



UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

CANDIDATE NAME						
CENTRE NUMBER				ANDIDATE JMBER		

MATHEMATICS

0581/42

Paper 4 (Extended)

October/November 2012

2 hours 30 minutes

Candidates answer on the Question Paper.

Additional Materials: Electronic calculator

Mathematical tables (optional)

Geometrical instruments Tracing paper (optional)

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 130.



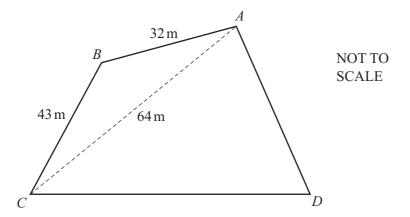
1

A f	actor	y produces bird food made with sunflower seed	, millet and ma	ize.	
(a)	The	amounts of sunflower seed, millet and maize a	re in the ratio		
		sunflower seed: millet: maize = $5:3:1$.			
	(i)	How much millet is there in 15 kg of bird food	!?		
			() (!)		1 507
					kg [2]
	(ii)	In a small bag of bird food there is 60 g of sun	flower seed.		
		What is the mass of bird food in a small bag?			
			Answer(a)(ii)		g [2]
			11.10.11.01.(0.0)(1.1)		8 [-]
(b)		iflower seeds cost \$204.50 for 30 kg from Jon's exchange rate is $$1 = €0.718$.	farm or €96.40) for 20kg from Ann's fa	arm.
		ich farm has the cheapest price per kilogram? u must show clearly all your working.			
			Answer(b)		[4]

(c)	Bags are filled with bird food at a rate of 420 grams per second.		For Examiner's
	How many 20 kg bags can be completely filled in 4 hours?		Use
	Answer(c)	[3]	
(d)	Brian buys bags of bird food from the factory and sells them in his shop for \$15.30 each. He makes 12.5% profit on each bag.		
	How much does Brian pay for each bag of bird food?		
	Answer(d) \$	[3]	
(e)	Brian orders 600 bags of bird food.		
	The probability that a bag is damaged is $\frac{1}{50}$.		
	How many bags would Brian expect to be damaged?		
	Answer(e)	[1]	
		<u> </u>	

2

For Examiner's Use



The diagram represents a field in the shape of a quadrilateral ABCD. AB = 32 m, BC = 43 m and AC = 64 m.

(a) (i) Show clearly that angle $CAB = 37.0^{\circ}$ correct to one decimal place.

Answer(a)(i)

[4]

(ii) Calculate the area of the triangle ABC.

Answer(a)(ii) _____ m² [2]

(b) $CD = 70 \,\text{m}$ and angle $DAC = 55^{\circ}$.

Calculate the perimeter of the whole field *ABCD*.

Answer(b) _____ m [6]

3	(a)	(i)	Factorise completely the expression $4x^2 - 18x - 10$.	
			Anguan(a)(i)	[2]
		(ii)	Answer(a)(i) Solve $4x^2 - 18x - 10 = 0$.	[3]
		()		
			Answer(a)(ii) x =	[1]
	(b)	Sol	we the equation $2x^2 - 7x - 10 = 0$.	
		Sho	ow all your working and give your answers correct to two decimal places.	
			Answer(b) x =	[4]
	(c)	Wr	ite $\frac{6}{3x-1} - \frac{2}{x-2}$ as a single fraction in its simplest form.	
			Answer(c)	[3]

4 (a)

A 32° B NOT TO SCALE

Points A, C and D lie on a circle centre O. BA and BC are tangents to the circle. Angle $ABC = 32^{\circ}$ and angle $DAB = 143^{\circ}$.

(i) Calculate angle AOC in quadrilateral AOCB.

Answer(a)(i) Angle AOC = [2]

(ii) Calculate angle ADC.

Answer(a)(ii) Angle ADC = [1]

(iii) Calculate angle OCD.

Answer(a)(iii) Angle OCD = [2]

(iv) OA = 6 cm.

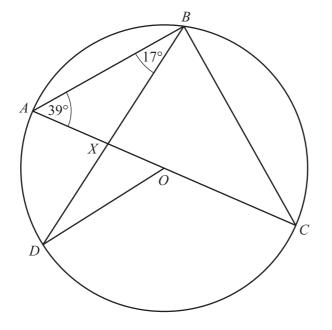
Calculate the length of AB.

