# General Certificate of Secondary Education 

## Statistics 3311

Higher Tier

## Mark Scheme

2009 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Statistics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
E Explain marks are awarded for a full and detailed explanation.
Mdep A method mark dependent on a previous method mark being awarded.
B dep A mark that can only be awarded if a previous independent mark has been awarded.
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$

## Higher Tier

| Q Answer | Mark | Comments |  |
| :---: | :---: | :---: | :--- |
| 1(a) | All 28 correct | B3 | B2 26 or 27 correct <br> B1 20 - 25 correct |


| $\mathbf{1 ( b )}$ | Letter T in the centre of $2^{\text {nd }}$ row | B1 | ' 39 ' rectangle |
| :---: | :--- | :--- | :--- |


| 2(a) | (All) voters / adults.... | B1 | oe (over) 18s |
| :---: | :--- | :--- | :--- |
|  | ....in the town / constituency / ward / <br> polling district / polling area | B1 | oe |
| B2 all people who (could) use the polling |  |  |  |
| station (oe) |  |  |  |
| B1 everyone in town (oe) |  |  |  |


| 2(b) | Better response rate | E1 | oe (for interview chosen) |
| :---: | :--- | :---: | :--- |
|  | Can explain questions | E1 |  |
| Alt 2(b) | Can be done when convenient | E1 | oe (for postal chosen) |
|  | Everyone gets exactly same questions | E1 |  |


| 2(c)(i) | Might not know the answer | E1 | oe |
| :--- | :--- | :--- | :--- |


| $\mathbf{2 ( c ) ( i i ) ~}$ | Needs option boxes | E1 | oe |
| :--- | :--- | :--- | :--- |


| 3(a) | Multiple or dual or comparative <br> bar <br> chart or diagram or graph | B1 | Also accept multiple / dual / comparative <br> frequency diagram |
| :---: | :---: | :---: | :--- |


| 3(b) | 5 | B1 |  |
| :--- | :--- | :--- | :--- |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 3(c) | Not possible to tell, the \% higher <br> (slightly) but we do not know <br> whether the population of 5 year olds <br> is larger/ necessary data not available | E2 | E1 Not possible to tell, reason attempted |
| :---: | :--- | :--- | :--- |
| Alt <br> 3(c) | True, population sizes will be similar <br> (so \% increase means actual increase) | E2 | E1 True, reason attempted . Allow 'Yes' for <br> true |


| $\mathbf{4 ( a ) ( \mathbf { i } )}$ | 0.3 | B1 | oe |
| :--- | :--- | :--- | :--- |


| 4(a)(ii) | $0.3 \times 0.3$ | M1 | ft their 0.3 as long as it is a valid probability |
| :--- | :--- | :---: | :--- |
|  | 0.09 | A1ft | oe |


| 4(a)(iii) | Independence | E1 | Accept description of independence |
| :--- | :--- | :--- | :--- |


| 4(b) | Adults $00-31$ | B1 | or any 32 values |
| :---: | :--- | :---: | :--- |
|  | Teenagers $32-61$ and <br> Children $62-99$ | B1 | or any distinct 30 and distinct 38 values <br> respectively |
|  |  | SC1 any one allocation set within 1 of being <br> correct |  |


| 4(c) | C A T T A C T A C T | B2ft | B1 ft 8 or 9 correct <br> ONLY ft if B1 or better awarded in part (b) <br> and where it is possible to check a unique <br> allocation (i.e no overlap) |
| :--- | :--- | :--- | :--- |


| 4(d) | 27 in male children cell | B1 |  |
| :--- | :--- | :---: | :--- |
|  | 30 in female children cell | B1 |  |
|  | 4 in male teenager cell and 4 in <br> female teenager cell | B1 |  |
|  | 15 in male adult cell and <br> female under $13+$ female adult $=50$ | B1 ft |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 5(a) | 5 correct plots and joined | B2 | B1 4 correct plots and joined or <br> 5 correct plots not joined <br> tolerance one small square |
| :---: | :--- | :---: | :---: |
| $\mathbf{5 ( b )}$ | Café closes early/some workers <br> day off | E1 | oe eg unpopular set lunch |


| 5(c) | Takings are highest each Friday | E1 | oe |
| :---: | :--- | :--- | :--- |
|  | Takings are reducing week by week | E1 | one comment about the pattern within a week, <br> one comment about the trend across weeks |


| 6(a) | England | B1 |  |
| :---: | :--- | :---: | :--- |
| $\mathbf{6 ( b ) ( \mathbf { i } )}$ | $65+18.4$ | M1 | Allow, for M1, 65 + any value from column 4 <br> or $65+15.5$ if working shown |
|  | 83.4 | A1 | Accept 83 |


