



UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

0581/43 **MATHEMATICS**

Paper 4 (Extended) October/November 2012

2 hours 30 minutes

Candidates answer on the Question Paper.

Additional Materials: Electronic calculator Geometrical instruments

Mathematical tables (optional) Tracing paper (optional)

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

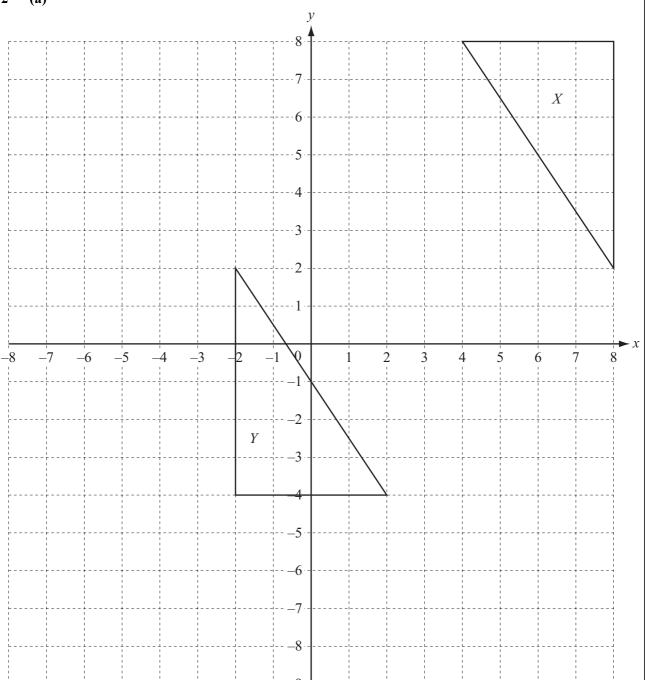
The total of the marks for this paper is 130.

1 (a)		e Martinez family travels by car to Seatown. e distance is 92 km and the journey takes 1 hour 25 minutes.	
	(i)	The family leaves home at 07 50. Write down the time they arrive at Seatown.	
	48 0	$Answer(a)(i) \qquad \qquad [1]$	
	(ii)	Calculate the average speed for the journey.	
		Answer(a)(ii) km/h [2]	
	(iii)	During the journey, the family stops for 10 minutes.	
		Calculate 10 minutes as a percentage of 1 hour 25 minutes.	
		Answer(a)(iii) $\%$ [1]	
	(iv)	92 km is 15% more than the distance from Seatown to Deecity.	
		Calculate the distance from Seatown to Deecity.	
		Answer(a)(iv) km [3]	

(b)	The	e Martinez family spends \$150 in the ratio			
		fuel: meals: gifts = $11:16:3$.			
	(i)	Show that \$15 is spent on gifts.			
		Answer (b)(i)			
					[2]
	(ii)	The femily have two eifte			[2]
	(11)	The family buys two gifts. The first gift costs \$8.25.			
		Find the ratio			
		cost of first gift : cost of second gift.			
		Give your answer in its simplest form.			
			Answer(b)(ii)	:	[2]

2 (a)

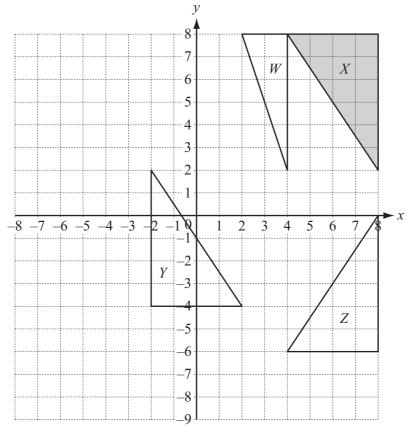
For Examiner's Use



- (i) Draw the translation of triangle *X* by the vector $\begin{pmatrix} -11 \\ -1 \end{pmatrix}$. [2]
- (ii) Draw the enlargement of triangle Y with centre (-6, -4) and scale factor $\frac{1}{2}$. [2]

(b)

Examiner's Use



Describe fully the **single** transformation that maps

(i) triangle X onto triangle Z,

(ii) triangle X onto triangle Y,

(iii) triangle X onto triangle W.

Answer(b)(i)	 [2]

- Answer(b)(ii) [3]
- Answer(b)(iii) [3]
- (c) Find the matrix that represents the transformation in part (b)(iii).