Answer(a)(iv) AB = cm [3]

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NOT TO SCALE

A, B, C and D are on the circumference of the circle centre O. AC is a diameter.

Angle $CAB = 39^{\circ}$ and angle $ABD = 17^{\circ}$.

(i) Calculate angle *ACB*.

$$Answer(b)(i) Angle ACB =$$
 [2]

(ii) Calculate angle *BXC*.

$$Answer(b)(ii) Angle BXC =$$
 [2]

(iii) Give the reason why angle DOA is 34°.

$$Answer(b)(iii)$$
 [1]

(iv) Calculate angle *BDO*.

$$Answer(b)(iv) Angle BDO = [1]$$

(v) The radius of the circle is 12 cm. Calculate the length of major arc ABCD.

$$Answer(b)(v)$$
 Arc $ABCD =$ cm [3]

5 (a) A farmer takes a sample of 158 potatoes from his crop. He records the mass of each potato and the results are shown in the table.

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Mass (m grams)	Frequency
$0 < m \le 40$	6
$40 < m \le 80$	10
$80 < m \le 120$	28
$120 < m \le 160$	76
$160 < m \le 200$	22
$200 < m \le 240$	16

Calculate an estimate of the mean mass. Show all your working.

	_	
Answer(a)	g [41

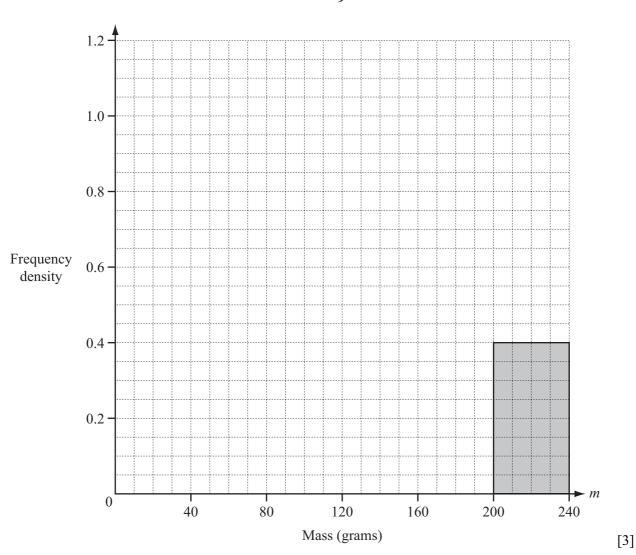
(b) A new frequency table is made from the results shown in the table in part (a).

Mass (<i>m</i> grams)	Frequency
$0 < m \le 80$	
$80 < m \le 200$	
$200 < m \le 240$	16

(i) Complete the table above.

[2]

(ii) On the grid opposite, complete the histogram to show the information in this new table.



(c) A bag contains 15 potatoes which have a mean mass of 136 g.

The farmer puts 3 potatoes which have a mean mass of 130 g into the bag.

Calculate the mean mass of all the potatoes in the bag.

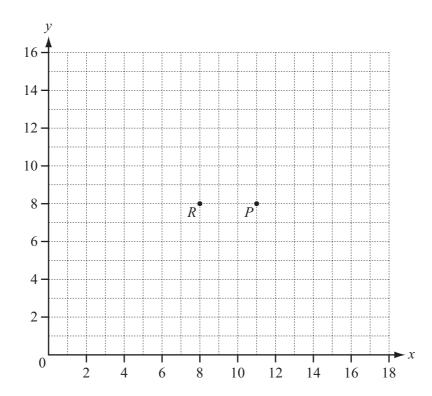
Answer(c) _____ g [3]

6 (a) Calculate the magnitude of the vector $\begin{pmatrix} 3 \\ -5 \end{pmatrix}$.

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Answer(a) [2]

(b)



(i) The points P and R are marked on the grid above.

$$\overrightarrow{PQ} = \begin{pmatrix} 3 \\ -5 \end{pmatrix}$$
. Draw the vector \overrightarrow{PQ} on the grid above. [1]

(ii) Draw the image of vector \overrightarrow{PQ} after rotation by 90° anticlockwise about R. [2]

(c)
$$\overrightarrow{DE} = 2\mathbf{a} + \mathbf{b}$$
 and $\overrightarrow{DC} = 3\mathbf{b} - \mathbf{a}$.

