

ADVANCED GCE

MATHEMATICS (MEI)

Methods for Advanced Mathematics (C3)

4753/01

QUESTION PAPER

Candidates answer on the printed answer book.

OCR supplied materials:

- Printed answer book 4753/01
- MEI Examination Formulae and Tables (MF2)

Other materials required:

- Scientific or graphical calculator

Wednesday 19 January 2011

Afternoon

Duration: 1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

These instructions are the same on the printed answer book and the question paper.

- The question paper will be found in the centre of the printed answer book.
- Write your name, centre number and candidate number in the spaces provided on the printed answer book. Please write clearly and in capital letters.
- **Write your answer to each question in the space provided in the printed answer book.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Answer **all** the questions.
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

INFORMATION FOR CANDIDATES

This information is the same on the printed answer book and the question paper.

- The number of marks is given in brackets [] at the end of each question or part question on the question paper.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.
- The total number of marks for this paper is **72**.
- The printed answer book consists of **12** pages. The question paper consists of **8** pages. Any blank pages are indicated.

INSTRUCTION TO EXAMS OFFICER / INVIGILATOR

- Do not send this question paper for marking; it should be retained in the centre or destroyed.

Section A (36 marks)

- 1 Given that $y = \sqrt[3]{1+x^2}$, find $\frac{dy}{dx}$. [4]
- 2 Solve the inequality $|2x + 1| \geq 4$. [4]
- 3 The area of a circular stain is growing at a rate of 1 mm^2 per second. Find the rate of increase of its radius at an instant when its radius is 2 mm. [5]
- 4 Use the triangle in Fig. 4 to prove that $\sin^2 \theta + \cos^2 \theta = 1$. For what values of θ is this proof valid? [3]

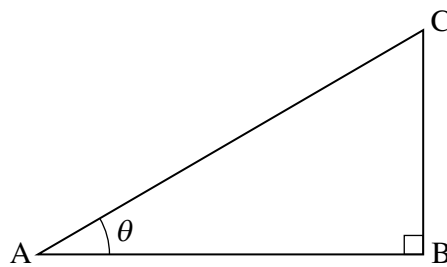


Fig. 4

- 5 (i) On a single set of axes, sketch the curves $y = e^x - 1$ and $y = 2e^{-x}$. [3]
- (ii) Find the exact coordinates of the point of intersection of these curves. [5]
- 6 A curve is defined by the equation $(x + y)^2 = 4x$. The point $(1, 1)$ lies on this curve.
- By differentiating implicitly, show that $\frac{dy}{dx} = \frac{2}{x+y} - 1$.
- Hence verify that the curve has a stationary point at $(1, 1)$. [4]

- 7 Fig. 7 shows the curve $y = f(x)$, where $f(x) = 1 + 2 \arctan x$, $x \in \mathbb{R}$. The scales on the x - and y -axes are the same.

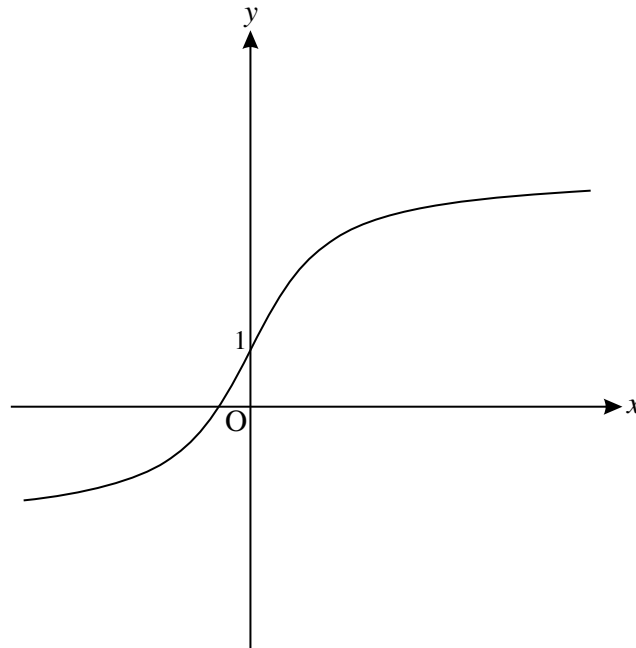


Fig. 7

- (i) Find the range of f , giving your answer in terms of π . [3]
- (ii) Find $f^{-1}(x)$, and add a sketch of the curve $y = f^{-1}(x)$ to the copy of Fig. 7. [5]

Section B (36 Marks)

- 8 (i) Use the substitution $u = 1 + x$ to show that

$$\int_0^1 \frac{x^3}{1+x} dx = \int_a^b \left(u^2 - 3u + 3 - \frac{1}{u} \right) du,$$

where a and b are to be found.

