



UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS  
General Certificate of Education  
Advanced Subsidiary Level and Advanced Level

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**MATHEMATICS (US)**

**9280/01**

Paper 1 Pure Mathematics 1 (P1)

**For Examination from 2013**

SPECIMEN MARK SCHEME

**1 hour 45 minutes**

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**MAXIMUM MARK: 75**

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This document consists of **6** printed pages.



## **Mark Scheme Notes**

Marks are of the following three types:

**M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips, or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g., by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark, and in some cases an M mark can be implied from a correct answer.

**A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

**B** Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more “method” steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol  $\nabla$  implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously “correct” answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.  
B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g., wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained that is correct to 3 s.f., or that would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers that arise from taking  $g$  equal to 9.8 or 9.81 instead of 10.

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasizing that no “follow through” from a previous error is allowed)
CWO	Correct Working Only often written by a “fortuitous” answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
SOS	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

### **Penalties**

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become “follow through  $\checkmark$ ” marks. MR is not applied when the candidate misreads their own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

<p><b>1</b> <math>{}^7C_2 x^5 \left(\frac{2}{x^2}\right)^4</math> SOI and leading to final answer</p> <p>84 or <math>84x</math> as final answer</p>	<p>B2</p> <p>B1</p> <p>[3]</p>	<p>B1 for 2/3 parts correct leading to ans.</p> <p>If no answer: <math>84x</math> seen scores B2, else <math>{}^7C_2 x^5 \left(\frac{2}{x^2}\right)^2</math> scores SCB1 only</p>
<p><b>2</b> <math>\left(\frac{dv}{dr} = \right) 4\pi r^2</math></p> <p><math>= 4\pi \times 10^2</math></p> <p><math>\frac{dr}{dt} = \frac{dv}{dt} \frac{dv}{dr}</math> <b>OE used</b></p> <p><math>\frac{50}{4\pi \times 10^2} = \frac{1}{8\pi}</math> or 0.0398</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>[4]</p>	<p>SOI at any point</p> <p>Correct link between differentials with <math>\frac{dr}{dt}</math> finally as subject</p> <p>Allow <math>\frac{50}{400\pi}</math>.</p> <p>Non-calculus methods <math>\frac{0}{4}</math></p>
<p><b>3 (i)</b> Correct shape – touching positive <math>x</math>-axis</p> <p><b>(ii)</b> <math>(\pi) \int (x-2)^4 dx</math></p> <p><math>(\pi) \left[ \frac{(x-2)^5}{5} \right]</math></p> <p><math>(\pi) [0 - (-32)/5]</math></p> <p><math>\frac{32\pi}{5}</math> or <math>6.4\pi</math></p>	<p>B1</p> <p>[1]</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>[4]</p>	<p>Ignore intersections with axes</p> <p>Use <math>(\pi) \int y^2 dx</math> &amp; attempt integrate but expansion before integrand needs 5 terms</p> <p>Use of limits 0, 2 on <i>their</i> <math>(\pi) \int y^2 dx</math> cao Rotation about <math>y</math>-axis max 1/5</p>
<p><b>4 (i)</b> <math>\vec{CP} = -6\mathbf{i} + 6\mathbf{j} - 2\mathbf{k}</math></p> <p><math>\vec{CQ} = -6\mathbf{i} + 6\mathbf{j} + 3\mathbf{k}</math></p> <p><b>(ii)</b> Scalar product = <math>36 + 36 - 6</math></p> <p><math>66 =  \vec{CP}   \vec{CQ}  \cos \theta</math></p> <p><math> \vec{CP}  = \sqrt{76}</math>, <math> \vec{CQ}  = \sqrt{81}</math></p> <p>Angle <math>PCQ = 32.7^\circ</math> (or <math>0.571</math> rad)</p>	<p>B1</p> <p>B1</p> <p>[2]</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>[4]</p>	<p>Use of <math>x_1x_2 + y_1y_2 + z_1z_2</math></p> <p>Linking everything correctly</p> <p>Correct magnitude for either cao <math>147.3^\circ</math> converted to <math>32.7^\circ</math> gets A0</p>