| $\mathbf{6 ( b ) ( i i )}$ | Getting to 65 excludes those who die <br> before then (so average age to which <br> they live is higher) | E1 | oe |
| :--- | :--- | :--- | :--- |


| 6(c) | England has a much higher <br> population (so its higher average has <br> more effect than the values for other <br> countries) | E1 | oe references to different population (sizes) in <br> different countries |
| :---: | :--- | :--- | :--- |


| $\mathbf{7 ( a )}$ | Non response | E1 | Not rounding |
| :--- | :--- | :--- | :--- |


| 7(b) | Linear scale showing attitude <br> extremes | B1 |  |
| :--- | :--- | :---: | :--- |
|  | Respondent marks position on scale | B1 |  |


| 7 7(c) | Retain exams | E1 |  |
| :--- | :--- | :---: | :--- |
|  | Leaving age not changed | E1 |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :--- | :--- | :--- |


| 8(a) | Rankings: 946631028157 | B1 | If treat final two in each set as tied B1 |
| :---: | :---: | :---: | :---: |
|  | 76148395210 | B1 |  |
|  | Differences | M1 |  |
|  | Sum of differences squared $=74$ | M1 |  |
|  | Formula and sub give sp.rank $=0.551(5)$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ |  |


| 8(b) | Some / moderate agreement | B1 | Not allow strong or simply positive |
| :---: | :--- | :---: | :--- |
| 8(c) | Opposite rankings: <br> High matched with low | E1 |  |
|  | No agreement: <br> Rankings do not match | E1 | Accept calculation error |


| 9(a) | Vitamin supplement | B1 |  |
| :--- | :--- | :---: | :--- |
|  | Exam performance | B1 |  |


| 9(b) | Academic ability | B1 |  |
| :--- | :--- | :---: | :--- |
|  | Matched ability groups | B1 |  |


| 9(c) | Children taking a vitamin supplement <br> will improve their exam performance <br> in Statistics | B1 |  |
| :--- | :--- | :--- | :--- |


| 9(d)(i) | Weight | B1 | fitness |
| :--- | :--- | :---: | :--- |
|  | Time spent studying | B1 | reaction to tests/exams |


| 9(d)(ii) | Random allocation mentioned | B1 |  |
| :--- | :--- | :---: | :--- |
|  | Identify each member of the pair and <br> toss a coin | B1 |  |


| $\mathbf{1 0 ( a )}$ | $(5.2 \times 3)+(2.1 \times 5)+(7.4 \times 12)=$ <br> $£ 114.90$ | $\mathrm{M} 1, \mathrm{~A} 1$ |
| :---: | :--- | :--- |


| Q Answer | Mark | Comments |  |
| :---: | :---: | :---: | :---: |
| $\mathbf{1 0 ( b )}$ | Their $(114.9 / 90) \times 100=127.7$ | M1 | (ft on their 114.9) |


| $\mathbf{1 0}(\mathbf{c})$ | Selling price increases at a faster rate | E1 ft |  |
| :--- | :--- | :--- | :--- |


| $\mathbf{1 1 ( a )}$ | $300 / 50=6$ | B1 |  |
| :---: | :--- | :---: | :--- |
|  | $\sqrt{\frac{1962}{50}-36}$ | M1 | Formula and substitution |
|  | $\sqrt{3.24}$ | A1ft | 3.24 A O on its own |
| 1.8 days | A1 |  |  |

\(\left.\begin{array}{|c|l|c|l|}\hline \mathbf{1 1}(\mathrm{b}) \& 6+/-2(1.8)=2.4 to 9.6 days \& M1 \& 1 for idea of a limit: 6(mean) \pm a quantity <br>
M1 dep <br>

A1 ft\end{array}\right]\)| for $\pm 2$ |
| :--- |
| for $2 \times$ 'their' 1.8 |


| $\mathbf{1 1}(\mathbf{c})$ | Point estimate equal to (their 6) | B1 ft |  |
| :---: | :--- | :--- | :--- |


| $\mathbf{1 1 ( d )}$ | Variability reduced by $1 / 2$ | E2 | Variability reduced E1 <br> or variability reduced by factor of 4 E1 <br> or sample size increased by factor of 4 E1 |
| :---: | :--- | :---: | :--- |


| 12(a) | $(24.2-3.9) / 14=1.45$ | M1, A1 |  |
| :---: | :--- | :---: | :--- |
|  | $24.2=(1.45)(20)+\mathrm{c}$ <br> $\mathrm{c}=-4.8$ <br> $\mathrm{y}=1.45 x-4.8$ | M 1 |  |


| $\mathbf{1 2 ( b )}$ | $(1.45 \times 68-4.8)$ <br> 93.8 | M1 |  |
| :---: | :--- | :---: | :--- |
| A1 | Accept 94 with/without working |  |  |