Hence evaluate $\int_0^1 \frac{x^3}{1+x} dx$, giving your answer in exact form. [7]

Fig. 8 shows the curve $y = x^2 \ln(1+x)$.

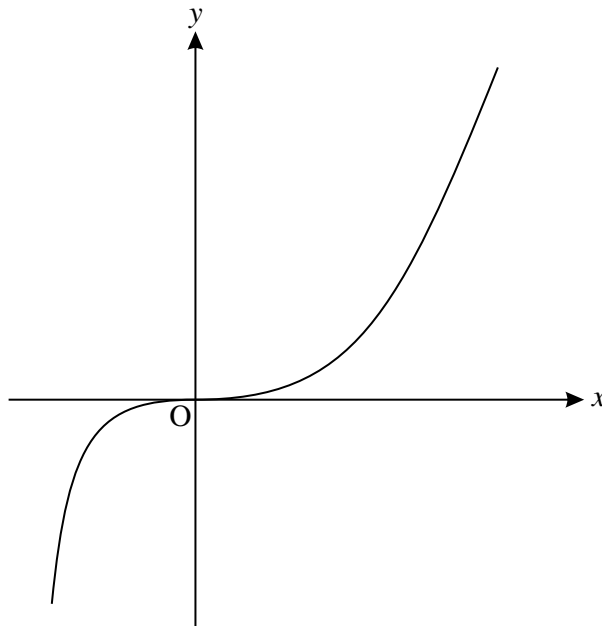


Fig. 8

- (ii) Find $\frac{dy}{dx}$.

Verify that the origin is a stationary point of the curve. [5]

- (iii) Using integration by parts, and the result of part (i), find the exact area enclosed by the curve $y = x^2 \ln(1+x)$, the x -axis and the line $x = 1$. [6]

- 9 Fig. 9 shows the curve $y = f(x)$, where $f(x) = \frac{1}{\cos^2 x}$, $-\frac{1}{2}\pi < x < \frac{1}{2}\pi$, together with its asymptotes $x = \frac{1}{2}\pi$ and $x = -\frac{1}{2}\pi$.

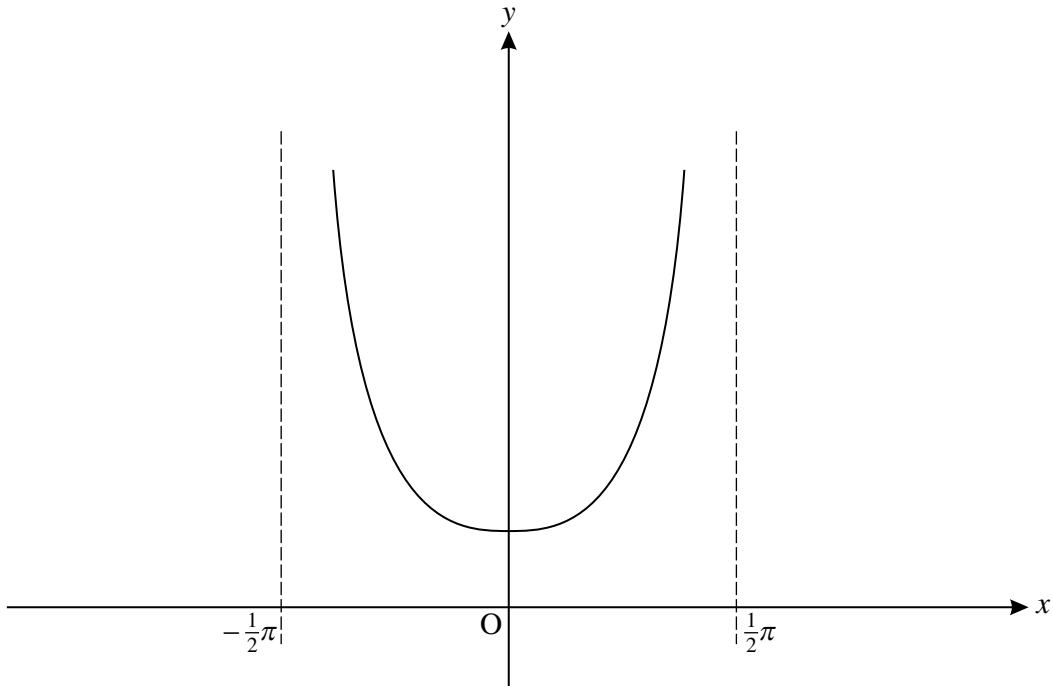


Fig. 9

- (i) Use the quotient rule to show that the derivative of $\frac{\sin x}{\cos x}$ is $\frac{1}{\cos^2 x}$. [3]

- (ii) Find the area bounded by the curve $y = f(x)$, the x -axis, the y -axis and the line $x = \frac{1}{4}\pi$. [3]

The function $g(x)$ is defined by $g(x) = \frac{1}{2}f(x + \frac{1}{4}\pi)$.