<p>5 (i) <math>\frac{2\sin^2 \theta \sin^2 \theta}{1 - \sin^2 \theta} = 1</math>  <math>2\sin^4 \theta + \sin^2 \theta - 1 = 0</math></p> <p>(ii) <math>(2\sin^2 \theta - 1)(\sin^2 \theta + 1) = 0</math>  <math>\sin \theta = \frac{(\pm)1}{\sqrt{2}}</math>  <math>\theta = 45^\circ, 135^\circ</math>  <math>\theta = 225^\circ, 315^\circ</math></p>	<p>M1 A1 [2] M1 A1 A1 A1 [4]</p>	<p>Equation as function of <math>\sin \theta</math></p> <p><b>AG</b></p> <p>Or use formula on quadratic in <math>\sin^2 \theta</math></p> <p>Provided no excess solutions in range</p>
<p>6 (i) <math>z = 3x + 2\left(\frac{600}{x}\right)</math> or <math>x\frac{(z-3x)}{2} = 600 \rightarrow</math> <b>AG</b></p> <p>(ii) <math>\frac{dz}{dx} = 3 - \frac{1200}{x^2}</math> or <math>\frac{dz}{dy} = 2 - \frac{1800}{y^2}</math>  <math>= 0 \rightarrow x = 20</math> or <math>= 0 \rightarrow y = 30</math>  <math>z = 60 + \frac{120}{20} = 120</math>  <math>\frac{d^2z}{dx^2} = \frac{2400}{x^3}</math>  <math>&gt; 0 \Rightarrow</math> minimum</p>	<p>B1 [1] B1 M1A1 A1<sup>h</sup> B1<sup>h</sup> B1 [6]</p>	<p>OE</p> <p>Set to 0 &amp; attempt to solve. Allow <math>\pm 20</math>  Ft from <i>their</i> <math>x</math> provided positive  Or other valid method</p> <p>Dep. on <math>\frac{d^2z}{dx^2} = \frac{k}{x^3}</math> (<math>k &gt; 0</math>) or other  valid method.</p>
<p>7 (i) <math>\frac{3(1+2x)^{-1}}{-1} + (c)</math>  <math>y = \frac{3(1+2x)^{-1}}{-2} + (c)</math>  Sub (1, (1/2))  <math>\frac{1}{2} = \frac{3}{-6} + c \Rightarrow c = 1</math></p> <p>(ii) <math>(1+2x)^2 (&gt;) 9</math> or <math>4x^2 + 4x - 8 (&gt;) 0</math>  1, -2  <math>x &gt; 1, x &lt; -2</math> ISW</p>	<p>B1 B1(indep) M1 A1 [4] M1 A1 A1 [3]</p>	<p>Division by 2 <math>y =</math> necessary  Dependent on <math>c</math> present</p> <p>Use of <math>y = mx + c</math> etc. gets 0/4</p> <p><b>OE</b></p>
<p>8 (i) 1000, 2000, 3000... or 50, 100, 150...  <math>\frac{40}{2(1000 + 40000)}</math> or <math>\frac{40}{2(2000 + 39000)}</math>  <math>\times 5\%</math> of attempt at valid sum  41000</p> <p>(ii) 1000, <math>1000 \times 1.1</math>, <math>1000 \times 1.1^2 + \dots</math> or with <math>a = 50</math>  <math>\frac{1000(1.1^{40} - 1)}{1.1 - 1}</math>  22100</p>	<p>M1 M1 M1 A1 [4] M1 M1 A1 [3]</p>	<p>Recognize series, correct <math>a/d</math> (or 3 terms )</p> <p>Correct use of formula</p> <p>Can be awarded in either (i) or (ii)  cao</p> <p>Recognize series, correct <math>a/r</math> (or 3 terms)</p> <p>Correct use of formula. Allow e.g. <math>r = 0.1</math></p> <p>Or answers rounding to this</p>

