right)$ | M1 | oe |
|  | 15 | A1 |  |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 3 3a | Suitable key |  | B1 |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- |
|  | 2 | 4 | 8 |  | B2 |
| 1 | 2 | 5 | 6 | 9 | 9 |
| 0 | 2 | 4 | 6 |  | B1 complete but unordered leaves <br> or <br> B1 one correct row (only award for first row <br> if single digit values used throughout) |
| $3 b$ | $26-25$ or $2+25$ | M1 | oe |  |  |
|  | 1,27 | A1 | either answer implies M1 <br> SC1 Range (for 13 days) $=24$ seen <br> or $26-2=24$ seen |  |  |


| 4a | $200<t \leq 240$ | B1 |  |
| :---: | :---: | :---: | :---: |
| 4b | $16 \times 220(=3520) \text { or } 4 \times 260(=1040)$ $\text { or } 4 \times 300(=1200) \text { or } 2 \times 380(=760)$ <br> or $2 \times 460(=920)$ or $2 \times 500(=1000)$ or $8440$ | M1 | Attempt at $f x$ using one correct midpoint |
|  | (their 3520 + their $1040+$ their $1200+$ their $0+$ their $760+$ their $0+$ their 920 + their 1000) $\div 30$ | M1 dep | 1055 implies M1M0A0 <br> 7473.(...) implies M1M1A0 |
|  | 281 or 282 or 281.3(...) | A1 | SC2 301.(3..) or 261.(3..) |
| 4c | Ticks modal class and gives valid reason <br> eg Current performance in this class or <br> This class has shorter times | B1 | oe the mean is affected by a few (older) slower times <br> or <br> older/slower times irrelevant to current performance |


| 5 Fa | $1430-1250(=180)$ | M1 | $\frac{1430}{1250}(\times 100)$ |
| :---: | :--- | :---: | :--- |
|  | $\frac{\text { their } 180}{1250} \times 100$ or 0.144 | M1 dep | oe <br> 1.144 or 114.4 |
| 5 | 14.4 | A1 | B2 |
| At least 3 non-overlapping, <br> exhaustive boxes with units | B1 at least 3 non-overlapping, exhaustive <br> boxes without units <br> B1 at least 3 with gaps but no overlaps or <br> B1 at least 3 with overlaps but no gaps or <br> B1 2 exhaustive and non-overlapping |  |  |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 6 a | $\frac{28}{40}$ or $70 \%$ or 0.7 | B1 | oe |
| :---: | :--- | :--- | :--- |
| 6 b | their $\frac{28}{40} \times 10(=7)$ or |  | ft their $\frac{28}{40}$ from part $(\mathrm{a}) \times 10$ for red |
| $\frac{9}{40} \times 10(=2.25$ or 2$)$ or | M1 | oe $28 \div 4$ or $9 \div 4$ or $3 \div 4$ |  |
| $\frac{3}{40} \times 10(=0.75$ or 1$)$ |  |  |  |
|  | 7 and 2 and 1 | M1 | Must give integer answers |