Answer(c) [2]

3

netal cuboid has a volume of 1080 cm ³ and a mass of	f8kg.		
Calculate the mass of one cubic centimetre of the rigid Give your answer in grams.	metal.		
	Answer(a)	{	g [1]
The base of the cuboid measures 12 cm by 10 cm.			
Calculate the height of the cuboid.			
	Answer(b)	cm	[2]
The cuboid is melted down and made into a sphere	with radius r cm.		
(i) Calculate the value of r .	4		
[The volume, V , of a sphere with radius r is V	$=\frac{4}{3}\pi r^3.$		
	Answer(c)(i) r =		[3]
	Calculate the mass of one cubic centimetre of the regive your answer in grams. The base of the cuboid measures 12 cm by 10 cm. Calculate the height of the cuboid. The cuboid is melted down and made into a sphere (i) Calculate the value of r.	The base of the cuboid measures 12 cm by 10 cm. Calculate the height of the cuboid. Answer(b) The cuboid is melted down and made into a sphere with radius r cm. (i) Calculate the value of r . [The volume, V , of a sphere with radius r is $V = \frac{4}{3}\pi r^3$.]	Calculate the mass of one cubic centimetre of the metal. Give your answer in grams. Answer(a)

	(ii)	Calculate the surface area of the sphere.
		[The surface area, A, of a sphere with radius r is $A = 4\pi r^2$.]
		$Answer(c)(ii) \qquad cm^2 [2]$
(d)	The par	arger sphere has a radius R cm. surface area of the sphere with radius r cm in \mathbf{t} (c). d the value of $\frac{R}{r}$.
		$Answer(d) \qquad \qquad [2]$

4

$$f(x) = \frac{2}{x^2} - 3x, \ x \neq 0$$

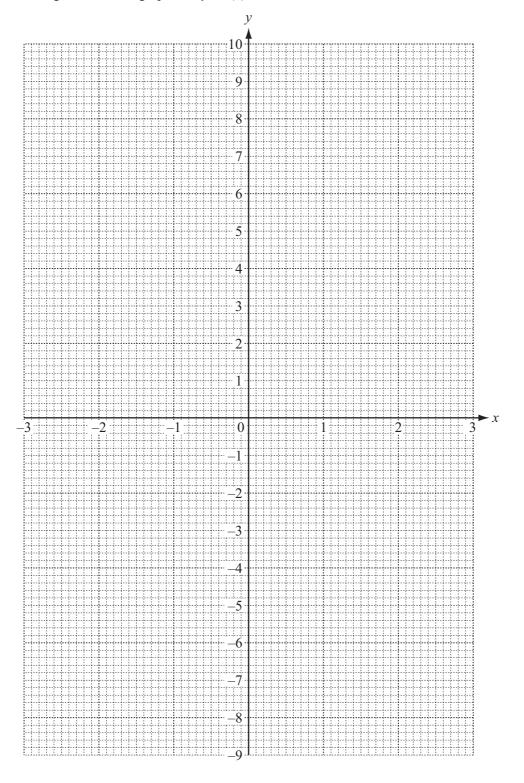
Examiner's Use

(a) Complete the table.

х	-3	-2.5	-2	-1.5	-1	-0.5	0.5	1	1.5	2	2.5	3
f(x)	9.2	7.8	6.5	5.4		9.5	6.5		-3.6	-5.5	-7.2	-8.8

[2]

(b) On the grid, draw the graph of y = f(x), for $-3 \le x \le -0.5$ and $0.5 \le x \le 3$.



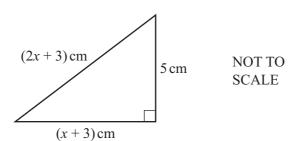
[5]

	e your graph to solve the equations. $f(x) = 4$	For Examiner'. Use
	Answer(c)(i) x = $f(x) = 3x$ [1]	
	Answer(c)(ii) x = [2]	
	e equation $f(x) = 3x$ can be written as $x^3 = k$. d the value of k .	
1.111	d the value of k.	
	Answer(d) k =	
(e) (i)	Draw the straight line through the points $(-1, 5)$ and $(3, -9)$. [1]	
(ii)	Find the equation of this line.	
	<i>Answer(e)</i> (ii)[3]	
(iii)	Complete the statement.	
	The straight line in part (e)(ii) is a to the graph of $y = f(x)$. [1]	