Find \overrightarrow{CE} in terms of **a** and **b**. Write your answer in its simplest form.

$$Answer(c) \overrightarrow{CE} =$$
 [2]

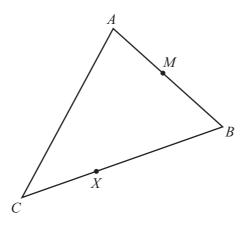
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(d)
$$\overrightarrow{OT} = \begin{pmatrix} -2\\5 \end{pmatrix}$$
 and $\overrightarrow{OV} = \begin{pmatrix} 5\\-1 \end{pmatrix}$.

Write \overrightarrow{TV} as a column vector.

$$Answer(d) \overrightarrow{TV} =$$
 [2]

(e)



NOT TO SCALE

 $\overrightarrow{AB} = \mathbf{b}$ and $\overrightarrow{AC} = \mathbf{c}$.

(i) Find \overrightarrow{CB} in terms of **b** and **c**.

$$Answer(e)(i) \overrightarrow{CB} =$$
 [1]

(ii) X divides CB in the ratio 1:3. M is the midpoint of AB.

Find \overrightarrow{MX} in terms of **b** and **c**. Show all your working and write your answer in its simplest form.

$$Answer(e)(ii) \overrightarrow{MX} = [4]$$

7 Jay makes wooden boxes in two sizes. He makes x small boxes and y large boxes.

He makes at least 5 small boxes.

The greatest number of **large** boxes he can make is 8.

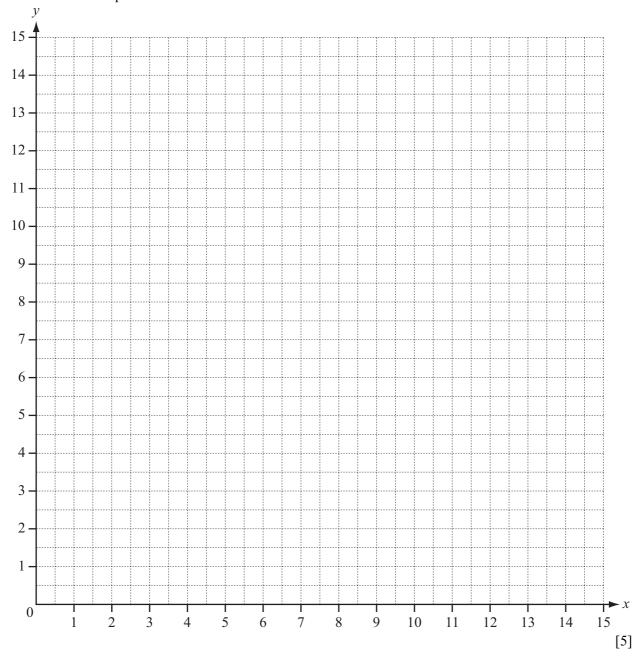
The greatest total number of boxes is 14.

The number of large boxes is at least half the number of small boxes.

(a) (i) Write down four inequalities in x and y to show this information.

Answer(a)(i)	
	 [4]

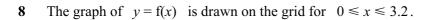
(ii) Draw four lines on the grid and write the letter R in the region which represents these inequalities.

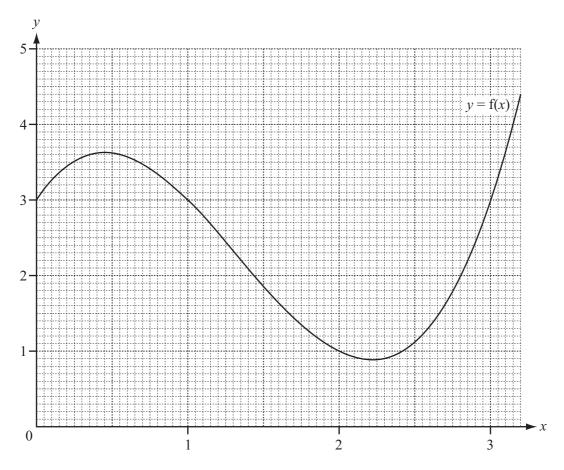


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(b)	The	e price of the small box is \$20 and the price of the large box is \$45. What is the greatest amount of money he receives when he sells all the boxes he has made?	For Examiner's Use
	(ii)	Answer(b)(i) \$ [2] For this amount of money, how many boxes of each size did he make?	
		Answer(b)(ii) small boxes and large boxes [1]	





- (a) (i) Draw the tangent to the curve y = f(x) at x = 2.5. [1]
 - (ii) Use your tangent to estimate the gradient of the curve at x = 2.5.

