

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

8032785298

MATHEMATICS 0581/41

Paper 4 (Extended) October/November 2012

2 hours 30 minutes

Candidates answer on the Question Paper.

Additional Materials: Electronic calculator Geometrical instruments

Mathematical tables (optional) Tracing paper (optional)

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 130.

International Examinations

1

A or A^* NOT TO SCALE $A ext{ or } D$ $A ext{ or } A^*$

Boys

For Examiner's Use

The pie charts show information on the grades achieved in mathematics by the girls and boys at a school.

(a) For the Girls' pie chart, calculate

Girls

(i) x,

B, C or D

 $(x+18)^{\circ}$

A or *A**

E, F or G

$$Answer(a)(i) x =$$
 [2]

(ii) the angle for grades B, C or D.

(b) Calculate the percentage of the **Boys** who achieved grades E, F or G.

- (c) There were 140 girls and 180 boys.
 - (i) Calculate the percentage of students (girls and boys) who achieved grades A or A^* .

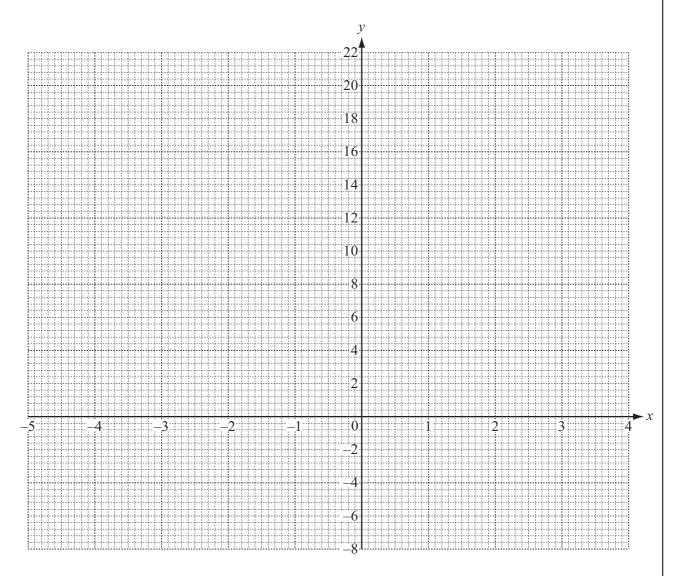
 $Answer(c)(i) \qquad \qquad \% [3]$

(ii) How many more boys	(ii) How many more boys than girls achieved grades B , C or D ?				
		Answ	<i>er(c)</i> (ii)		[2]
		71115 W			[2]
d) The table shows informat their mathematics examina		mes, t minutes,	, taken by 80 of	the girls to comp	lete
Time taken (t minutes)	$40 < t \le 60$	$60 < t \le 80$	80 < <i>t</i> ≤ 120	$120 < t \le 150$	
Frequency	5	14	29	32	
(i) Calculate an estimate	of the mean tim	e taken by these	e 80 girls to comp	olete the examinati	on.
		Answ	<i>ver(d)</i> (i)	min	[4]
(ii) On a histogram, the h	eight of the colu	ımn for the inter	rval $60 < t \le 80$	is 2.8 cm.	
Calculate the heights Do not draw the hist		e columns.			
Answe	er(d)(ii) $40 < 1$	$t \le 60 \text{ column } 1$	neight =	cm	
	80 < t	≤ 120 column l	neight =	cm	
	120 < <i>t</i>	≤ 150 column l	neight =	cm	[4]

[3]

х	-5	-4	-3	-2	-1	0	1	2	3	4
у	-2.5	12	16.5		7.5	0		-6	1.5	

(ii) On the grid, draw the graph of $y = \frac{1}{2}x^3 + x^2 - 7x$ for $-5 \le x \le 4$.



[4]

(b) Use your graph to solve the equation $\frac{1}{2}x^3 + x^2 - 7x = 2$.

(c)	By drawing a suitable tangent	calculate an estimate of the	e gradient of the graph where $x = -4$.
-----	-------------------------------	------------------------------	--

(d) (i) On the grid draw the line
$$y = 10 - 5x$$
 for $-2 \le x \le 3$. [3]

(ii) Use your graphs to solve the equation
$$\frac{1}{2}x^3 + x^2 - 7x = 10 - 5x$$
.