| $\mathbf{1 2 ( c ) ( i )}$ | Negative mark | E1 | Must be explained |
| :--- | :--- | :--- | :--- |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\mathbf{1 2 ( c ) ( i i ) ~}$ | Mark exceeding 100 | E1 |  |
| :--- | :--- | :--- | :--- |


| $\mathbf{1 3 ( a )}$ | Divisions at $0.5,2.5 \ldots$ etc | B1 <br> B1 | B1 for sight of continuity corrrection: <br> B1 For 'time' limits fully correct |
| :---: | :--- | :---: | :--- |
|  | fq. Density $1,1.25,2,3.3,6.5,4,1$ | M1, A2 | -1 for each error |
|  | Fully correct graph | B1 | Heights, scale, labels |


| 13(b) | Negative | B1 |  |
| :---: | :--- | :---: | :--- |
|  | Long left hand tail | E1 | or correct reference to relative position of <br> mode, median etc. |


| 13(c) | $9^{\text {th }}$ decile corresponds to $45^{\text {th }}$ term: | B1 | ref. $5^{\text {th }}$. from top : allow final $10 \%:$ <br> $90 \%$ if used needs to be fully explained |
| :---: | :--- | :---: | :--- |
|  | Must be in class $16.5-22.5$ | B1dep | or $15-16$ only goes to $44^{\text {th }}$ |


| $\mathbf{1 3}(\mathbf{d})$ | $(8 / 50) \times 100=16 \%$ | M1, A1 | SC1 For $(6 / 50) \times 100=12 \%$ <br> or SC1 for $\frac{6+\text { incorrect fraction of } 8}{50} \times 100=\ldots$ |
| :---: | :--- | :--- | :--- |


| 14(a) | Readings at 60,90 etc | B1 |  |
| :--- | :--- | :---: | :--- |
|  | Position of median on plot box | B1 |  |
|  | Quartiles | B1 |  |
|  | Box and whiskers | B1 |  |


| $\mathbf{1 4 ( b )}$ | $\mathrm{IQR}=25.2-24.6=0.6$ | M 1 |  |
| :--- | :--- | :---: | :--- |
|  | $1.5 \times 0.6=0.9$ | M 1 |  |
|  | Outside of 26.1 | A1ft | their 26.1 accept 23.7-26.1 or equiv. interval |


| $\mathbf{1 4 ( c ) ( i )}$ | Supplier C | B1 |  |
| :--- | :--- | :--- | :--- |


| $\mathbf{1 4 ( c ) ( i i ) ~}$ | Supplier B above the median $50 \%$ <br> scrapped | E1 | or as a result of median |
| :--- | :--- | :---: | :--- |
|  | Supplier A rejects at upper end | E1 | or outside of limits |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\mathbf{1 4 ( d )}$ | Cost, on time delivery,quality | B1 | oe |
| :--- | :--- | :--- | :--- |


| $\mathbf{1 5 ( a )}$ | Tree diagram: first set of branches | B1 |  |
| :--- | :--- | :---: | :--- |
|  | remaining sets | B1 $\times 3$ |  |


| 15(b) | $1-\operatorname{Pr}$ (late) | M1 | or $\mathrm{P}(\mathrm{E})+\mathrm{P}(\mathrm{T})$ |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { Any one of: } \\ & 0.3 \times \text { their } 0.2(=0.06) \\ & \text { or their } 0.25 \times \text { 'their' } 0.23 \\ & \quad(=0.0575) \\ & \text { or 'their' } 0.45 \times \text { 'their' } 0.05 \\ & \quad(=0.0225) \end{aligned}$ | M1 | Any one of: <br> $0.3 \times$ 'their' $0.65(=0.195)$ <br> their $0.25 \times$ their $0.12(=0.03)$ <br> 'their' $0.45 \times$ their $0.75(=0.3375)$ <br> $0.3 \times 0.15(=0.045)$ <br> their $0.25 \times 0.65(=0.1625)$ <br> 'their' $0.45 \times 0.2(=0.09)$ |
|  | $\begin{aligned} & \text { 'their' } 0.06+\text { 'their' } 0.0575 \\ & \text { + 'their' } 0.0225 \end{aligned}$ | M1 dep | All 6 added |
|  | $1-(0.06+0.0575+0.0225)=0.86$ | A1 | $0.5625+0.2975=0.86$ |


| $\mathbf{1 5 ( c )}$ | their $0.75+0.2=0.95$ | M1, A1 | cao their $0.4275 /$ their 0.45 M1 |
| :--- | :--- | :--- | :--- | :--- |


| $\mathbf{1 5}(\mathbf{d})$ | $(1-0.86)=0.14$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | $(0.14 \times 0.14 \times 0.86)$ | M1, A1 |  |
|  | $\times 3$ | M1 |  |
|  | $=0.0505(68)$ | A1 | cao accept 0.0506 or 0.051 |