<p><b>9 (i)</b> <math>AS = r \tan \theta</math>  Area <math>OAB = r^2 \tan \theta</math> or <math>(OAS) = \frac{1}{2} r^2 \tan \theta</math>  Area of sector = <math>\frac{1}{2} r^2 \times 2\theta (= r^2 \theta)</math>  Shaded area = <math>r^2 (\tan \theta - \theta)</math></p>	M1 A1 B1 A1  [4]	Or $(AB) = 2r \tan \theta$ or $(AO) = \frac{r}{\cos \theta}$  Or $OAB = \frac{1}{2} \frac{r^2}{\cos 2\theta} \sin 2\theta$ <b>OE</b> Or area sector $(OPS) = \frac{1}{2} r^2 \theta$ Allow e.g. $r^2 \tan \theta - \frac{1}{2} r^2 2\theta$
<p><b>(ii)</b> <math>\cos \frac{\pi}{3} = \frac{6}{OA} \Rightarrow OA = 12</math>  <math>AP = 6</math>  <math>AS = 6 \tan \frac{\pi}{3} = \frac{6}{OA} \Rightarrow OA = 12</math>  Arc <math>(PST) = 12 \frac{\pi}{3}</math>  Perimeter = <math>12 + 12\sqrt{3} + 4\pi</math></p>	M1 A1 B1 B1 A1  [5]	  Or arc $(PS) = 6 \frac{\pi}{3}$ or arc $(ST) = 6 \frac{\pi}{3}$ Allow unsimplified $4\pi$
<p><b>10 (i)</b> <math>2(x-1)^2 - 1</math> OR <math>a = 2, b = -1, c = -1</math>  <math>A = (1, -1)</math></p> <p><b>(ii)</b> <math>2x^2 - 5x - 3 = 0 \Rightarrow (2x+1)(x-3) = 0</math>  <math>x = -\frac{1}{2}, y = 3\frac{1}{2}</math></p> <p><b>(iii)</b> Mid point of <math>AP = (2, 3)</math>  Slope of line = <math>\frac{\frac{1}{2}}{\frac{-5}{2}} = \frac{-1}{5}</math>  Equation is <math>y - 3 = \frac{-1}{5}(x - 2)</math></p>	B1, B1, B1 B1✓ [4] M1, M1 A1 [3] B1✓ B1 B1 [3]	Allow alt. method for final mark  <b>OE</b> in $y$ Complete elim & simplify, attempt soln. Additional (3, 7) not penalized Follow through on <i>their A</i>  <b>OE</b> Or $y - 3\frac{1}{2} = -\frac{1}{5(x + \frac{1}{2})}$
<p><b>11 (i)</b> <math>f(g(x)) = 2x^2 - 3, \quad g(f(x)) = 4x^2 + 4x - 1</math></p> <p><b>(ii)</b> <math>2a^2 - 3 = 4a^2 + 4a - 1 \Rightarrow 2a^2 + 4a + 2 = 0</math>  <math>(a+1)^2 = 0</math>  <math>a = -1</math></p> <p><b>(iii)</b> <math>b^2 - b - 2 = 0 \rightarrow (b+1)(b-2) = 0</math>  <math>b = 2</math> Allow <math>b = -1</math> in addition</p> <p><b>(iv)</b> <math>f^{-1}(x) = \frac{1}{2}(x-1)</math>  <math>f^{-1}(g(x)) = \frac{1}{2}(x^2 - 3)</math></p> <p><b>(v)</b> <math>x = (\pm)\sqrt{y+2}</math>  <math>h^{-1}(x) = -\sqrt{x+2}</math></p>	B1, B1 [2] M1 M1 A1 [3] M1 A1 [2] B1 B1✓ [2] M1 A1 [2]	fg and gf clearly transposed gets B0B0  Dep. quadratic. Allow $x$ for all 3 marks Allow marks in <b>(ii)</b> if transposed in <b>(i)</b>  Allow in terms of $x$ for M1 only Correct answer without working B2  Must be simplified. Ft from <i>their</i> $f^{-1}$