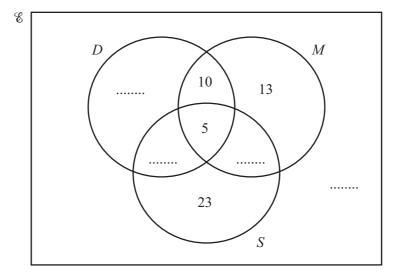
$$Answer(d)(ii) x =$$
 [1]

3 90 students are asked which school clubs they attend.

Examiner's Use

[4]

- $D = \{\text{students who attend drama club}\}\$
- $M = \{$ students who attend music club $\}$
- $S = \{ \text{ students who attend sports club} \}$
- 39 students attend music club.
- 26 students attend exactly two clubs.
- 35 students attend drama club.



- (b) How many students attend
 - (i) all three clubs,

Answer(b)(i)	[1]
11.10.110.101	 L * J

(ii) one club only?

$$Answer(b)(ii)$$
 [1]

(c) Find

(i) $n(D \cap M)$,

 $Answer(c)(i) \qquad [1]$

(ii) $n((D \cap M) \cap S')$.

Answer(c)(ii) [1]

(d)	One	e of the 90 students is chosen at random.	For Examiner's
	Fine	d the probability that the student	Use
	(i)	only attends music club,	
	(ii)	Answer(d)(i) [1] attends both music and drama clubs.	I
		<i>Answer(d)</i> (ii)[1]	
(e)	Two	o of the 90 students are chosen at random without replacement.	
	Fine	d the probability that	
	(i)	they both attend all three clubs,	
	(ii)	Answer(e)(i)[2] one of them attends sports club only and the other attends music club only.	
		Answer(e)(ii)[3]	 -

4	(a)	Solve the equati	ons
		(i) $4x - 7 = 8$	- 2 <i>x</i>

$$Answer(a)(i) x =$$
 [2]

(ii)
$$\frac{x-7}{3} = 2$$

$$Answer(a)(ii) x =$$
 [2]

- **(b)** Simplify the expressions.
 - (i) $(3xy^4)^3$

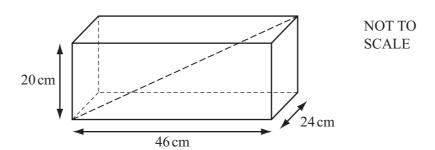
$$Answer(b)(i)$$
 [2]

(ii)
$$(16a^6b^2)^{\frac{1}{2}}$$

(iii)
$$\frac{x^2 - 7x - 8}{x^2 - 64}$$

© UCLES 2012

5 (a)



For Examiner's Use

Jose has a fish tank in the shape of a cuboid measuring 46 cm by 24 cm by 20 cm.

Calculate the length of the diagonal shown in the diagram.

Answer(a)	cm	[3]	
		L- J	

(b) Maria has a fish tank with a volume of 20 000 cm³.

Write the volume of Maria's fish tank as a percentage of the volume of Jose's fish tank.

(c) Lorenzo's fish tank is mathematically similar to Jose's and double the volume.

Calculate the dimensions of Lorenzo's fish tank.

(d) A sphere has a volume of 20 000 cm³. Calculate its radius. [The volume, V, of a sphere with radius r is $V = \frac{4}{3}\pi r^3$.]

6 (a)
$$\mathbf{a} = \begin{pmatrix} -2 \\ 3 \end{pmatrix}$$
 $\mathbf{b} = \begin{pmatrix} 2 \\ -7 \end{pmatrix}$ $\mathbf{c} = \begin{pmatrix} -10 \\ 21 \end{pmatrix}$

(i) Find $2\mathbf{a} + \mathbf{b}$.

 $Answer(a)(i) \qquad \qquad \boxed{ \qquad }$

(ii) Find $|\mathbf{b}|$.

Answer(a)(ii) _____ [2]

(iii) $m\mathbf{a} + n\mathbf{b} = \mathbf{c}$

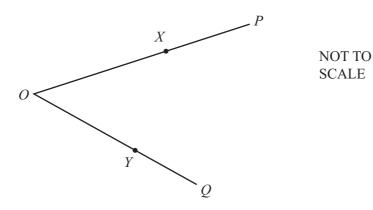
Find the values of *m* and *n*. Show all your working.