- (iii) Verify that the curves $y = f(x)$ and $y = g(x)$ cross at $(0, 1)$. [3]

- (iv) State a sequence of two transformations such that the curve $y = f(x)$ is mapped to the curve $y = g(x)$.

On the copy of Fig. 9, sketch the curve $y = g(x)$, indicating clearly the coordinates of the minimum point and the equations of the asymptotes to the curve. [8]

- (v) Use your result from part (ii) to write down the area bounded by the curve $y = g(x)$, the x -axis, the y -axis and the line $x = -\frac{1}{4}\pi$. [1]

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Candidate forename		Candidate surname	
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Centre number						Candidate number				
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Section A (36 marks)

1	
2	

5 (i)

5 (ii)

6	



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7 (i)

7 (ii)

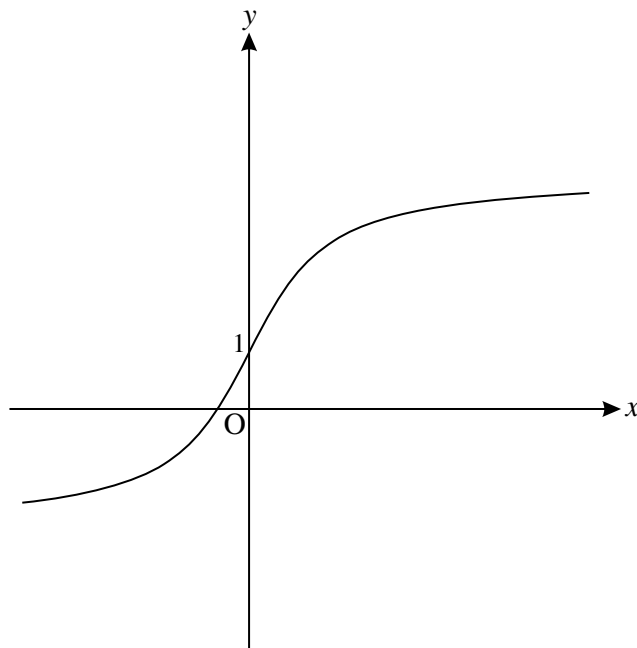


Fig. 7

Section B (36 marks)

8 (i)	

8 (ii)	

8 (iii)	
9 (i)	

9 (ii)	
9 (iii)	

9 (iv)

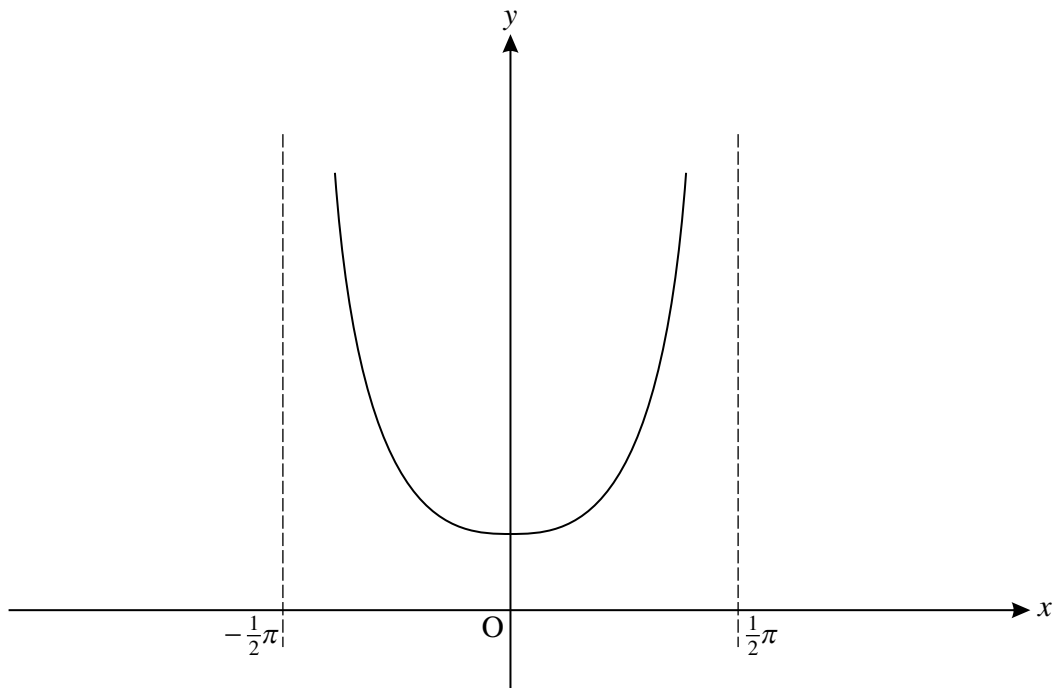


Fig. 9

9 (v)