## ADVANCED SUBSIDIARY GCE <br> MATHEMATICS

Core Mathematics 2

## QUESTION PAPER

Candidates answer on the Printed Answer Book
OCR Supplied Materials:

- Printed Answer Book 4722
- List of Formulae (MF1)

Other Materials Required:

- Scientific or graphical calculator

Friday 22 May 2009
Morning
Duration: 1 hour 30 minutes

## INSTRUCTIONS TO CANDIDATES

These instructions are the same on the Printed Answer Book and the Question Paper.

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Printed Answer Book.
- The questions are on the inserted Question Paper.
- Write your answer to each question in the space provided in the Printed Answer Book. Additional paper may be used if necessary but you must clearly show your Candidate Number, Centre Number and question number(s).
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer all the questions.
- Do not write in the bar codes.
- You are permitted to use a graphical calculator in this paper.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.


## INFORMATION FOR CANDIDATES

This information is the same on the Printed Answer Book and the Question Paper.

- The number of marks is given in brackets [ ] at the end of each question or part question on the Question Paper.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is 72.
- The Printed Answer Book consists of 12 pages. The Question Paper consists of $\mathbf{4}$ pages. Any blank pages are indicated.


## INSTRUCTION TO EXAMS OFFICER / INVIGILATOR

- Do not send this Question Paper for marking; it should be retained in the centre or destroyed.

1 The lengths of the three sides of a triangle are $6.4 \mathrm{~cm}, 7.0 \mathrm{~cm}$ and 11.3 cm .
(i) Find the largest angle in the triangle.
(ii) Find the area of the triangle.

2 The tenth term of an arithmetic progression is equal to twice the fourth term. The twentieth term of the progression is 44 .
(i) Find the first term and the common difference.
(ii) Find the sum of the first 50 terms.

3 Use logarithms to solve the equation $7^{x}=2^{x+1}$, giving the value of $x$ correct to 3 significant figures.

4 (i) Find the binomial expansion of $\left(x^{2}-5\right)^{3}$, simplifying the terms.
(ii) Hence find $\int\left(x^{2}-5\right)^{3} \mathrm{~d} x$.

5 Solve each of the following equations for $0^{\circ} \leqslant x \leqslant 180^{\circ}$.
(i) $\sin 2 x=0.5$
(ii) $2 \sin ^{2} x=2-\sqrt{3} \cos x$

6 The gradient of a curve is given by $\frac{\mathrm{d} y}{\mathrm{~d} x}=3 x^{2}+a$, where $a$ is a constant. The curve passes through the points $(-1,2)$ and $(2,17)$. Find the equation of the curve.

7 The polynomial $\mathrm{f}(x)$ is given by $\mathrm{f}(x)=2 x^{3}+9 x^{2}+11 x-8$.
(i) Find the remainder when $\mathrm{f}(x)$ is divided by $(x+2)$.
(ii) Use the factor theorem to show that $(2 x-1)$ is a factor of $\mathrm{f}(x)$.
(iii) Express $\mathrm{f}(x)$ as a product of a linear factor and a quadratic factor.
(iv) State the number of real roots of the equation $\mathrm{f}(x)=0$, giving a reason for your answer.


Fig. 1

Fig. 1 shows a sector $A O B$ of a circle, centre $O$ and radius $O A$. The angle $A O B$ is 1.2 radians and the area of the sector is $60 \mathrm{~cm}^{2}$.
(i) Find the perimeter of the sector.

A pattern on a T-shirt, the start of which is shown in Fig. 2, consists of a sequence of similar sectors. The first sector in the pattern is sector $A O B$ from Fig. 1, and the area of each successive sector is $\frac{3}{5}$ of the area of the previous one.


Fig. 2
(ii) (a) Find the area of the fifth sector in the pattern.
(b) Find the total area of the first ten sectors in the pattern.
(c) Explain why the total area will never exceed a certain limit, no matter how many sectors are used, and state the value of this limit.

9 (i) Sketch the graph of $y=4 k^{x}$, where $k$ is a constant such that $k>1$. State the coordinates of any points of intersection with the axes.
(ii) The point $P$ on the curve $y=4 k^{x}$ has its $y$-coordinate equal to $20 k^{2}$. Show that the $x$-coordinate of $P$ may be written as $2+\log _{k} 5$.
(iii) (a) Use the trapezium rule, with two strips each of width $\frac{1}{2}$, to find an expression for the approximate value of

$$
\begin{equation*}
\int_{0}^{1} 4 k^{x} \mathrm{~d} x \tag{3}
\end{equation*}
$$

(b) Given that this approximate value is equal to 16 , find the value of $k$.

There are no questions printed on this page.

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