Answer(a)(iii) m =

n = [6]

(b)

For Examiner's Use



In the diagram, OX:XP = 3:2 and OY:YQ = 3:2. $\overrightarrow{OP} = \mathbf{p}$ and $\overrightarrow{OQ} = \mathbf{q}$.

(i) Write \overrightarrow{PQ} in terms of **p** and **q**.

 $Answer(b)(i) \overrightarrow{PQ} =$ [1]

(ii) Write \overrightarrow{XY} in terms of **p** and **q**.

 $Answer(b)(ii) \overrightarrow{XY} =$ [1]

(iii) Complete the following sentences.

The lines XY and PQ are

The triangles *OXY* and *OPQ* are

The ratio of the area of triangle *OXY* to the area of triangle *OPQ* is [3]

7

W A X NOT TO SCALE

B
O
7 cm

For Examiner's Use

The vertices A, B, C, D and E of a regular pentagon lie on the circumference of a circle, centre O, radius 7 cm.

They also lie on the sides of a rectangle WXYZ.

- (a) Show that
 - (i) angle $DOC = 72^{\circ}$,

Answer(a)(i)

[1]

(ii) angle $DCB = 108^{\circ}$,

Answer(a)(ii)

[2]

(iii) angle $CBY = 18^{\circ}$.

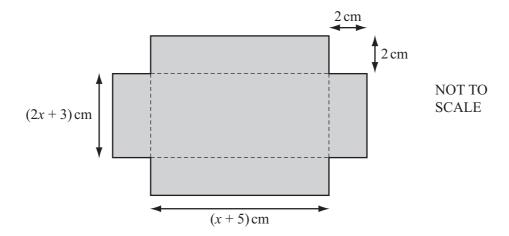
Answer(a)(iii)

[1]

(b)	figures.	of the pentagon is 8.23 cm correct to three significant	For Examiner's Use
	Answer(b)		
(c)	Calculate (i) the area of the triangle <i>DOC</i> ,	[3]	
	(i) the area of the triangle 2000,		
	(ii) the area of the pentagon ABCDE,	Answer(c)(i) cm^2 [2]	
	(iii) the area of the sector <i>ODC</i> ,	Answer(c)(ii) cm ² [1]	
	(iv) the length XY.	Answer(c)(iii) cm ² [2]	
(d)	Calculate the ratio	Answer(c)(iv) cm [2]	
	area of the pentagon $ABCDE$: Give your answer in the form $1:n$.	area of the rectangle WXYZ.	
		$Answer(d) 1: \qquad \qquad [5]$	

8 A rectangular piece of card has a square of side 2 cm removed from each corner.

For Examiner's Use



(a) Write expressions, in terms of x, for the dimensions of the rectangular card before the squares are removed from the corners.

Answer(a) cm by cm [2]

(b) The diagram shows a net for an open box. Show that the volume, $V \text{cm}^3$, of the open box is given by the formula $V = 4x^2 + 26x + 30$.

Answer(b)

[3]

(c)	(i)	Calculate the values of x when $V = 75$. Show all your working and give your answers correct to two decimal places.
		Answer(c)(i) x =
	(ii)	Write down the length of the longest edge of the box.
		Answer(c)(ii) cm [1]

Question 9 is printed on the next page.

9 Distances from the Sun can be measured in astronomical units, AU. Earth is a distance of 1 AU from the Sun. One AU is approximately 1.496×10^8 km.

For Examiner's Use

The table shows distances from the Sun.

Name	Distance from the Sun in AU	Distance from the Sun in kilometres
Earth	1	1.496 × 10 ⁸
Mercury	0.387	
Jupiter		7.79 × 10 ⁸
Pluto		5.91 × 10 ⁹

(a)	Complete the table.						[3]
(b)	Light travels at approximately 300 000 kilometres per second.						
	(i)		oes it take ligh nswer in secon	nt to travel from the	e Sun to Earth?		
					Answer(b)(i)		s [2]
	(ii)		oes it take ligh nswer in minu	t to travel from the tes.	e Sun to Pluto?		
					Answer(b)(ii)	·1	min [2]
(c)	One light year is the distance that light travels in one year (365 days).						
	How far is one light year in kilometres? Give your answer in standard form.						
					Answer(c)		km [3]
(d)	How many astronomical units (AU) are equal to one light year?						

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

Answer(d)

AU [2]

University of Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.