## ADVANCED SUBSIDIARY GCE MATHEMATICS (MEI) <br> Further Concepts for Advanced Mathematics (FP1)

Candidates answer on the Answer Booklet
Thursday 27 May 2010
OCR Supplied Materials: Morning

- 8 page Answer Booklet
- MEI Examination Formulae and Tables (MF2)

Other Materials Required:

- Scientific or graphical calculator

Duration: 1 hour 30 minutes

## INSTRUCTIONS TO CANDIDATES

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer all the questions.
- Do not write in the bar codes.
- You are permitted to use a graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.


## INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [ ] at the end of each question or part question.
- You are advised that an answer may receive no marks unless you show sufficient detail of the working to indicate that a correct method is being used.
- The total number of marks for this paper is 72.
- This document consists of 4 pages. Any blank pages are indicated.


## Section A (36 marks)

1 Find the values of $A, B$ and $C$ in the identity $4 x^{2}-16 x+C \equiv A(x+B)^{2}+2$.

2 You are given that $\mathbf{M}=\left(\begin{array}{rr}2 & -5 \\ 3 & 7\end{array}\right)$.
$\mathbf{M}\binom{x}{y}=\binom{9}{-1}$ represents two simultaneous equations.
(i) Write down these two equations.
(ii) Find $\mathbf{M}^{-1}$ and use it to solve the equations.

3 The cubic equation $2 z^{3}-z^{2}+4 z+k=0$, where $k$ is real, has a root $z=1+2 \mathrm{j}$.
Write down the other complex root. Hence find the real root and the value of $k$.

4 The roots of the cubic equation $x^{3}-2 x^{2}-8 x+11=0$ are $\alpha, \beta$ and $\gamma$. Find the cubic equation with roots $\alpha+1, \beta+1$ and $\gamma+1$.

5 Use the result $\frac{1}{5 r-1}-\frac{1}{5 r+4} \equiv \frac{5}{(5 r-1)(5 r+4)}$ and the method of differences to find

$$
\sum_{r=1}^{n} \frac{1}{(5 r-1)(5 r+4)}
$$

simplifying your answer.

6 A sequence is defined by $u_{1}=2$ and $u_{n+1}=\frac{u_{n}}{1+u_{n}}$.
(i) Calculate $u_{3}$.
(ii) Prove by induction that $u_{n}=\frac{2}{2 n-1}$.

Section B (36 marks)
7 Fig. 7 shows an incomplete sketch of $y=\frac{(2 x-1)(x+3)}{(x-3)(x-2)}$.


Fig. 7
(i) Find the coordinates of the points where the curve cuts the axes.
(ii) Write down the equations of the three asymptotes.
(iii) Determine whether the curve approaches the horizontal asymptote from above or below for large positive values of $x$, justifying your answer. Copy and complete the sketch.
(iv) Solve the inequality $\frac{(2 x-1)(x+3)}{(x-3)(x-2)}<2$.

8 Two complex numbers, $\alpha$ and $\beta$, are given by $\alpha=\sqrt{3}+\mathrm{j}$ and $\beta=3 \mathrm{j}$.
(i) Find the modulus and argument of $\alpha$ and $\beta$.
(ii) Find $\alpha \beta$ and $\frac{\beta}{\alpha}$, giving your answers in the form $a+b \mathrm{j}$, showing your working.
(iii) Plot $\alpha, \beta, \alpha \beta$ and $\frac{\beta}{\alpha}$ on a single Argand diagram.

9 The matrices $\mathbf{P}=\left(\begin{array}{rr}0 & 1 \\ -1 & 0\end{array}\right)$ and $\mathbf{Q}=\left(\begin{array}{ll}2 & 0 \\ 0 & 1\end{array}\right)$ represent transformations $P$ and $Q$ respectively.
(i) Describe fully the transformations P and Q .


Fig. 9

Fig. 9 shows triangle T with vertices $\mathrm{A}(2,0), \mathrm{B}(1,2)$ and $\mathrm{C}(3,1)$.
Triangle T is transformed first by transformation P , then by transformation Q .
(ii) Find the single matrix that represents this composite transformation.
(iii) This composite transformation maps triangle T onto triangle $\mathrm{T}^{\prime}$, with vertices $\mathrm{A}^{\prime}, \mathrm{B}^{\prime}$ and $\mathrm{C}^{\prime}$. Calculate the coordinates of $\mathrm{A}^{\prime}, \mathrm{B}^{\prime}$ and $\mathrm{C}^{\prime}$.
$\mathrm{T}^{\prime}$ is reflected in the line $y=-x$ to give a new triangle, $\mathrm{T}^{\prime \prime}$.
(iv) Find the matrix $\mathbf{R}$ that represents reflection in the line $y=-x$.
(v) A single transformation maps $\mathrm{T}^{\prime \prime}$ onto the original triangle, T. Find the matrix representing this transformation.

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