| 7a | Cumulative frequencies correct in table <br> 2, 10, 44, 54, 60 | M1 | Allow one addition error in cumulative frequencies but must be increasing <br> May be implied by graph ( $\pm \frac{1}{2}$ sq) |
| :---: | :---: | :---: | :---: |
|  | Smooth curve or polygon through all points at correct heights | A1 | Must be an increasing function but not a single straight line Ignore below their 95 |
|  | 5 points at increasing heights, plotted at upper class bounds ( $\pm \frac{1}{2} \mathrm{sq}$ ) 95, 100, 105, 110, 115 | Q1 | Strand (ii) - logical organised working <br> Allow one missing upper class bound |
| 7b | The correct integer value for 109 from their graph <br> eg 52 <br> or correct interpolation from table <br> ie $(44+0.8 \times 10=) 52$ | B1 ft | ft an increasing function but not a single straight line |
|  | Number of boys $=45$ | B1 | Accept 45.75 from $\frac{3}{4}(60+1)$ |
|  | their $52+$ their 45 | M1 | The correct value $\pm 2$ for 109 from their increasing graph (not a straight line) or from correct interpolation method Their 45 in range $[45,50]$ |
|  | 97 | A1 ft | ft their 52 + their 45 |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 8 | All correct ie each head $=\frac{2}{5}$ and each tail $=\frac{3}{5}$ | B3 | oe <br> B2 all pairs of probabilities add to 1 and at least one pair correct <br> B1 two correct probabilities in correct positions |
| 9 | $10 p$ and $9 p, \quad p$ an integer $>1$ and <br> $5 q$ and $4 q, \quad q$ an integer $>1$ | M1 | eg 20, 18 and 10, 8 |
|  | $10 p$ and $9 p$ and $5 q$ and $4 q$, $p, q$ integers $>1$ and $9 p=5 q$ <br> or $25 r: 18 r$ | M1 | eg 100, 90 and 90, 72 |
|  | 25:18 | A1 |  |
| 10 | $\left(\frac{1}{2}\right)^{5} \div\left(7.15 \times 10^{-8}\right)$ <br> or <br> $\frac{1}{32}$ oe seen | M1 | oe Condone bracket error in $\left(7.15 \times 10^{-8}\right)$ Condone use of $\frac{2}{5}$ for $\frac{1}{2}$ or $\frac{32}{3125}$ oe seen (following Q8) |
|  | = 437062.(...) | A1 | May be implied |
|  | $4.4 \times 10^{5}$ | Q1ft | Strand (i) Correct notation required <br> ft any decimal (at least 3 sf ) rounded to 2 sf and written in correct standard form <br> $4.37 \ldots \times 10^{5}$ scores M1A1Q0 <br> 440000 scores M1A1Q0 |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 11a | median $=1000 \div 2=500$ | M1 | Accept 500.5 |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 20 \times 9(=180) \text { or } \\ & 10 \times 40(=400) \text { or } \\ & 10 \times 34(=340) \text { and } 20 \times 4(=80) \end{aligned}$ | M1 |  |
|  | $\begin{aligned} & \frac{500-\text { their } 180}{\text { their } 400} \times 10(=8) \\ & \text { or } \\ & \frac{\text { their } 400+\text { their } 180-500}{\text { their } 400} \times 10(=2) \end{aligned}$ | M1dep | oe $\frac{320}{400} \times 10(=8)$ or $\frac{4}{5} \times 10(=8)$ <br> or <br> $\frac{80}{400} \times 10(=2) \quad$ or $\quad \frac{1}{5} \times 10(=2)$ <br> Either their 180 or their 400 must be correct |
|  | 38 | A1 | Accept 38.0125 (from 500.5) |
|  | Alternative method |  |  |
|  | half of area $=20$ large squares | M1 |  |
|  | (first area $=$ ) 7.2 or (second area =) 16 or (third area =) 13.6 and (fourth area =) 3.2 | M1 |  |
|  | $\begin{aligned} & \frac{20-\text { their } 7.2}{\text { their } 16} \times 10(=8) \\ & \text { or } \\ & \frac{\text { their } 16+\text { their } 7.2-20}{\text { their } 16} \times 10(=2) \end{aligned}$ | M1dep | oe $\frac{12.8}{16} \times 10(=8)$ or $\frac{4}{5} \times 10(=8)$ <br> or $\frac{3.2}{16} \times 10(=2) \quad \text { or } \quad \frac{1}{5} \times 10(=2)$ <br> Either their 7.2 or their 16 must be correct |
|  | 38 | A1 |  |


| 11b | $\begin{aligned} & 1000 \div 100=10 \text { or } \\ & 100 \div 1000\left(=\frac{1}{10}\right) \text { or } \\ & 10 \times 40 \div 40=10 \text { or } \\ & 40 \div(10 \times 40)\left(=\frac{1}{10}\right) \end{aligned}$ | M1 | oe <br> 34 seen in correct position in table |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 20 \times 9 \div 10(=18) \text { or } \\ & 20 \times 4 \div 10(=8) \end{aligned}$ | M1 | oe |
|  | 18, 34 and 8 | A1 |  |


| 12 | 1.05 seen | B1 | oe |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $9000 \div 1.05^{3}$ | M2 | $9000 \div 1.05$ (=8571.(...)) | M1 |
|  |  |  | $\begin{aligned} & \text { their } 8571 .(\ldots) \div 1.05(=8163 .(\ldots)) \\ & \text { their } 8163 .(\ldots) \div 1.05 \quad(=7774 .(\ldots)) \end{aligned}$ | M1 |
|  | 7774.54 or 7774.55 or 7775 | A1 |  |  |
|  | Alternative method |  |  |  |
|  | 1.05 seen | B1 | oe |  |
|  | Two trials correctly evaluated of the form $n \times 1.05^{3}$ with second trial closer to $£ 9000$ | M1 |  |  |
|  | Two trials correctly evaluated of the form $n \times 1.05^{3}$ with second trial closer to $£ 9000$ <br> and <br> both values of $n$ in range [7700, 7800] | M1 |  |  |
|  | 7774.54 or 7774.55 or 7775 | A1 |  |  |

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