5

(a)	Marcos buys 2 bottles		3 bottles of len	nonade.			
	The total cost is \$3.60		~ \$0.25 m and to	h a 41 a . a a 4 a C .	1	4	
	The cost of one bottle Find the cost of one b		s \$0.25 more t	nan the cost of o	one bottle of wa	ter.	
	Tilld the cost of one o	ottic of water.					
				Answer(a) \$			[4]
				Answer (a) \$			ניין
(b)					1		
		1		2		NOT TO	
	$5\mathrm{cm}^2$	ycm	6	cm ²	L / CIII	SCALE	
		_		2)			
	x cm		(x +	2) cm			
	The diagram shows to	wo rectangles.					
	The first rectangle me		y cm and has	an area of 5 cm ²			
	The second rectangle	measures $(x +$	2) cm by Ycm	and has an area	$1 \text{ of } 6 \text{ cm}^2$.		
	(i) When $y + Y = 1$,	ala a	0 10 – (`			
	(i) When $y + Y = 1$,	, snow that x	-9x - 10 = 0).			
	Answer (b)(i)						
							[4]
	(ii) Factorise $x^2 - 9$	0r - 10					
	(ii) Tactorise x	x 10.					
				Answer(b)(ii)			[2]
					•••••	•••••	r .1
((iii) Calculate the per	rimeter of the f	irst rectangle.				
				Answer(b)(iii)		cm	[2]

(c)



For Examiner's Use

The diagram shows a right-angled triangle with sides of length 5 cm, (x + 3) cm and (2x + 3) cm.

(i) Show that $3x^2 + 6x - 25 = 0$.

Answer (c)(i)

[4]

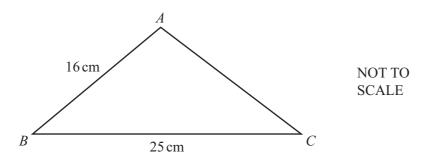
(ii) Solve the equation $3x^2 + 6x - 25 = 0$. Show all your working and give your answers correct to 2 decimal places.

(iii) Calculate the area of the triangle.

Answer(c)(iii) cm² [2]

6

For Examiner's Use



The area of triangle ABC is 130 cm^2 . AB = 16 cm and BC = 25 cm.

(a)	Show clearly th	at angle ABC	$=40.5^{\circ},$	correct to	one o	decimal	place
-----	-----------------	--------------	------------------	------------	-------	---------	-------

Answer (a)

[3]

(b) Calculate the length of *AC*.

(c) Calculate the shortest distance from A to BC.

Answer(c) cm [2]

7	(a)
/	(a)



Two discs are chosen at random without replacement from the five discs shown in the diagram.

(i) Find the probability that both discs are numbered 2.

Answer(a)(i) [2]

(ii) Find the probability that the numbers on the **two** discs have a total of 5.

Answer(a)(ii) [3]

(iii) Find the probability that the numbers on the two discs do **not** have a total of 5.

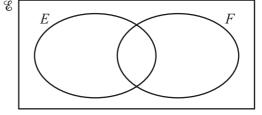
Answer(a)(iii) [1]

(b) A group of international students take part in a survey on the nationality of their parents.

 $E = \{\text{students with an English parent}\}\$

 $F = \{\text{students with a French parent}\}\$

 $n(\mathscr{C}) = 50, \ n(E) = 15, \ n(F) = 9 \ and \ n(E \cup F)' = 33.$



(i) Find $n(E \cap F)$.

Answer(b)(i) [1]

(ii) Find $n(E' \cup F)$.

Answer(b)(ii) [1]

(iii) A student is chosen at random. Find the probability that this student has an English parent and a French parent.

Answer(b)(iii) [1]

(iv) A student who has a French parent is chosen at random. Find the probability that this student also has an English parent.

Answer(b)(iv) [1]

8 (a)

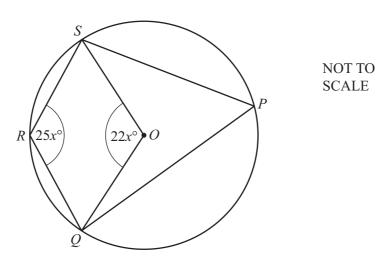
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В

A, B, C and D lie on a circle. The chords AC and BD intersect at X. Angle $BAC = 28^{\circ}$ and angle $AXD = 52^{\circ}$. Calculate angle XCD.