(b) Use the graph to solve f(x) = 2, for $0 \le x \le 3.2$.

(c)
$$g(x) = \frac{x}{2} + \frac{2}{x^2} \quad x \neq 0.$$

(i) Complete the table for values of g(x), correct to 1 decimal place.

x	0.7	1	1.5	2	2.5	3
g(x)			1.6		1.6	1.7

[2]

[3]

- (ii) On the grid opposite, draw the graph of y = g(x) for $0.7 \le x \le 3$.
- (iii) Solve f(x) = g(x) for $0.7 \le x \le 3$.

Answer(c) (iii)
$$x =$$
 or $x =$ or $x =$ [3]

		16	
9	(a) &=	= {25 students in a class}	
	F =	= {students who study French}	
	S =	{students who study Spanish}	
	16	students study French and 18 students study Spanish.	
	2 st	tudents study neither of these.	
	(i)	Complete the Venn diagram to show this information.	
	(ii)	Find $n(F')$.	[2]
	()	Answer(a)(ii)	[1]
	(iii)	Find $n(F \cap S)'$. Answer(a)(iii)	[1]
	(iv)	One student is chosen at random.	
		Find the probability that this student studies both French and Spanish.	
		Answer(a)(iv)	[1]
	(v)	Two students are chosen at random without replacement.	
	(.)	Find the probability that they both study only Spanish.	

Answer(a)(v) [2]

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(b)	In another class the students all study at least one language from French, German and Spanis	sh.
	No student studies all three languages.	
	The set of students who study German is a proper subset of the set of students who strench.	tudy
	4 students study both French and German.	
	12 students study Spanish but not French.	
	9 students study French but not Spanish.	
	A total of 16 students study French.	
	(i) Draw a Venn diagram to represent this information.	
		[4]
	(ii) Find the total number of students in this class.	
	Answer(b)(ii)	[1]

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4.0	~	•		. •			
10	Consecutive	integers	are set	out in	rows 1	n a	grid.

(a) This grid has 5 columns.

1	2	3	4	5
6	7	8	9	10
11	12	13	14	15
16	17	18	19	20
0.1	22	22	2.4	2.5

а		b
	n	
С		d

21 22 23 24 25

26 27 28 29 30

31 32 33 34 35

The shape drawn encloses five numbers 7, 9, 13, 17 and 19. This is the n = 13 shape.

In this shape, a = 7, b = 9, c = 17 and d = 19.

(i) Calculate bc - ad for the n = 13 shape.

Answer(a)(i) [1]

(ii) For the 5 column grid, a = n - 6.

Write down b, c and d in terms of n for this grid.

Answer(a)(ii) b =

c =

d = [2]

(iii) Write down bc - ad in terms of n. Show clearly that it simplifies to 20.

Answer(a)(iii)

[2]

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(b) This grid has 6 columns. The shape is drawn for n = 10.

1	2	3	4	5	6
7	8	9	10	11	12
13	14	15	16	17	18
19	20	21	22	23	24
25	26	27	28	29	30
31	32	33	3/1	35	36

а		b
	n	
c		d

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(i) Calculate the value of bc - ad for n = 10.

Answer(b)(i) [1]

(ii) Without simplifying, write down bc - ad in terms of n for this grid.

Answer(b)(ii) [2]

(c) This grid has 7 columns.

1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28

32

33

34

35

a		b
	n	
c		d

Show clearly that bc - ad = 28 for n = 17.

30

31

29

Answer(c)

[1]

Question 10 continues on the next page.

(d)	Write down	the value of	bc - ad	when there are	t columns	in the	orid
(u)	WITHE GOWII	me value of	vc - aa	when there are	<i>t</i> Columns	s iii uie	gria

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 $Answer(d) \qquad [1]$

(e) Find the values of c, d and bc - ad for this shape.

2	3	4
	16	
c		d

Answer (e) c =

d =

bc - ad = [2]

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