Answer(a) Angle XCD = [3]

(b)

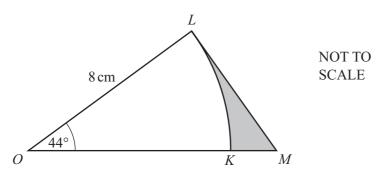


PQRS is a cyclic quadrilateral in the circle, centre *O*. Angle $QOS = 22x^{\circ}$ and angle $QRS = 25x^{\circ}$. Find the value of x.

Answer(b) x = [3]

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For Examiner's Use (c)



In the diagram OKL is a sector of a circle, centre O and radius 8 cm. OKM is a straight line and ML is a tangent to the circle at L. Angle $LOK = 44^{\circ}$.

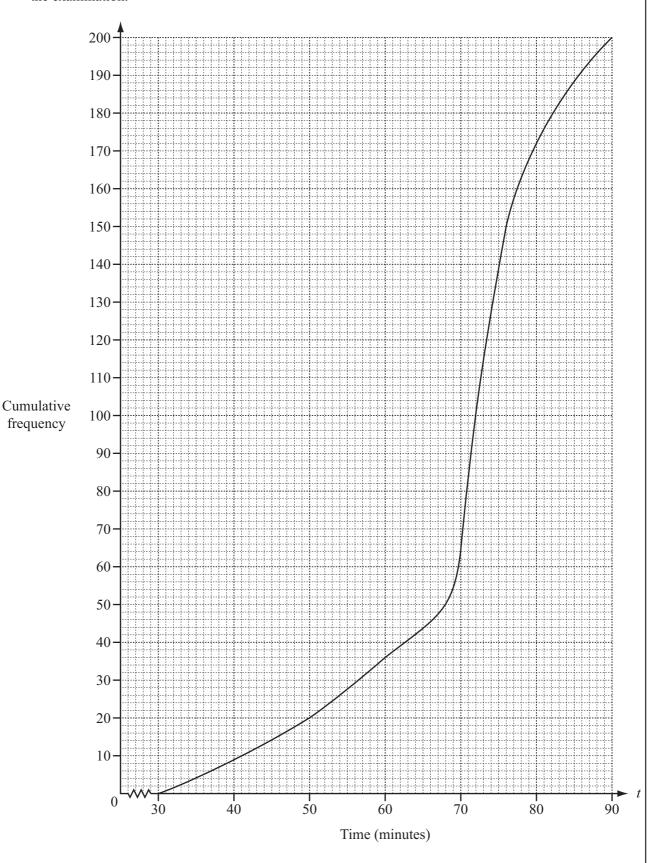
Calculate the area shaded in the diagram.

Answer(c)	cm^2	[5]
Answer (c)	 CIII	ردا

Examiner's Use 9 200 students take a Mathematics examination.

The cumulative frequency diagram shows information about the times taken, t minutes, to complete the examination.

For Examiner's Use



(a) Find							
(i)	the median,						
			A	Inswer(a)(i)		min [1]	
(ii)	the lower quartil	e,					
			A	Inswer(a)(ii)		min [1]	
(iii)	the inter-quartile	range,					
(iv)	the number of str	udents who took				min [1]	
(11)	the number of su	ducins who took				[2]	
(b) (i) Use the cumulative frequency diagram to complete the grouped frequency table.							
Time, t minutes	$30 < t \le 40$	$40 < t \le 50$	$50 < t \le 60$	$60 < t \le 70$	$70 < t \le 80$	$80 < t \le 90$	
Frequency	9		16	28	108	28	

[1]

Examiner's Use

(ii) Calculate an estimate of the mean time taken by the 200 students to complete the examination. Show all your working.

Answer(b)(ii) min [4]

10 (a) Complete the table for the 6th term and the nth term in each sequence.

For Examiner's Use

	Sequence	6th term	nth term
A	11, 9, 7, 5, 3		
В	1, 4, 9, 16, 25		
C	2, 6, 12, 20, 30		
D	3, 9, 27, 81, 243		
E	1, 3, 15, 61, 213		

- 4	_	
ı	- '	
,	-	

•	h)	Find	the	value	of the	100	th	term	in
١	U)	rinu	uic	varuc	or the	100	ш	tCIIII	ш

(i) Sequence A,

Answer(b)(i)	[1]
11.00,,0,	 L - 1

(ii) Sequence C.

(c)	Find the value of n in Sequence D when the n th term is equal to 6561.						
	Find the value of the 10th term in Sequence E .	$Answer(c) n = \dots$	[1]				
		Answer(d)	[1]				

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